

# SAT-based Program Synthesis

**Ruben Martins**

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**Carnegie  
Mellon  
University**

# What is Program Synthesis?

**Specifications  $\phi$**



**Program  $P$**



$$\exists P. \forall x. \phi(x, P(x))$$

- Find a program  $P$  that for all inputs  $x$  meets the specification  $\phi$



# Programming by Examples

Email	→	First Name
<u>Nancy.Freehafer@fourthcoffee.com</u>		Nancy
<u>Andrew.Cencini@northwindtraders.com</u>		Andrew
<u>Jan.Kotas@itwareinc.com</u>		Jan
<u>Mariya.Sergienko@graphicdesigns.com</u>		Mariya
<u>Alexander.David@contoso.com</u>		Alexander
<u>Amr.Zaid@traders.com</u>		Amr



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- Flash Fill (Excel 2013 feature):
  - Automating **string processing** in spreadsheets using input-output examples. POPL 2011



# Programming by Examples

Name	Month	Rate1	Rate2
Aira	1	12	23
Aira	2	18	73
Ben	1	53	19
Ben	2	22	87
Cat	1	22	87
Cat	2	67	43



Name	avg1	avg2
Aira	15.0	48
Ben	37.5	53
Cat	44.5	65

- Can we find a program that automatically **transforms tables** given input-output examples?



# Programming by Examples

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R program:

```
TBL_15=group_by(p8_input1, `Name`)  
TBL_7=summarise(TBL_15, avg2=mean(`Rate2`))  
TBL_3=inner_join(TBL_7, p8_input1)  
TBL_1=group_by(TBL_3, `Name`, `avg2`)  
morpheus=summarise(TBL_1, avg1=mean(`Rate1`))  
morpheus=select(morpheus, 1, 3, 2)
```

- Component-based synthesis of **table consolidation** and **transformation** tasks from examples. PLDI 2017



# Programming by Examples

- Can we find a **sequence of API calls** using **java.time** in Java 8 to get the day from a Date in string format?

```
public static int getDayFromString(String date, String pat) {
```

```
}
```

```
public static boolean test() {  
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- Component-based **synthesis for complex APIs**. POPL 2017





# Who can Program Synthesis help?



# Who can Program Synthesis help?

- Are we trying to replace programmers? **No!**
- We want to make programmers life easier
- Automating tedious and repetitive tasks



# Who can Program Synthesis help?



- Are we trying to replace programmers? **No!**
  - We want to make programmers life easier
  - Automating tedious and repetitive tasks
- 99% of computer users **cannot program!**
  - They struggle with simple repetitive tasks
  - Help non-CS people to automate their daily tasks



# How do Program Synthesizers Work?



**Enumerative Search**



**Stochastic Search**



**Constraint Solving**



# How do Program Synthesizers Work?



**Enumerative Search**



**Stochastic Search**



**Constraint Solving**

- Combinatorial search for all possible programs



# How do Program Synthesizers Work?



**Enumerative Search**



**Stochastic Search**



**Constraint Solving**

- Build a statistical models using large corpora
- Guide the search using statistical models



# How do Program Synthesizers Work?



**Enumerative Search**



**Stochastic Search**



**Constraint Solving**

- Encode the synthesis problem to SAT/SMT
- Prune infeasible incomplete programs with logical deduction



# Outline

- Examples of Synthesizers
- Synthesis of Java programs
- Conflict-driven Synthesis





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# Microsoft Program Synthesis using Examples SDK

A framework for automatic programming or data wrangling from input-output examples.

Latest version: [📄 Release notes](#) [📦 NuGet package](#) [🔧 Yeoman generator](#) [🔗 Samples](#)  
**6.20.1**

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## Program Synthesis Framework

Microsoft PROSE SDK is a framework of technologies for *programming by examples*: automatic generation of programs from input-output examples at runtime.

Given a domain-specific language (DSL) and some input-output examples for the desired program's behavior, PROSE synthesizes a ranked set of DSL programs that are consistent with the examples.

## Data Wrangling DSLs

PROSE SDK includes a pre-defined suite of technologies for various kinds of *data wrangling* – cleaning and pre-processing raw semi-structure data into a form amenable to analysis:

- [Flash Fill](#), a technology for *text transformation by examples*, available in [Microsoft Excel](#) and [PowerShell](#).
- *Data extraction from text files by examples*, available in [PowerShell](#) and [Azure Log Analytics](#).
- *Data extraction and transformation of JSON by examples*.
- *Predictive file splitting* technology, which splits a text file into the structured columns without any examples.



# Demo PROSE

<https://microsoft.github.io/prose/>



# Microsoft PROSE



Program synthesis in a real-world scenario



Very efficient for string manipulations



Provides a ranking for the most likely solutions



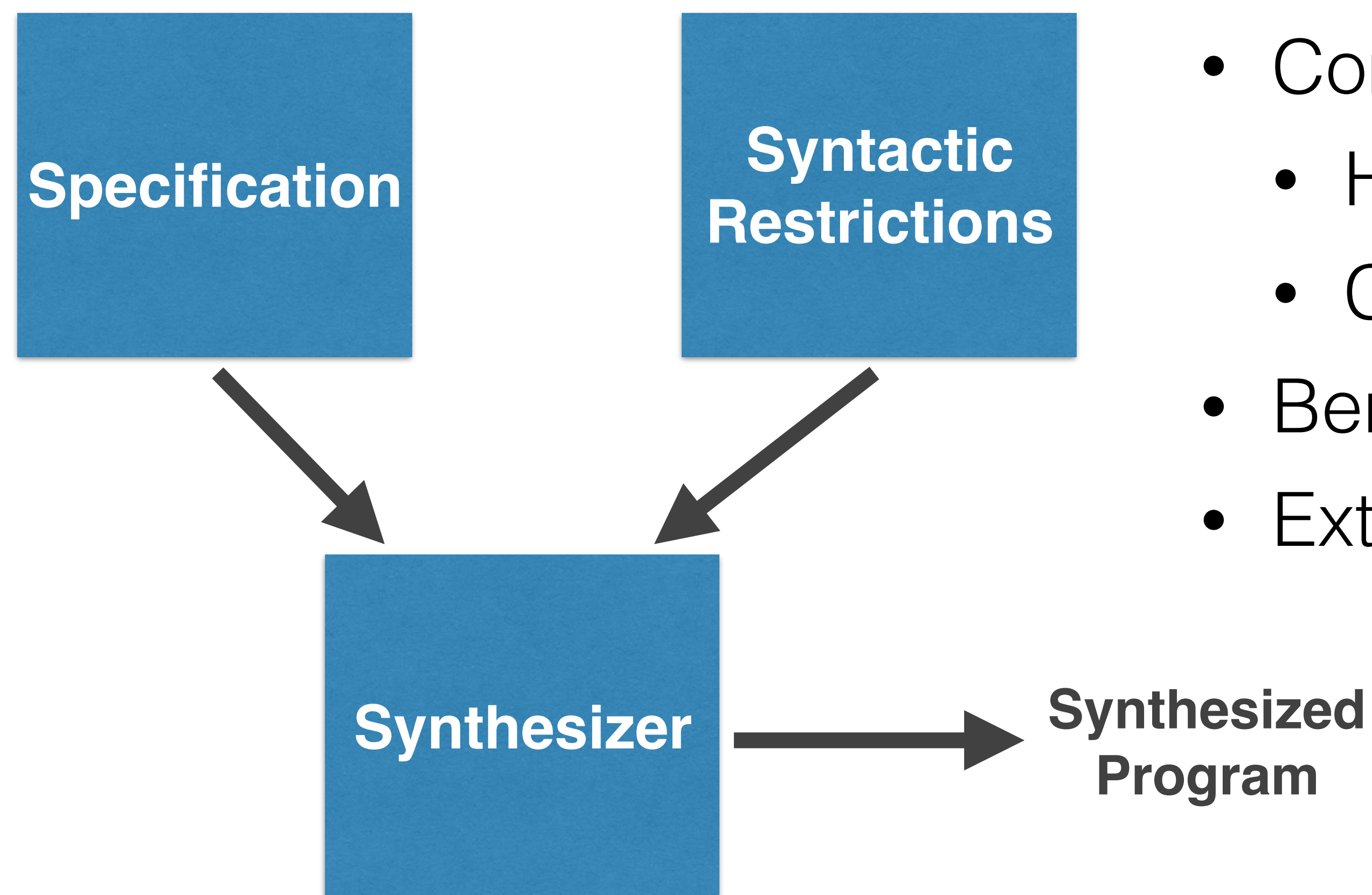
Requires witness functions for pruning the search space



Hard to extend to other domains



# Syntax-Guided Synthesis (SyGuS)

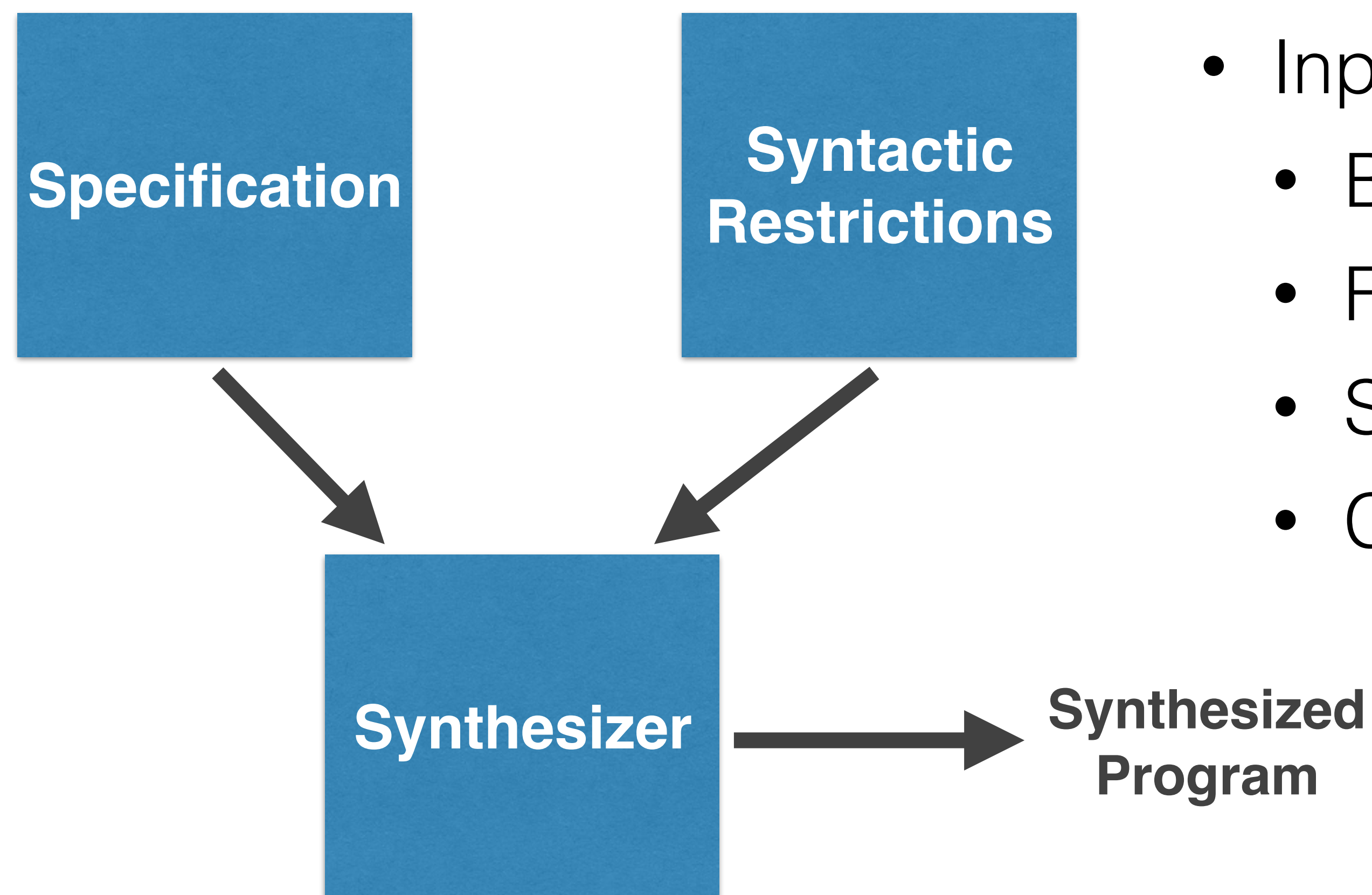


- Combine:
  - Human expert insights
  - Constraint solving
- Benefit from progress in SAT / SMT
- Extends SMT-LIB to SYNTH-LIB

- Syntax-Guided Synthesis. FMCAD 2013



# Syntax-Guided Synthesis (SyGuS)



- Inputs to SyGuS:
  - Background theory
  - Function to be synthesized
  - Specification
  - Context-free grammar



(set-logic LIA)



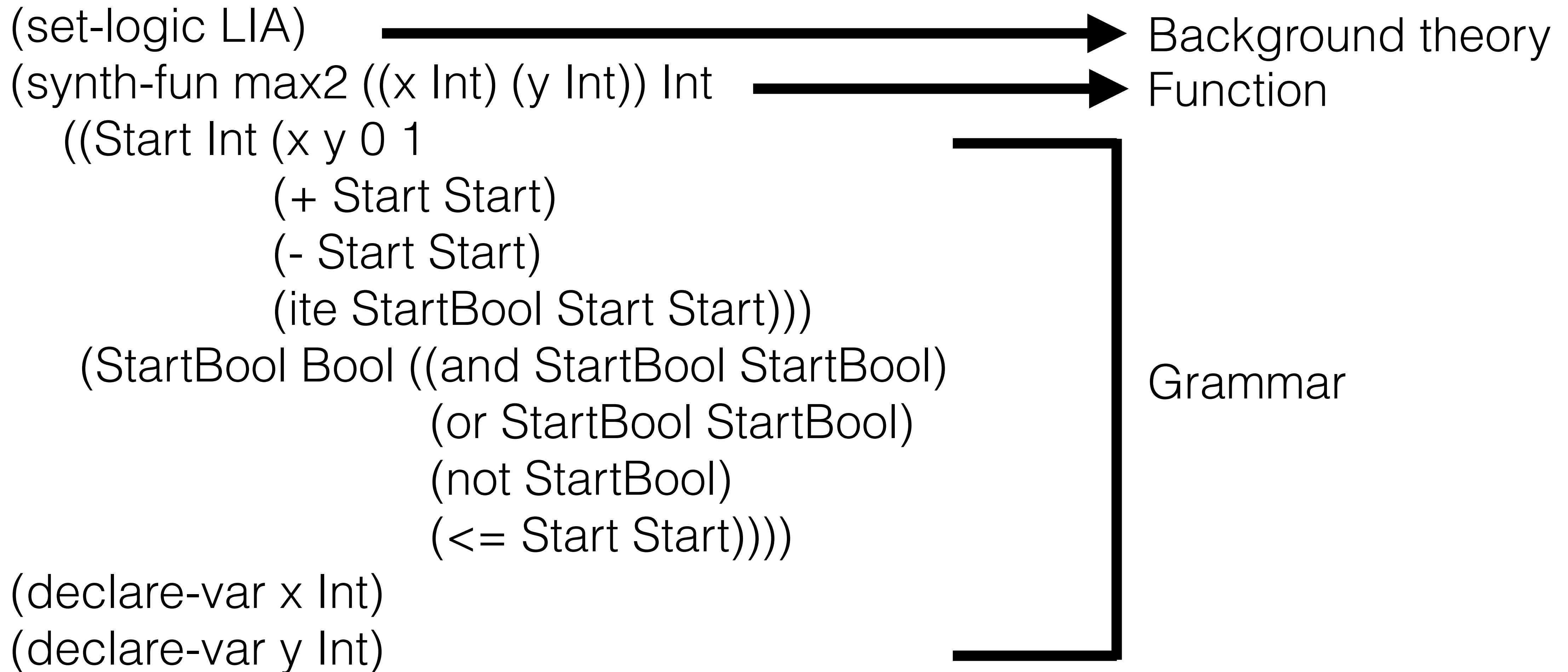
Background theory

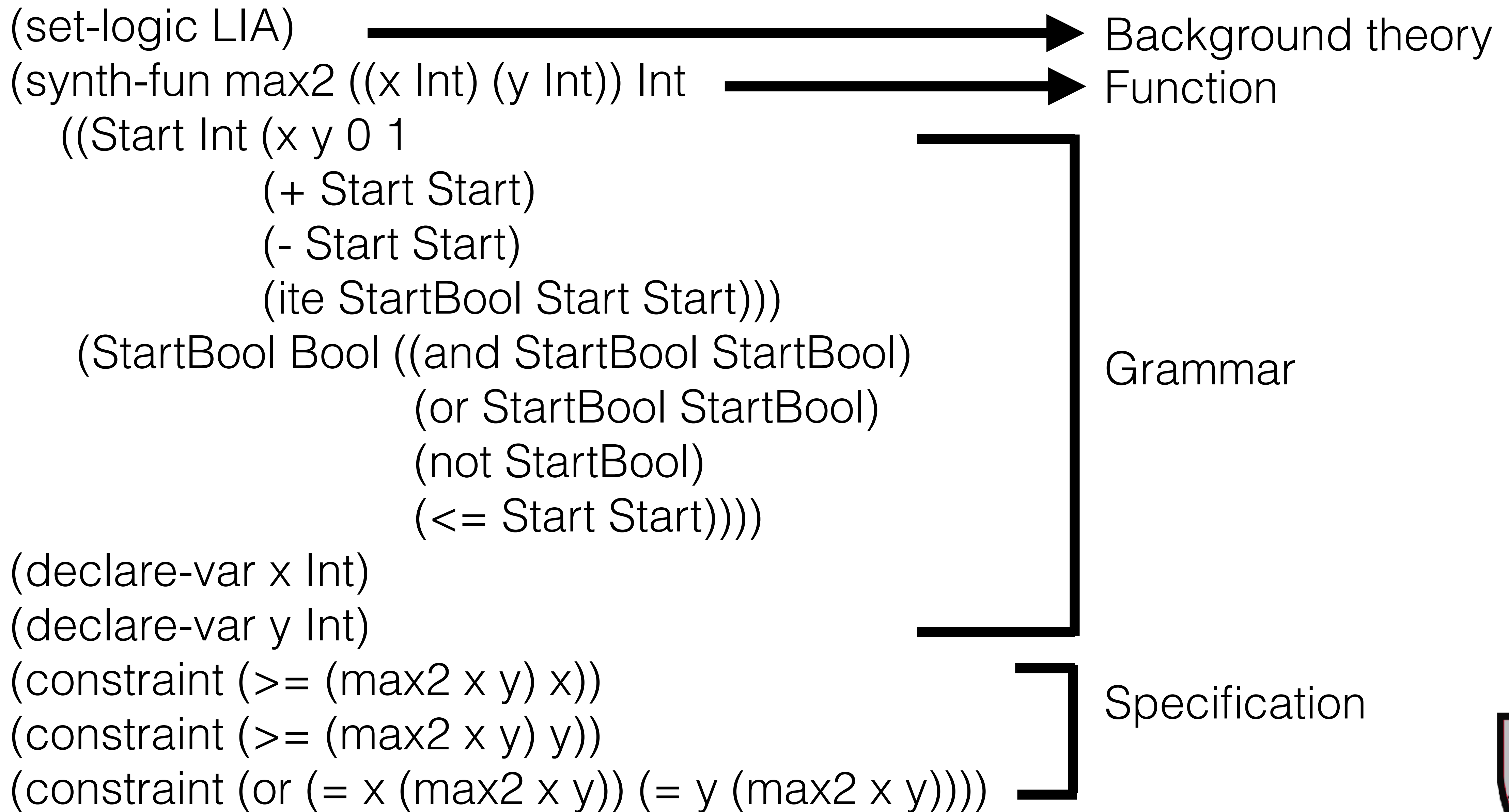


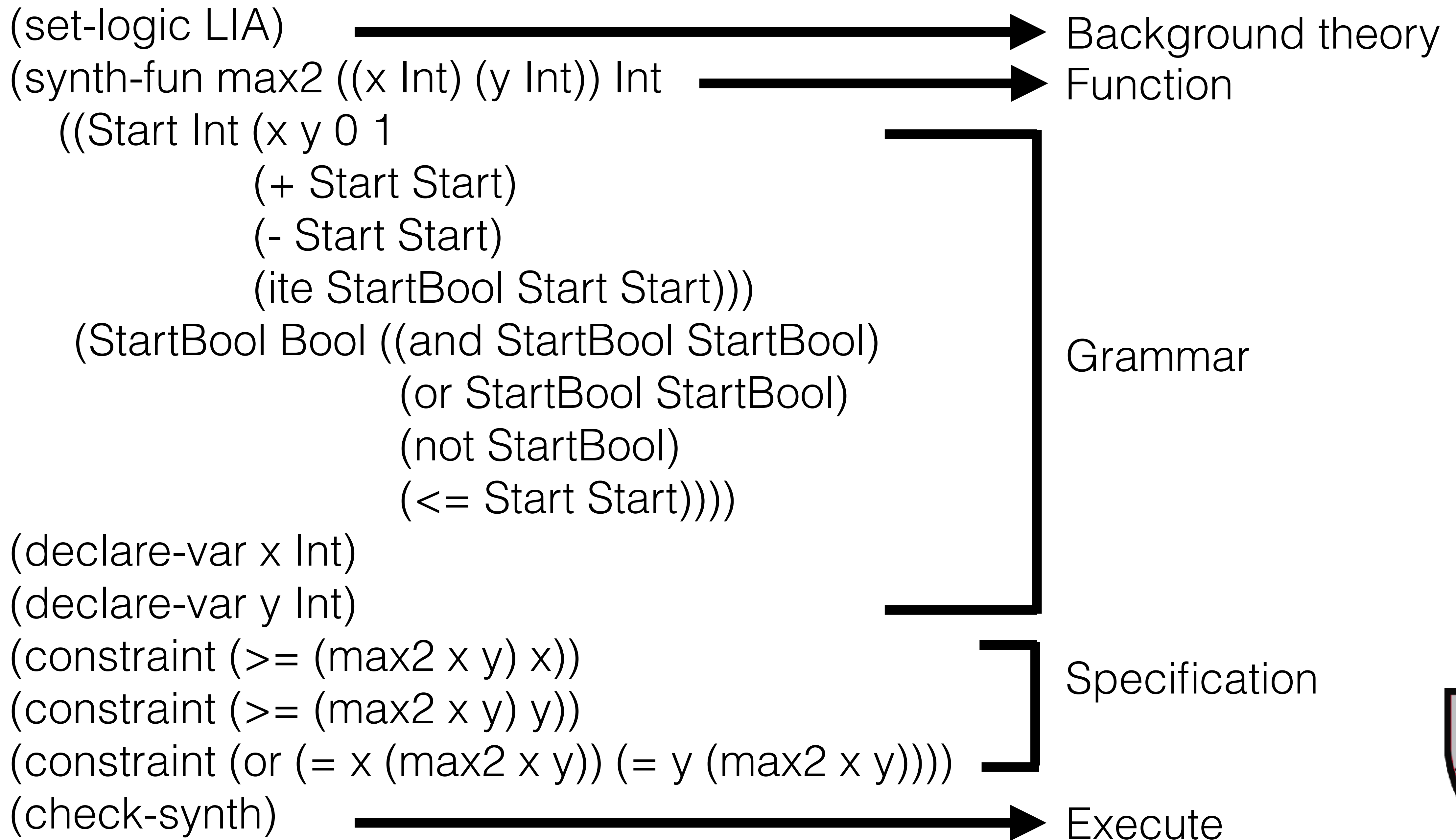
(set-logic LIA)  $\longrightarrow$  Background theory  
(synth-fun max2 ((x Int) (y Int)) Int)  $\longrightarrow$  Function











# Demo SyGus

<http://sygus.seas.upenn.edu/>



# Syntax-Guided Synthesis



Input is not specific to any synthesis problem



Specifications allows for human insights



Leverages the advances in SAT / SMT solving



Theories are restricted to SMT-LIB



Does not scale for large grammars



# Program Synthesis as Sketching

```
harness void doubleSketch(int x){  
    int t = x * ??;  
    assert t == x + x;  
}
```

- **Sketch** of the program:
  - Partial program with **holes** (“??”)
  - Synthesizer finds values to the holes that satisfies the specifications
  - Uses SAT / SMT technology to find the missing values
- Programming by sketching for bit-streaming programs. PLDI 2005



# Demo Sketch

<https://people.csail.mit.edu/asolar/>



# Sketching



Synthesis real-world code (C, Java)



Specifications allows for human insights



Leverages the advances in SAT / SMT solving



Holes must be expressed by SMT theories



Writing the sketch may be as hard as writing the program





# Synthesis of Java programs



```
import java.util.Random;
public final class RandomInteger {
    public static void main(String[] args){
        log("Generating 10 random integers in range 0..99.");
        Random randomGenerator = new Random();
        for (int idx = 1; idx <= 10; idx++){
            int randomInt = randomGenerator.nextInt(100);
            log("Generated: " + randomInt);
        }
        log("Done.");
    }
    private static void log(String msg){
        System.out.println(msg);
    }
}
```



**Send HTTP request**  
**Compute GCD**  
**Rotate an image**

Programmers spend a lot of effort  
learning APIs!

- Component-based synthesis for complex APIs. POPL 2017



# Synthesizing Programs with APIs

```
public static int getDayFromString(String date, String pat) {  
  
  
  
  
}
```



```
public static boolean test() {  
    return (getDayFromString("2013/06/13", "yyyy/MM/dd") == 13);  
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# Synthesizing Programs with APIs

```
public static int getDayFromString(String date, String pat) {  
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# Demo SyPet

<https://utopia-group.github.io/sypet/>



# SyPet



Works for real-world code



Can handle any Java library



Scales for large libraries



Does not work well for libraries with few types



Does not support loops or conditionals



# Outline

- Introduction to Syntax-Guided Synthesis (SyGus)

- Synthesis of Java code

- Conflict-driven Synthesis



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Use **Petri net reachability** analysis to look for well-typed programs of the desired type



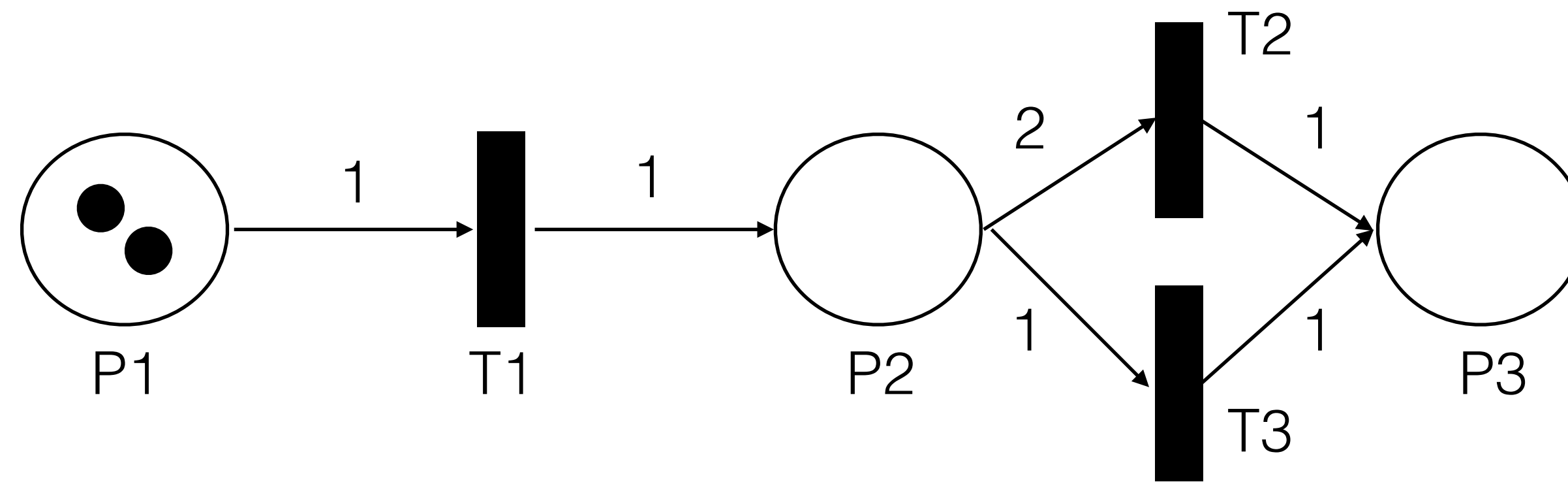
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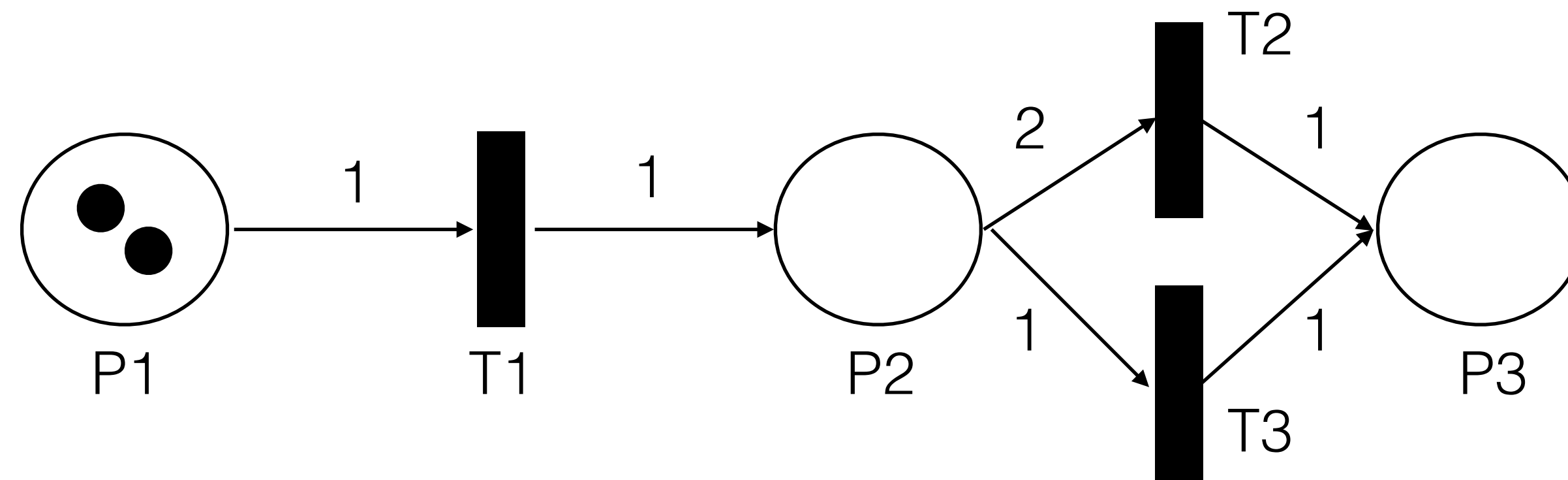
- Model relationships between APIs using Petri nets
- Use type signature of desired method to mark **initial** and **target** configurations
- Perform **reachability analysis** to find valid sequences of method calls



# Petri Nets in a Nutshell



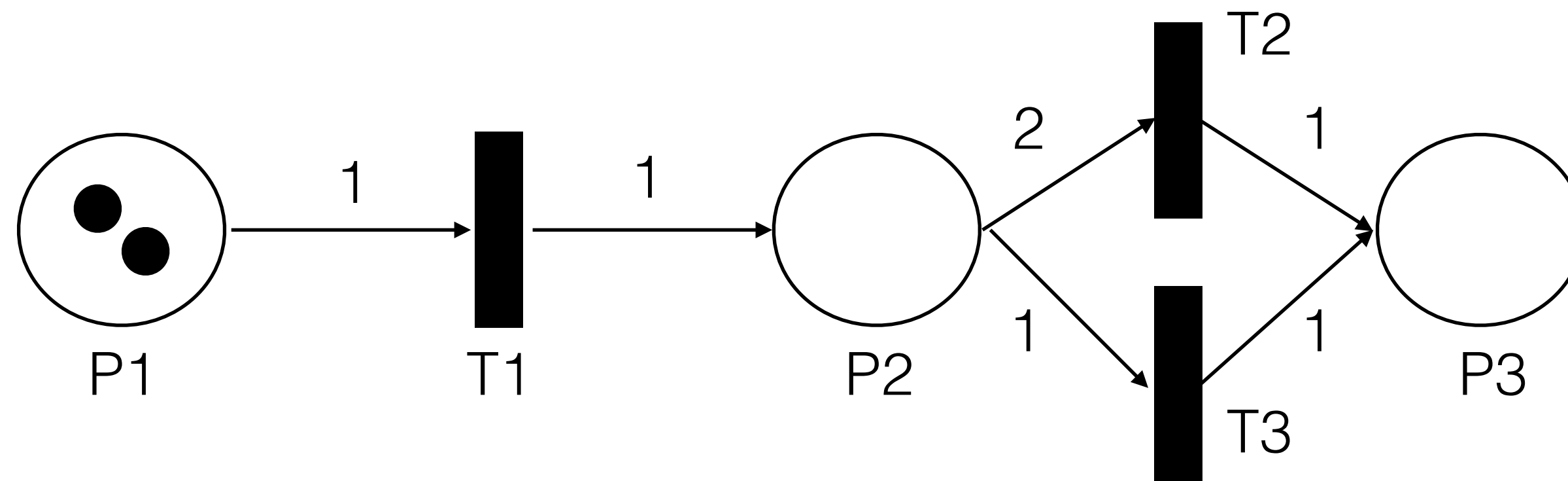
# Petri Nets in a Nutshell



- Petri net is a generalized graph with two kinds of nodes: **places** and **transitions**



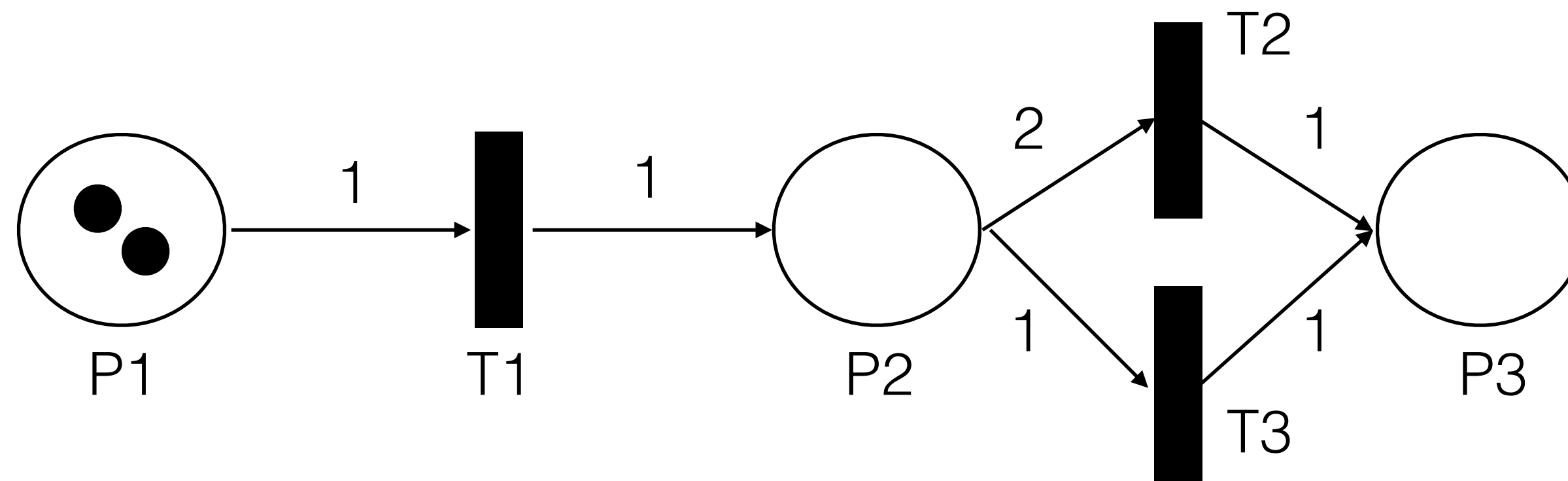
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- Each place contains zero or more tokens; edges are labeled with a number of tokens



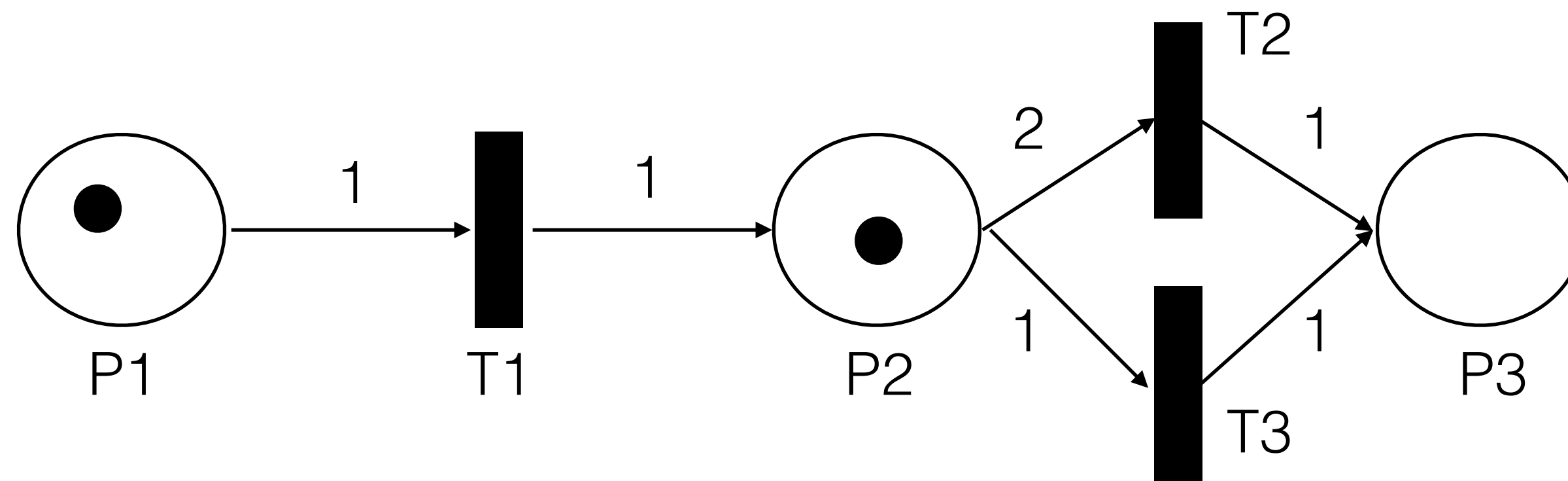
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- A transition  $T$  **can fire if**, for each incoming edge  $(p, T)$  with label  $n$ , place  $p$  **contains at least**  $n$  tokens
- **Firing** a transition  $T$  **consumes** (resp. produces) the indicated number of tokens at the source (resp. target) nodes



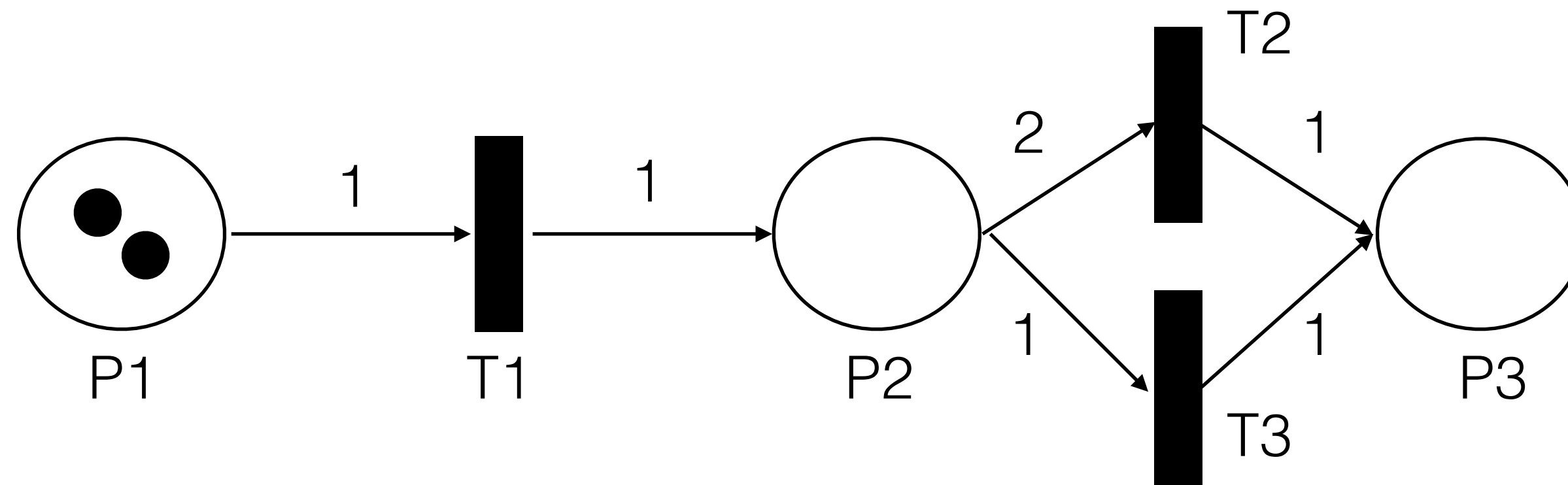
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# Reachability Problem in Petri Nets

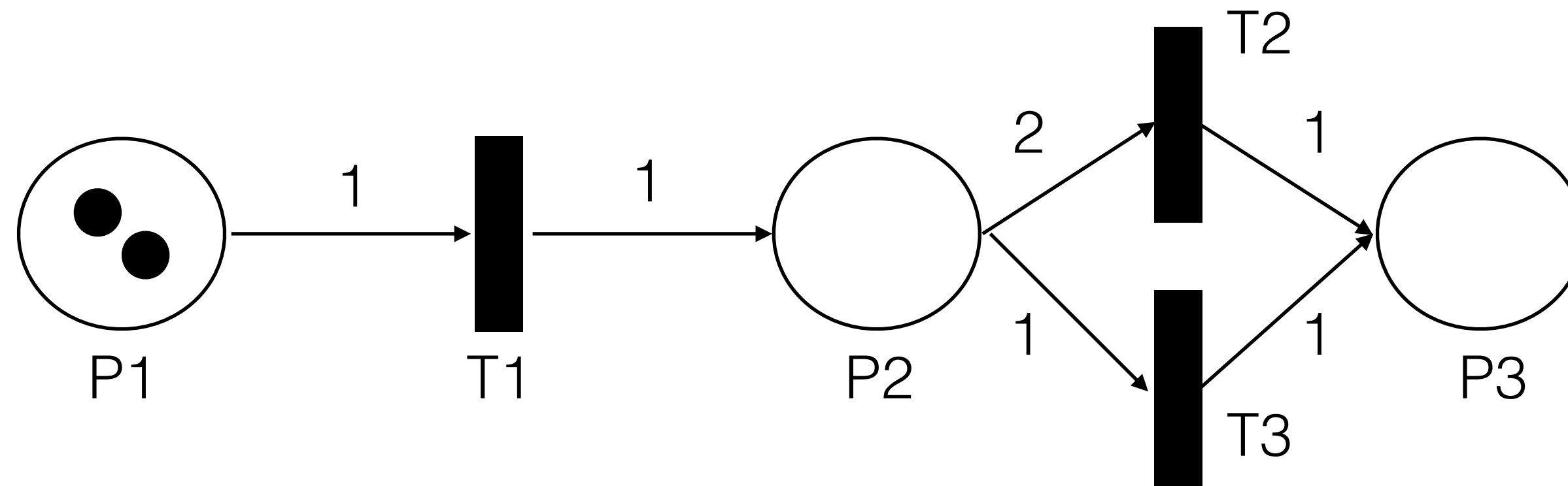


- **Reachability problem:** Given a Petri net with initial marking  $M$  and a target marking  $M'$ , is it possible to obtain  $M'$  by firing a sequence of transitions?





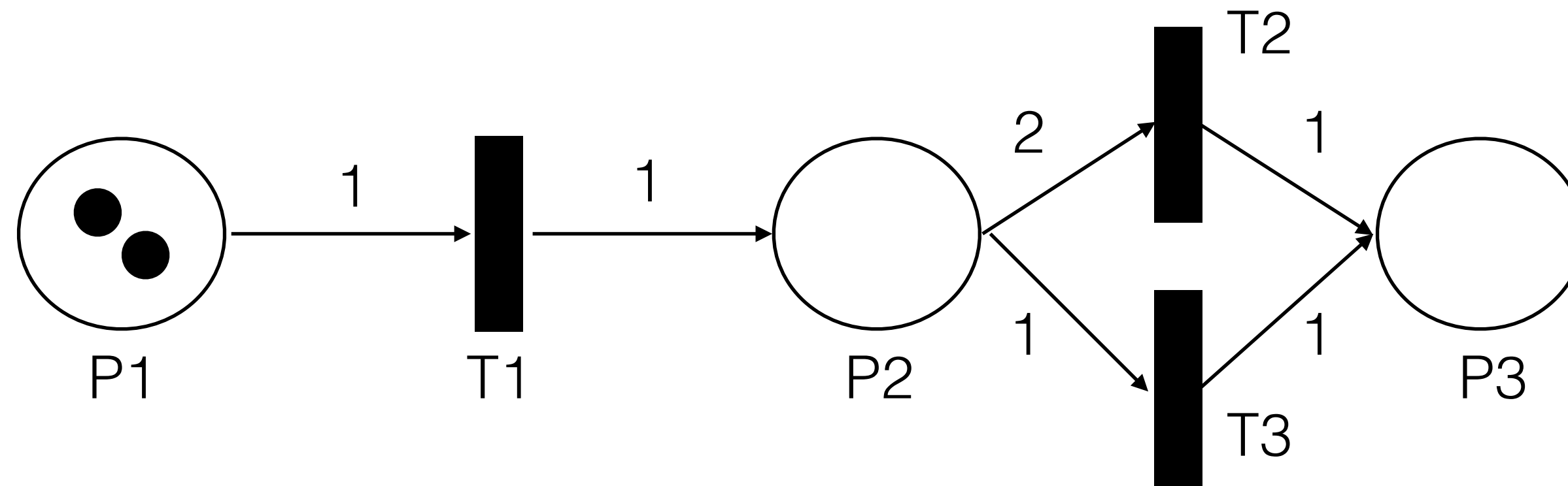
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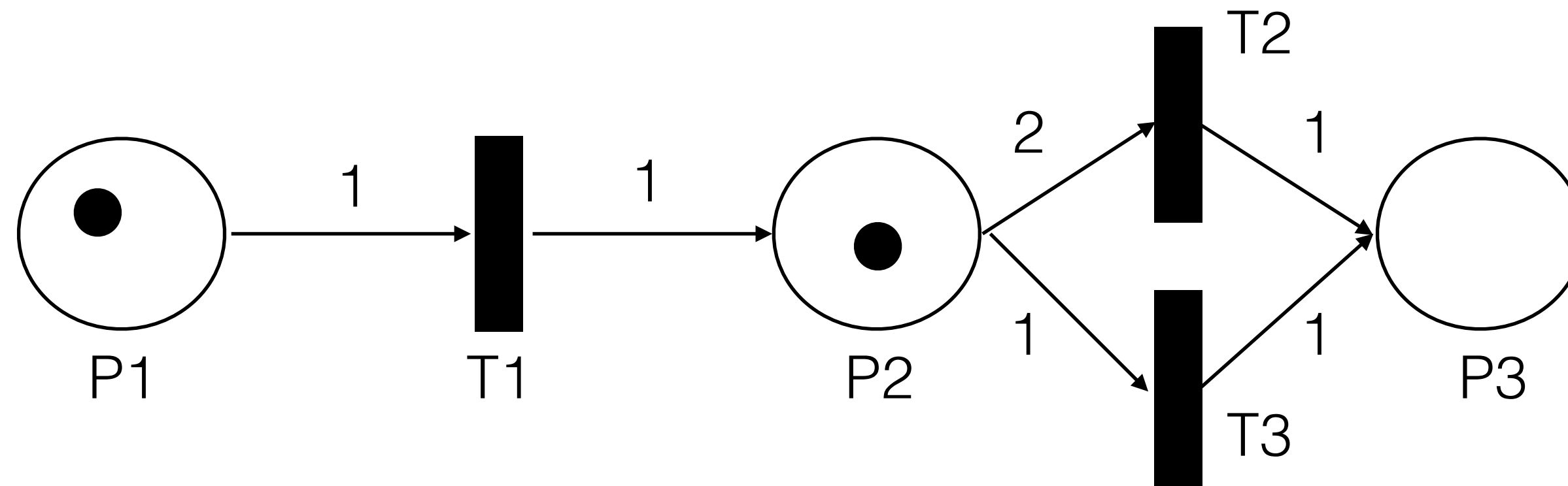
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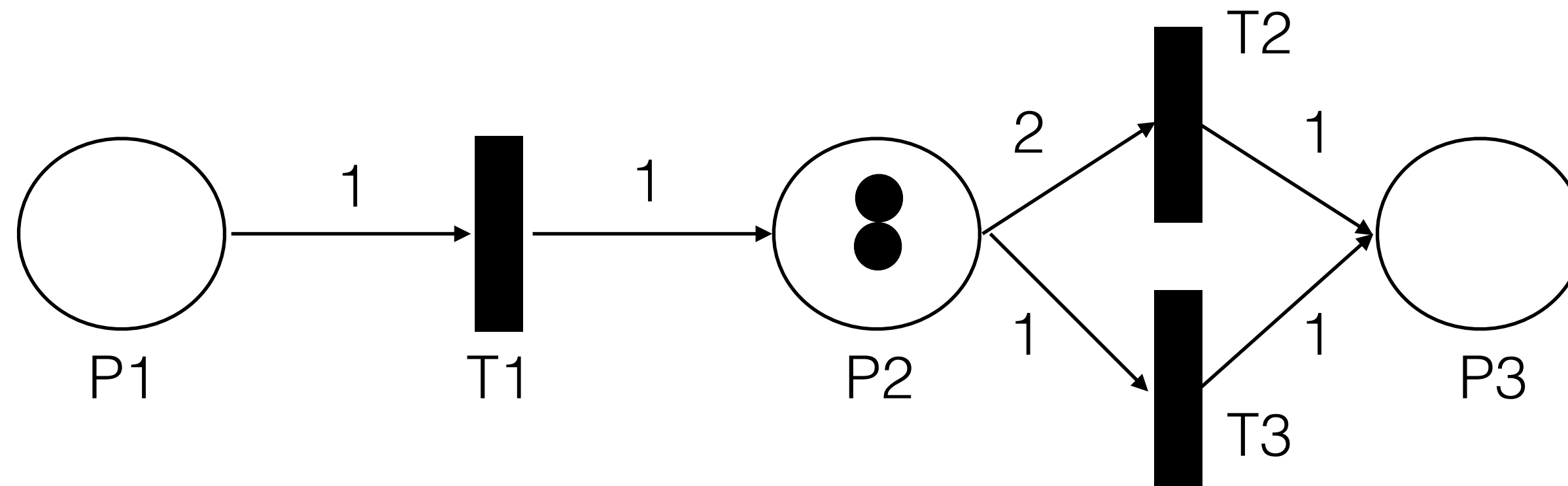
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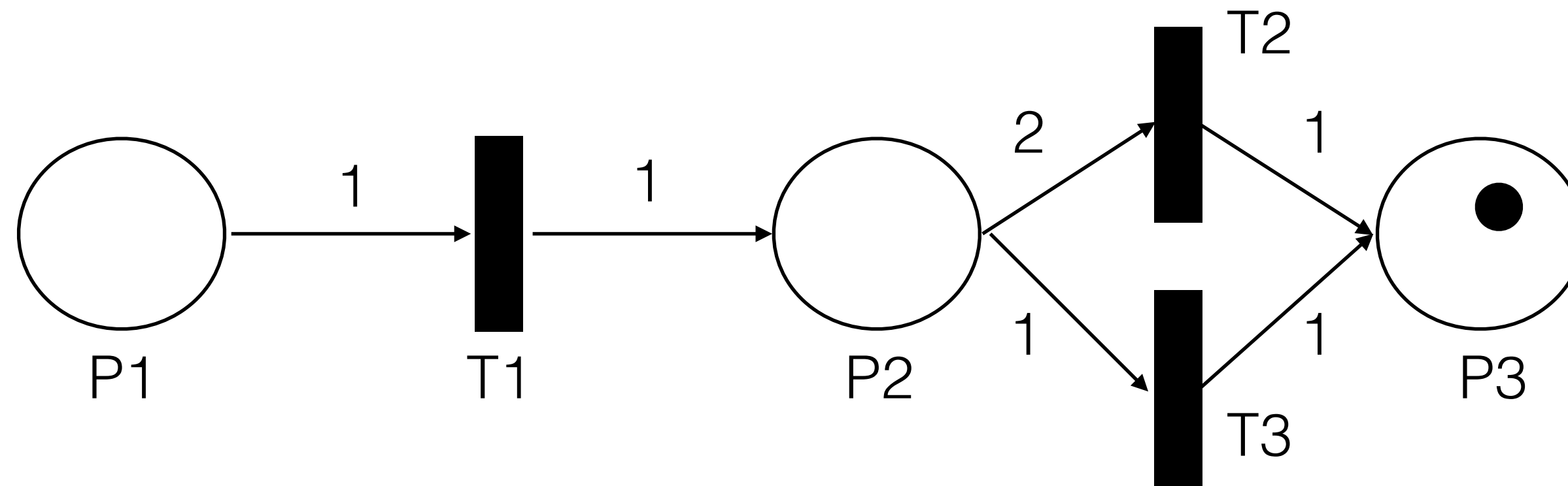
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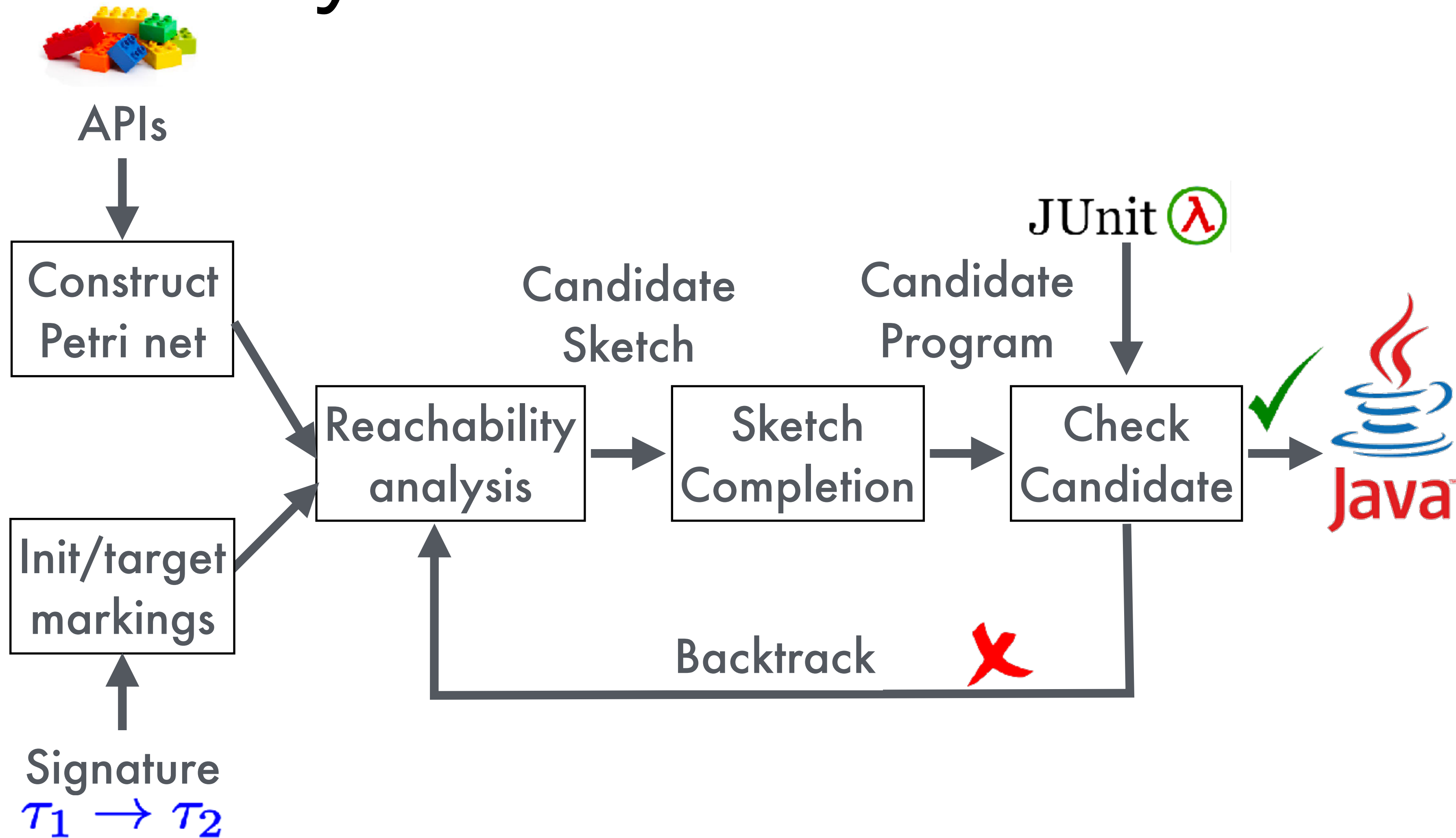
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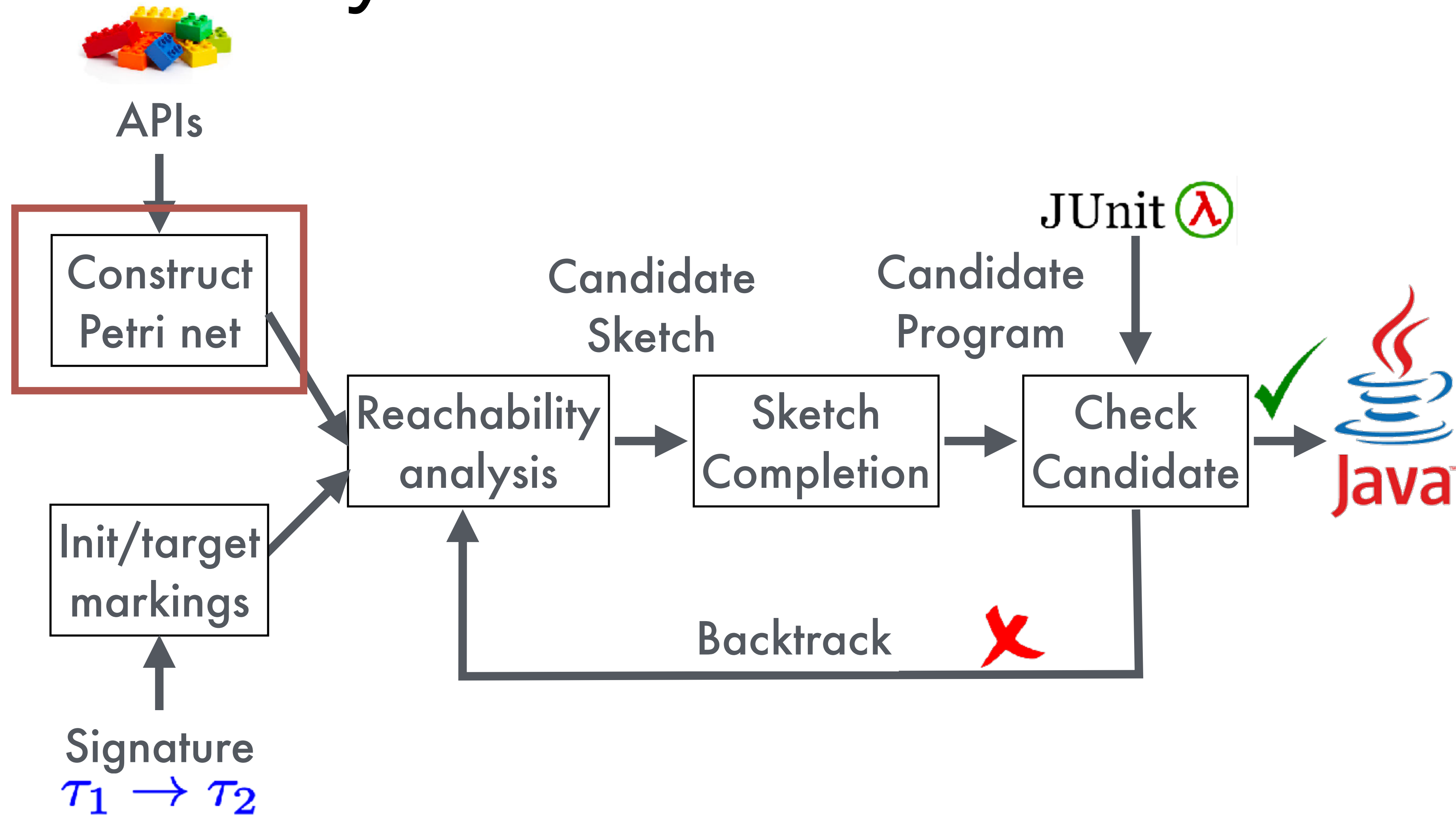
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# SyPet Architecture

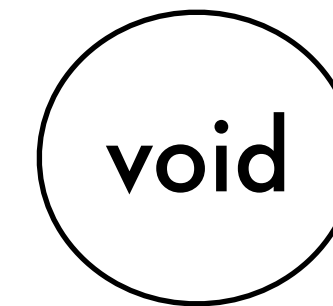
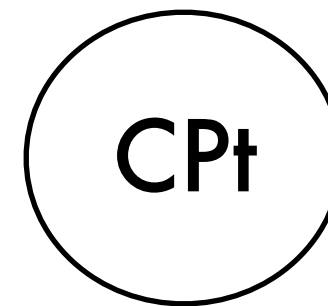
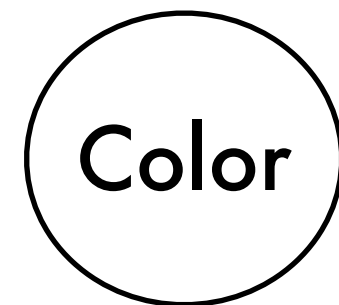
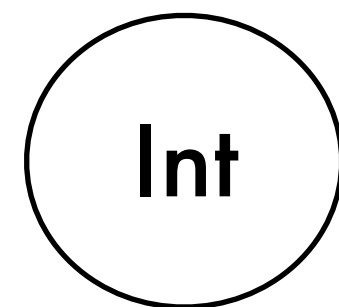


# SyPet Architecture



# Petri Net Construction

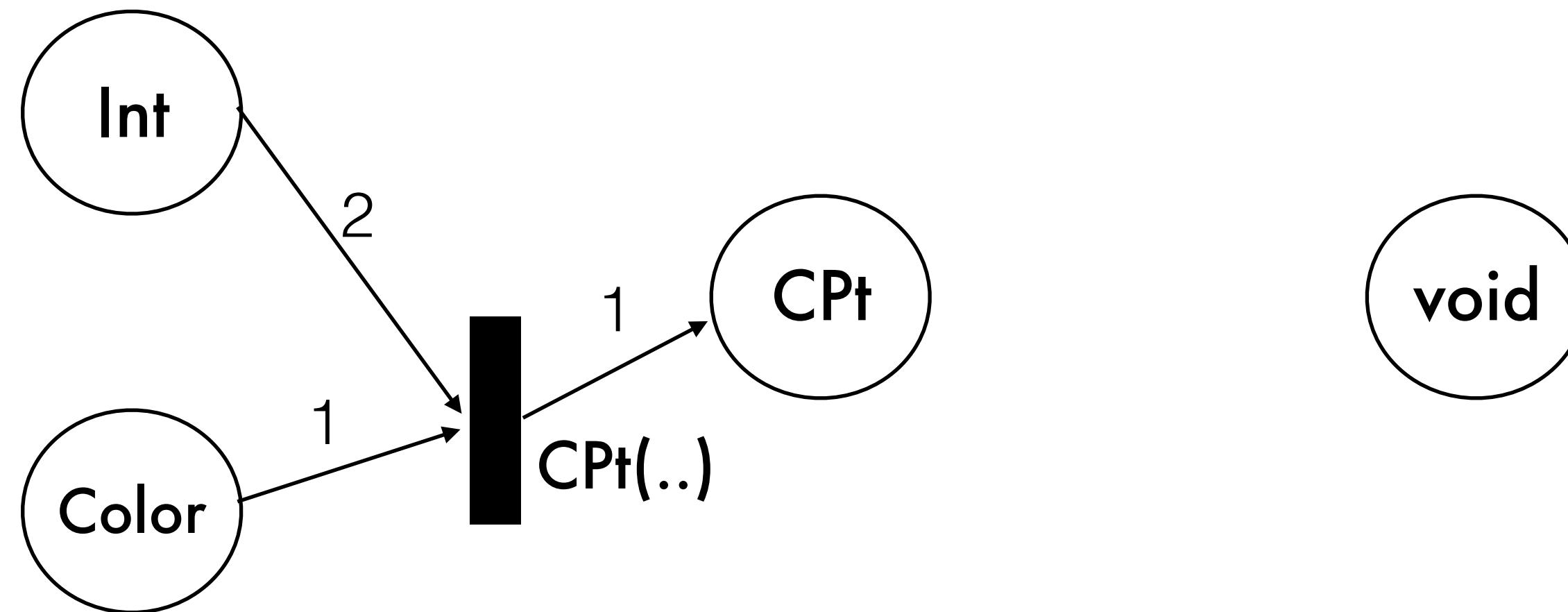
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    ...  
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```





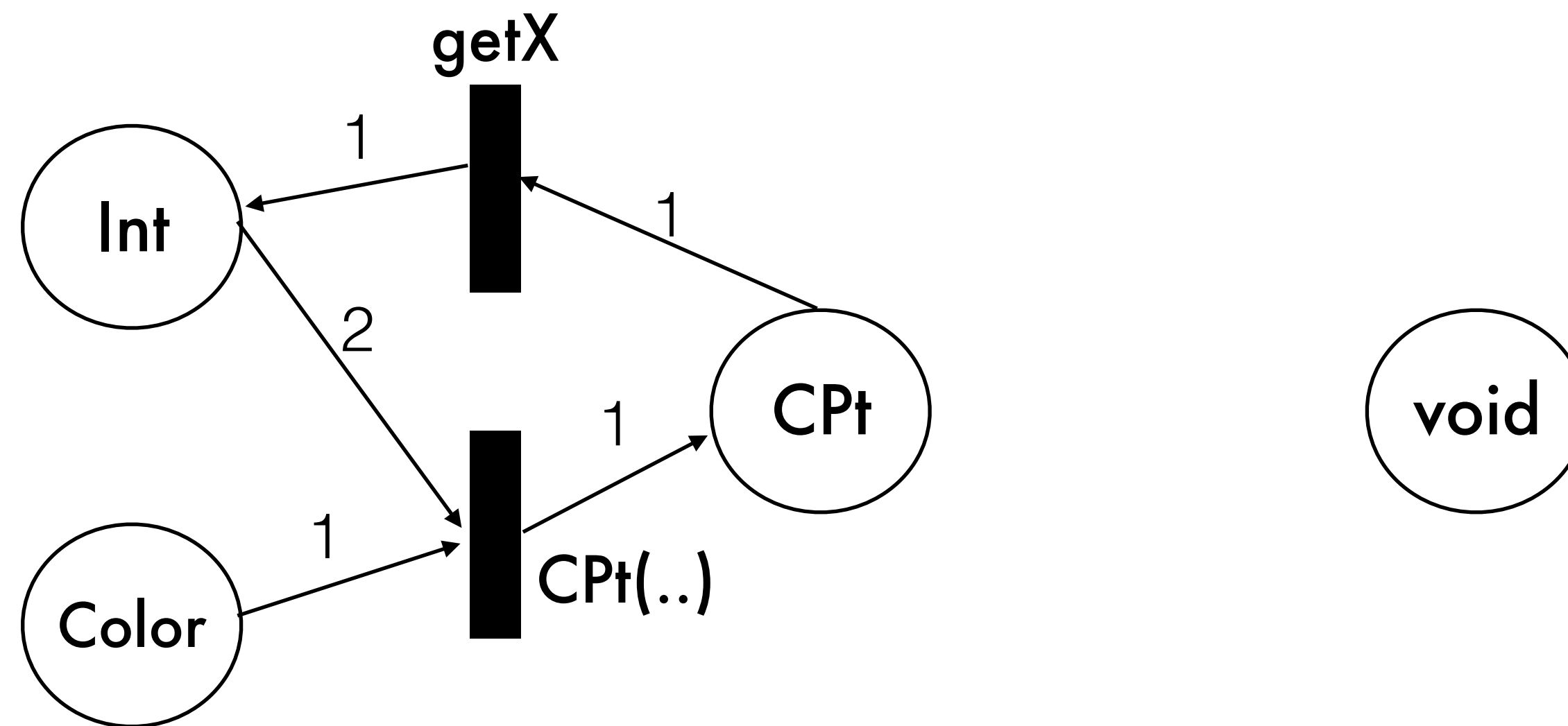
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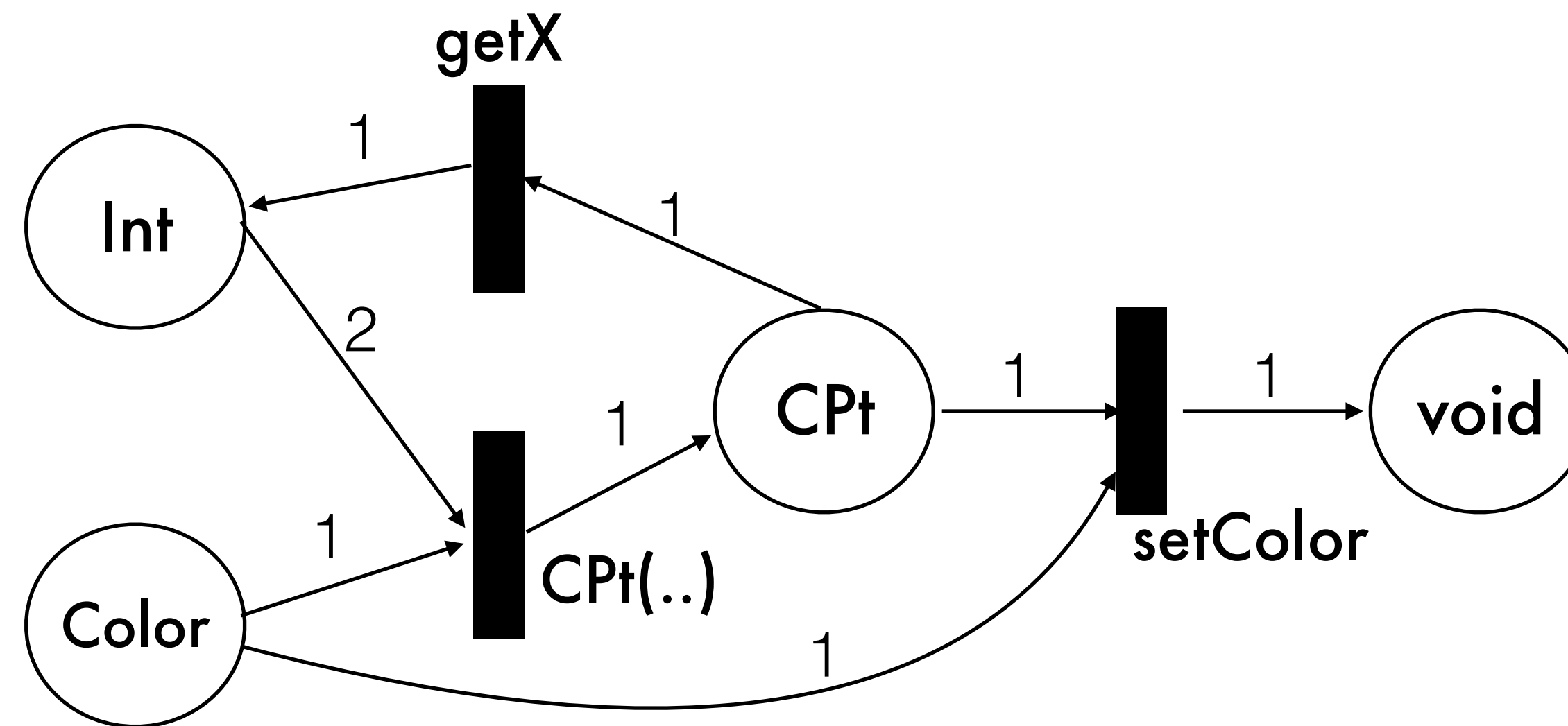
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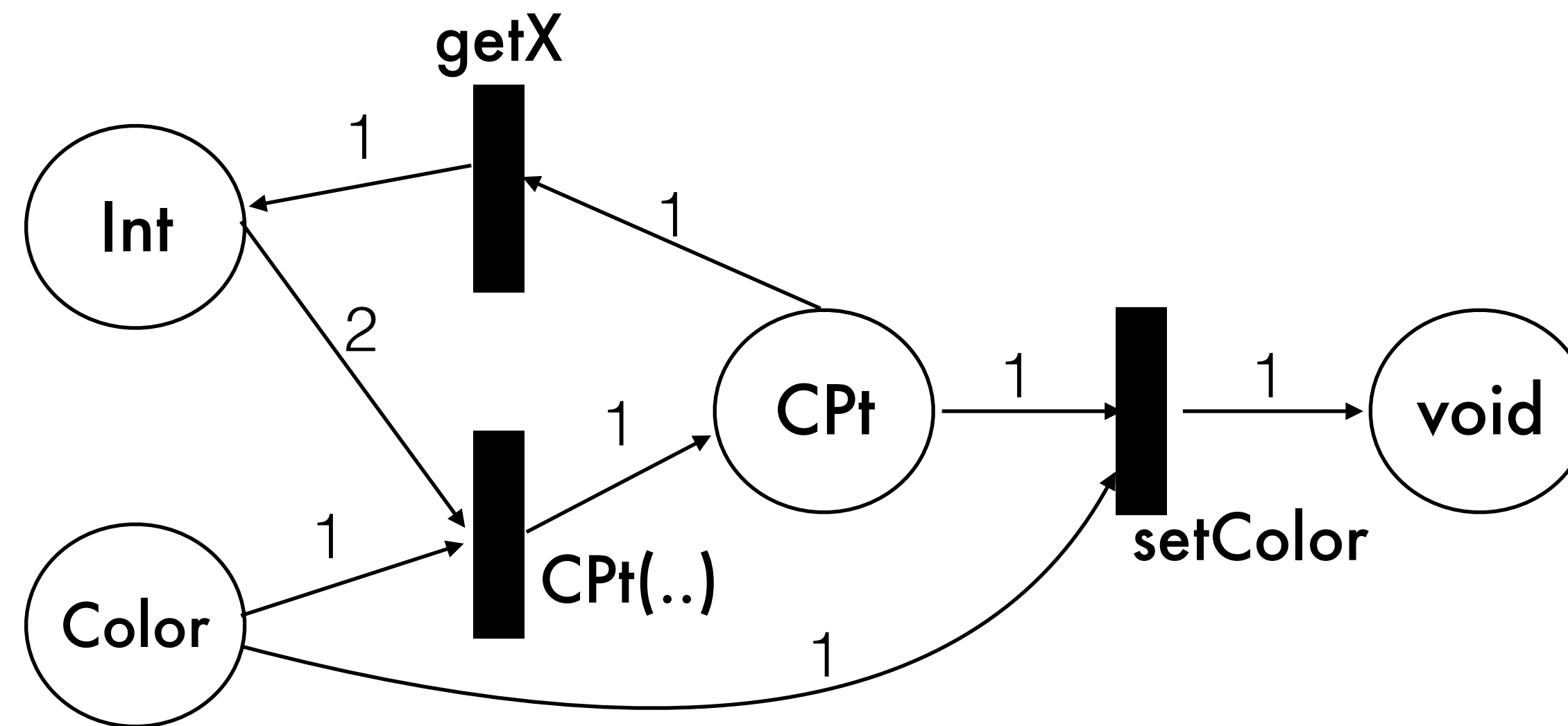


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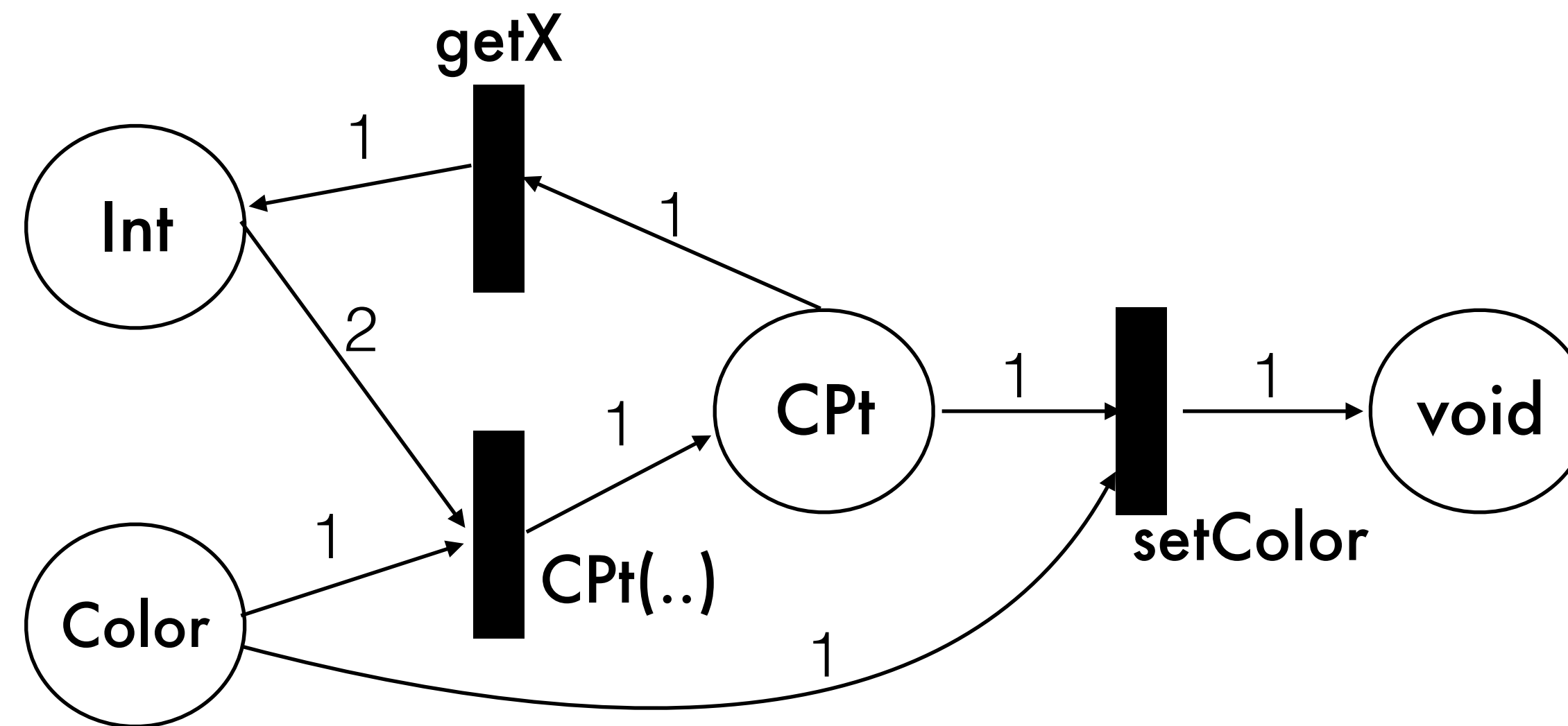


# Clone Transitions



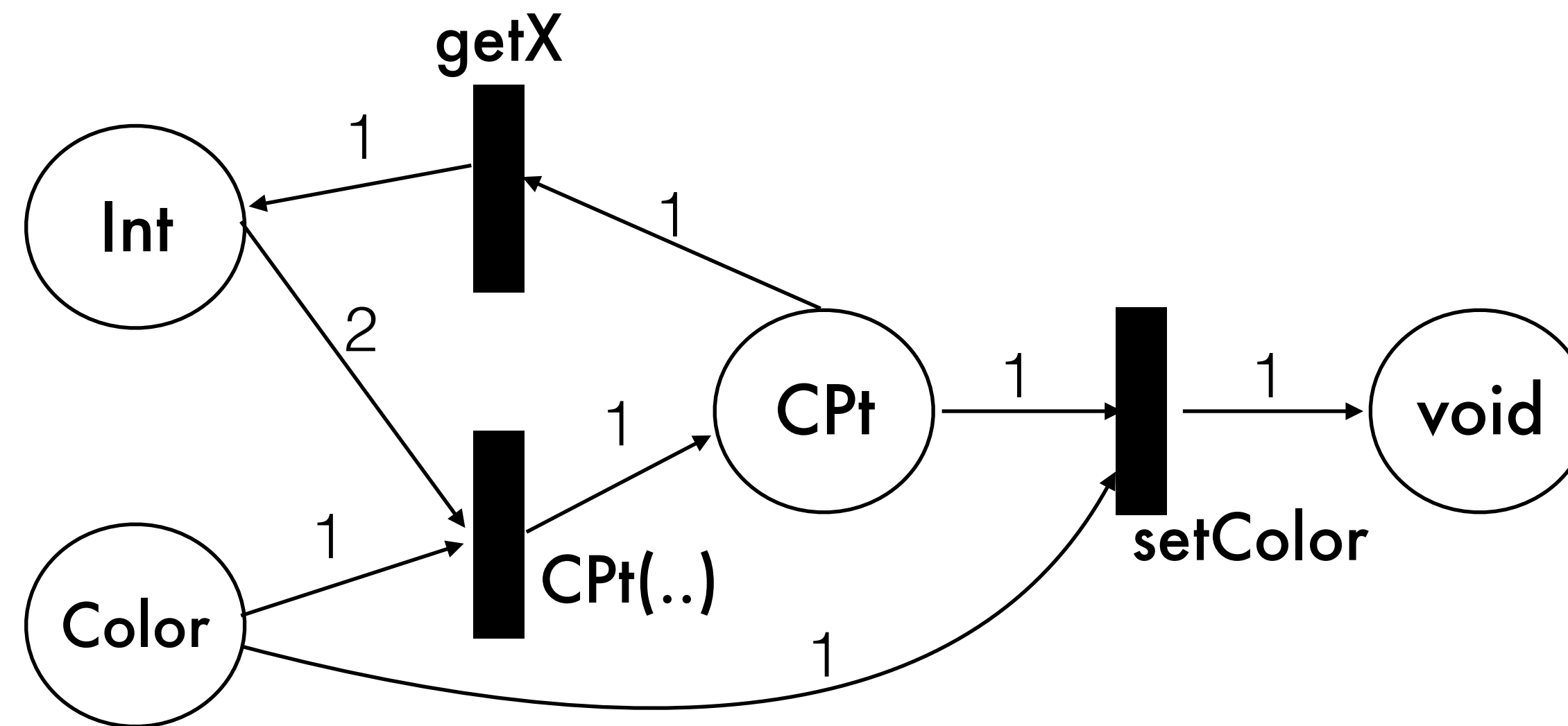
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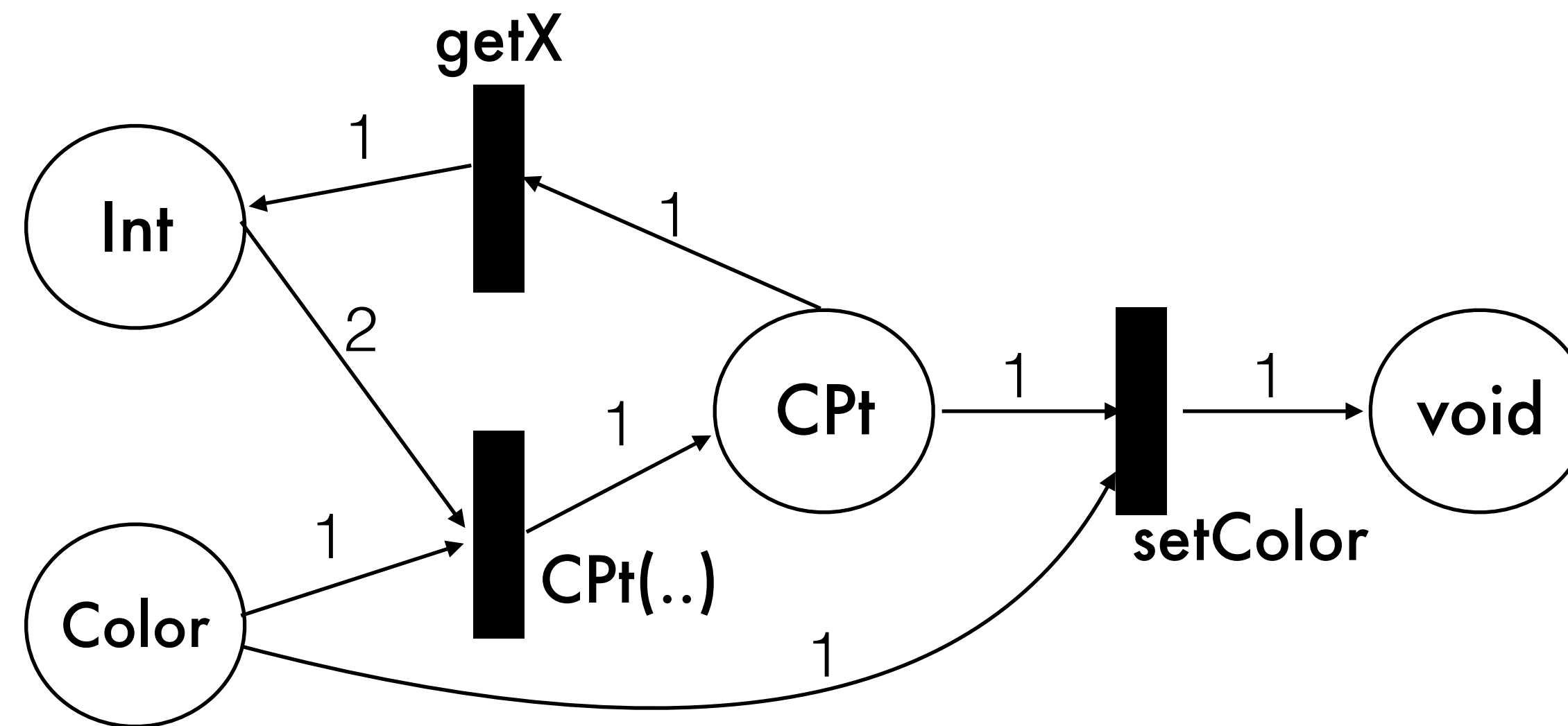
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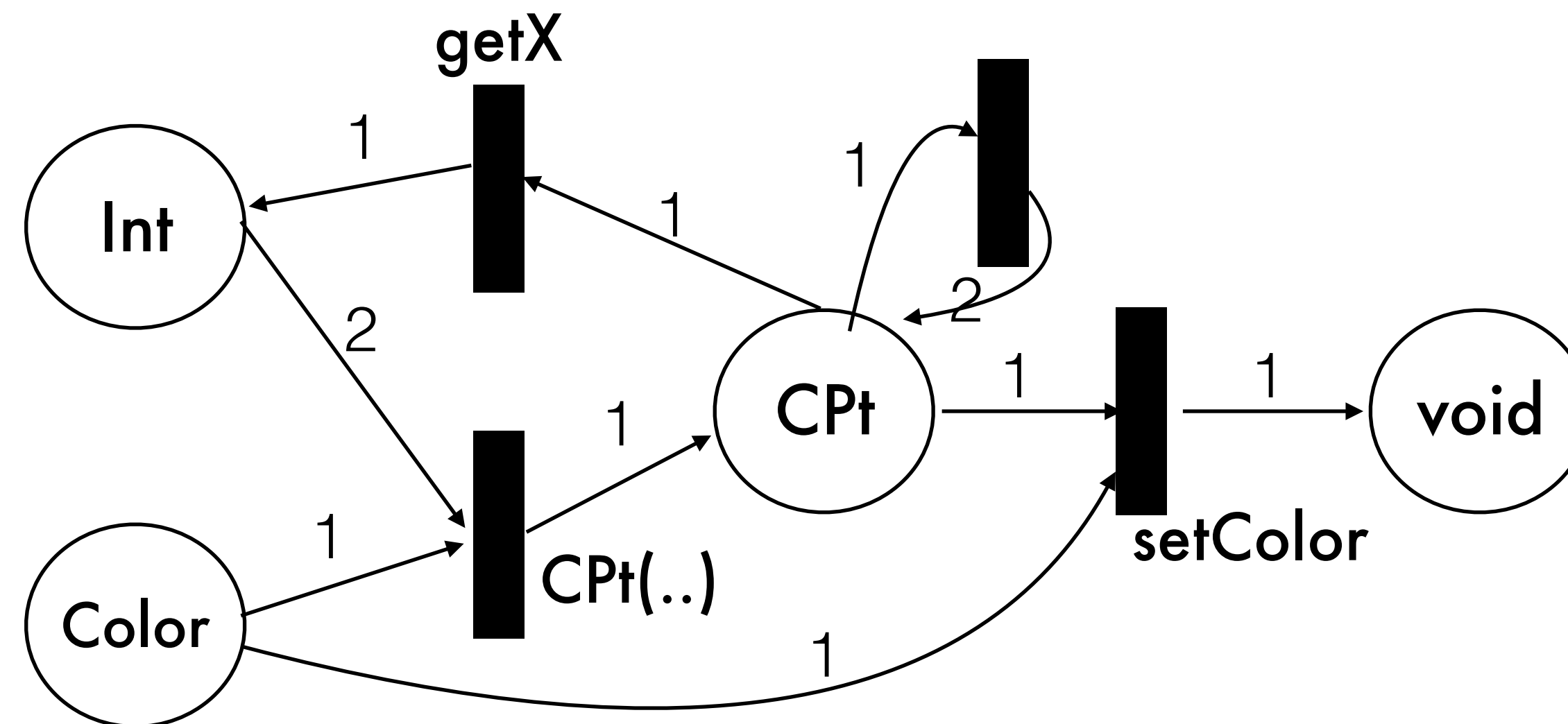
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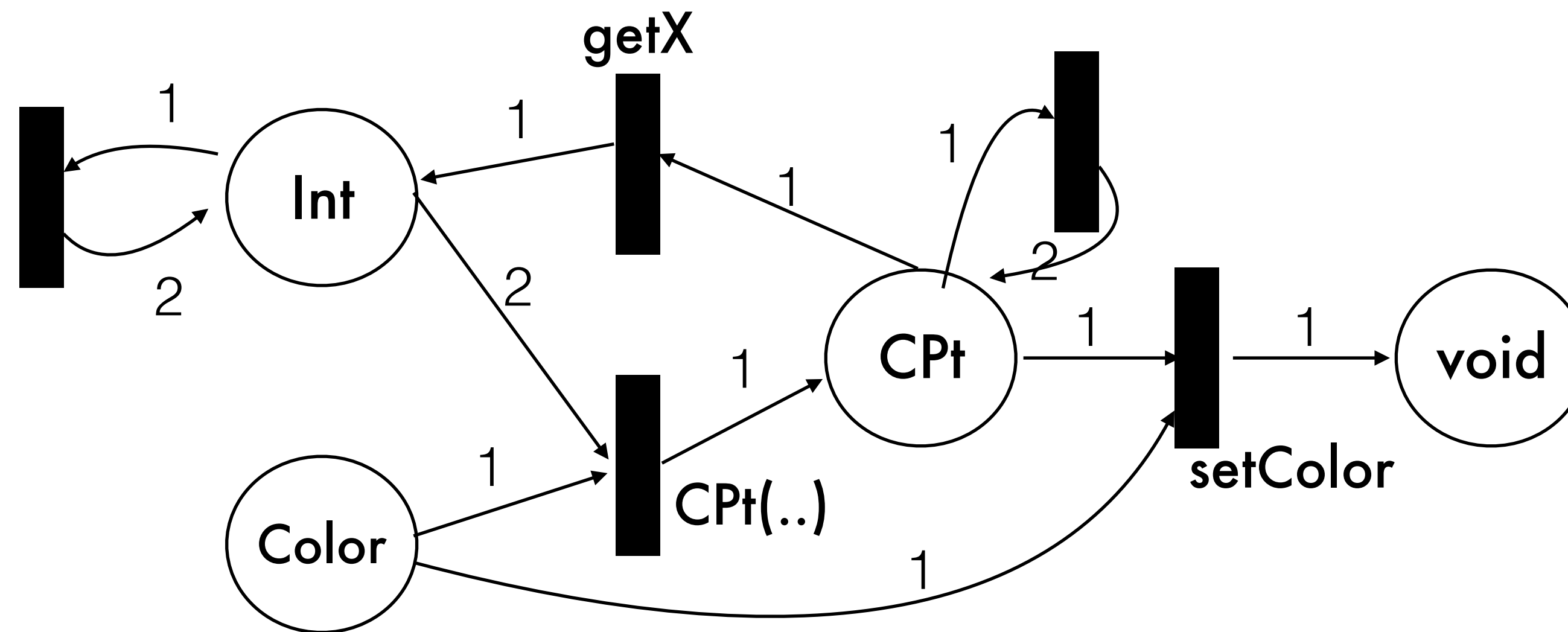
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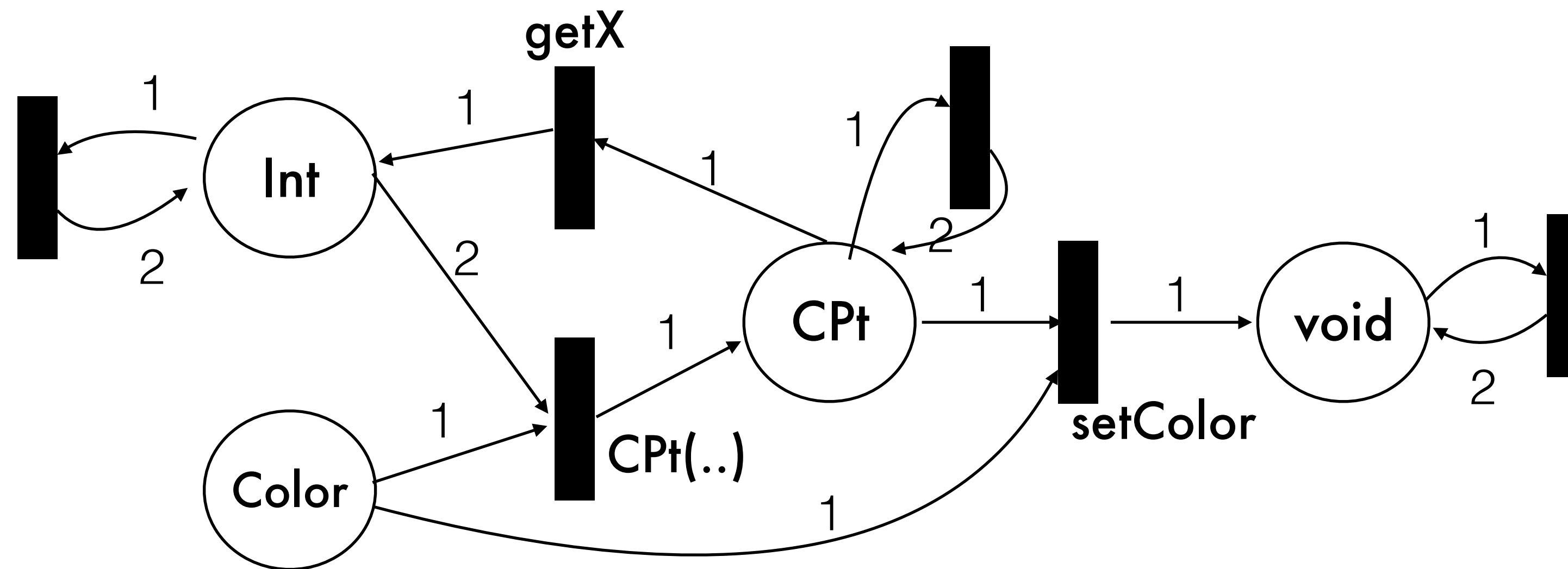
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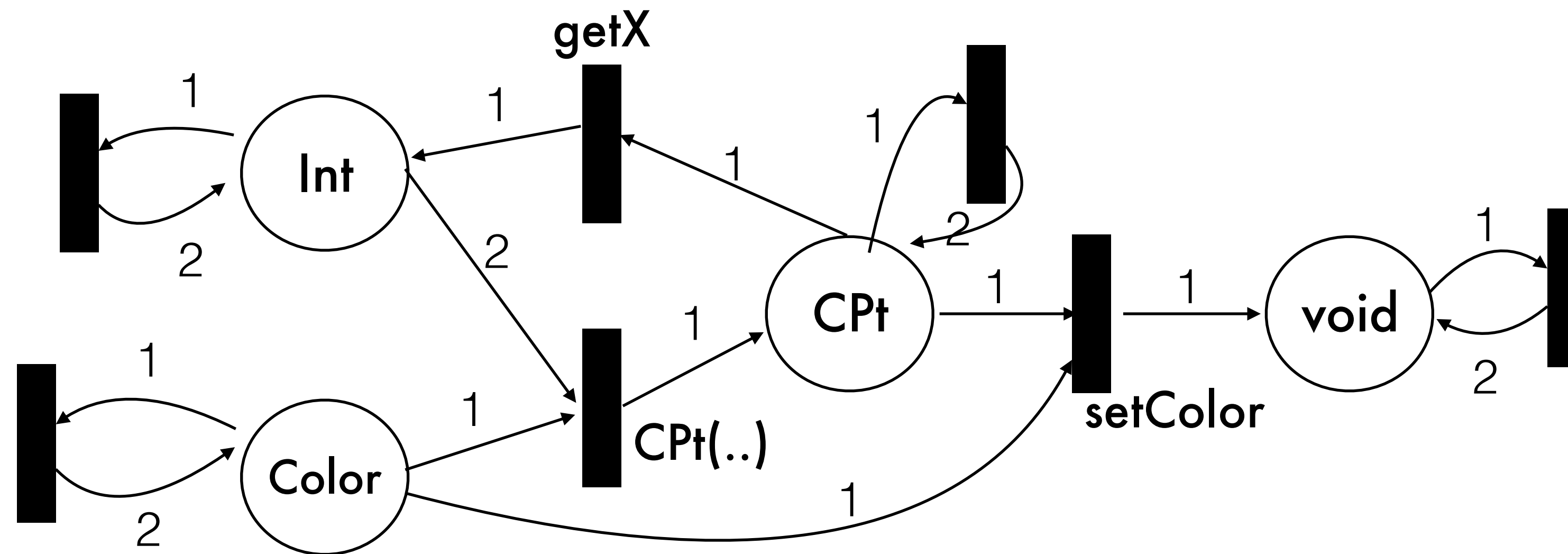
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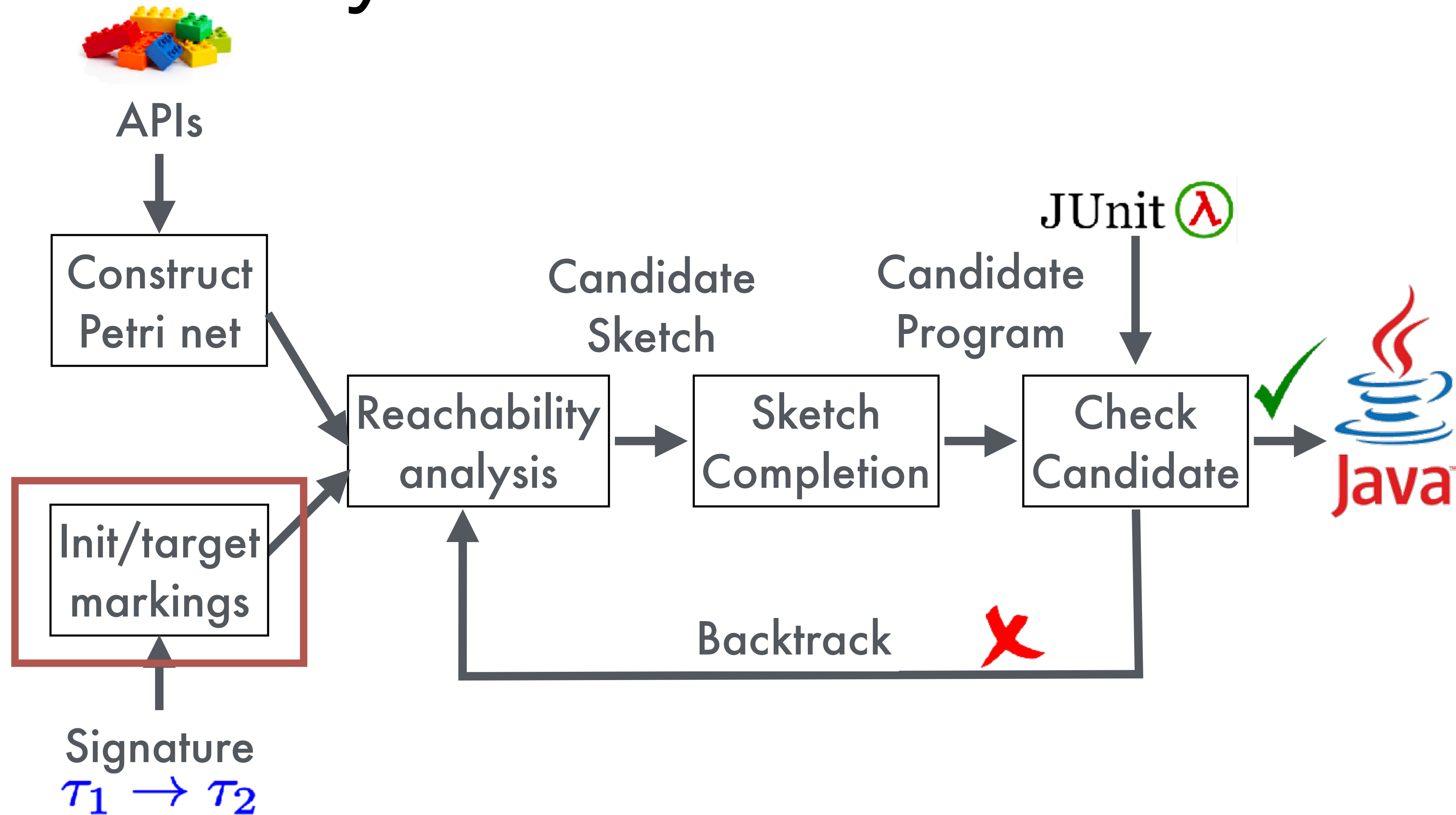


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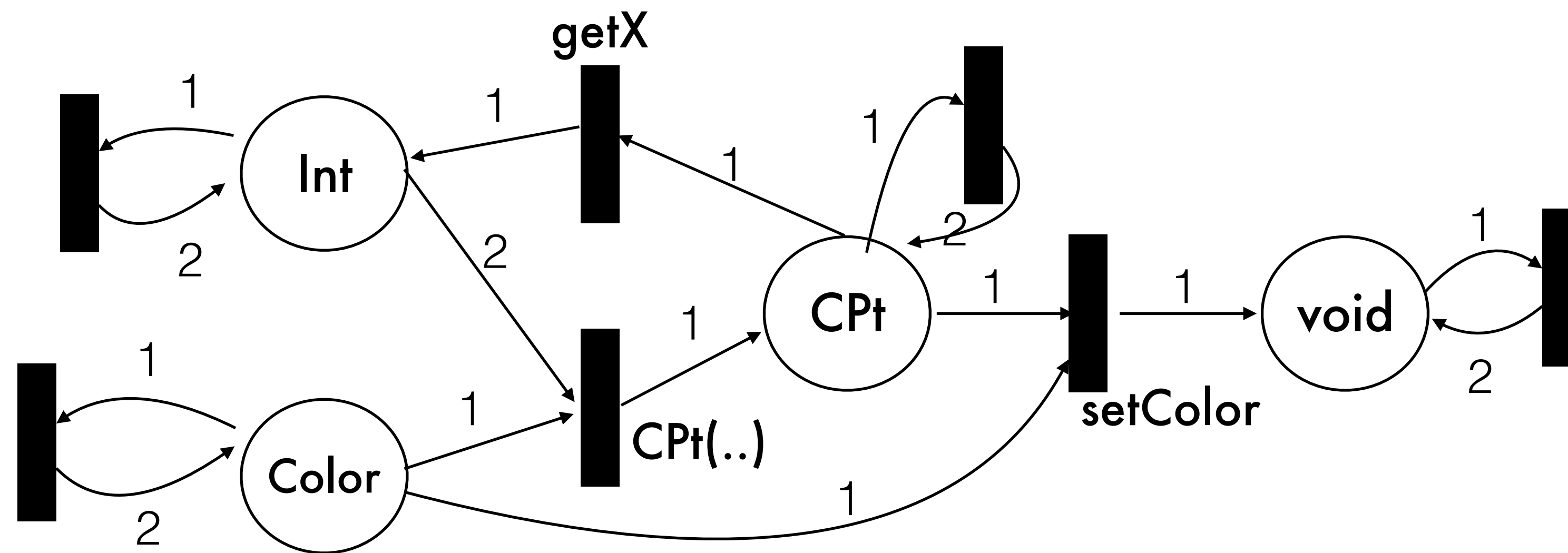


# SyPet Architecture



# Initial and Target Markings

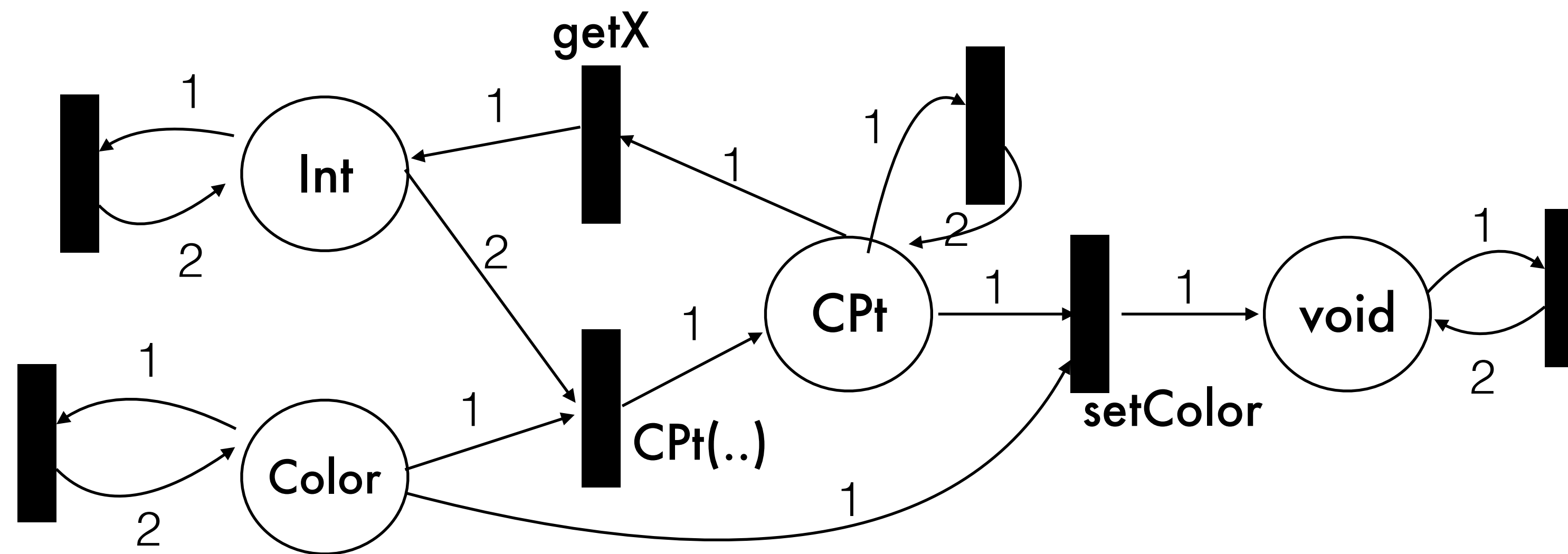
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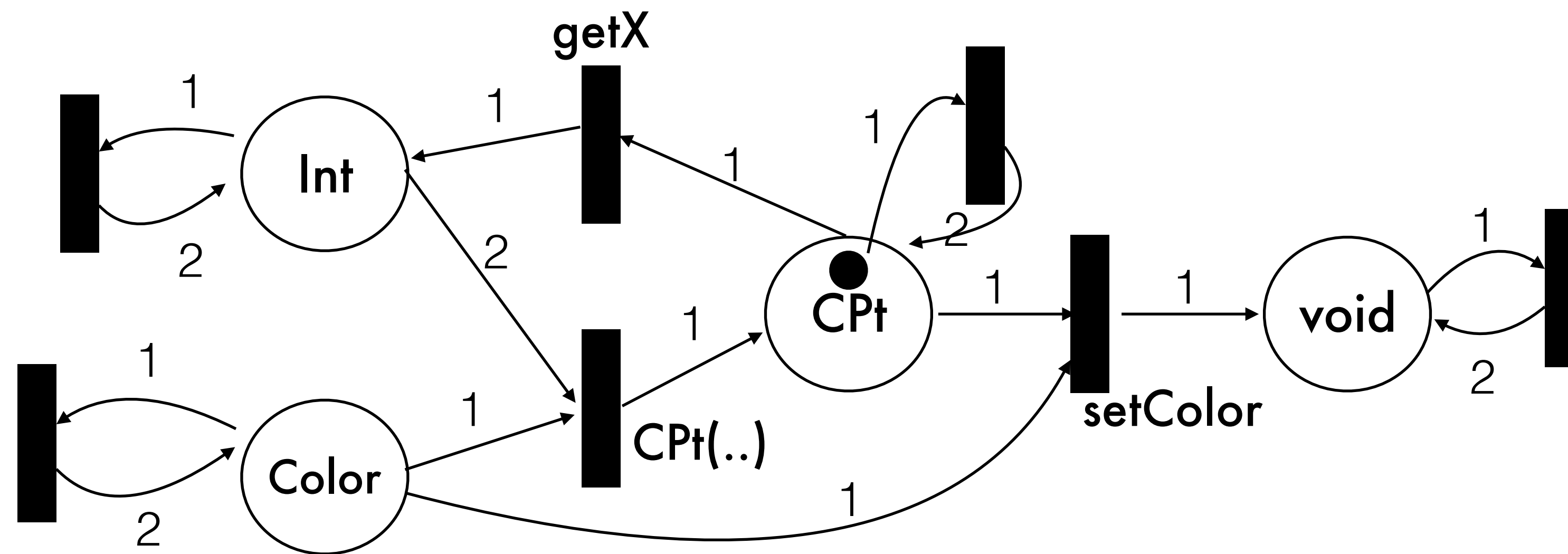
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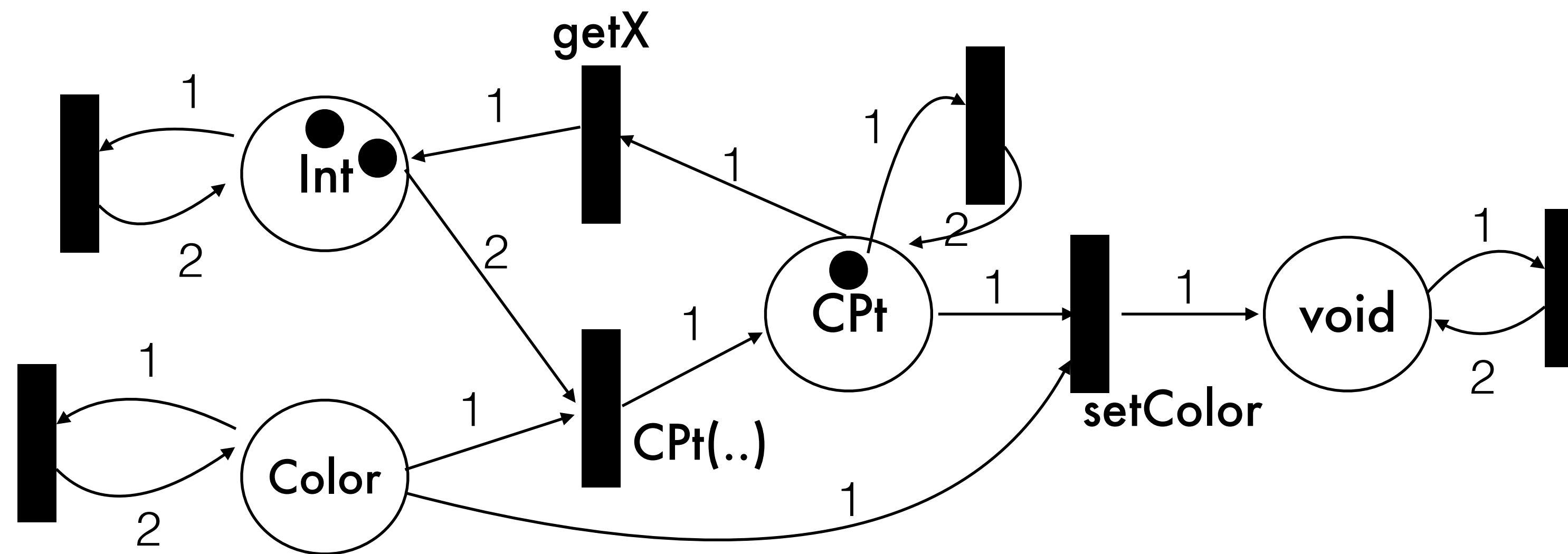
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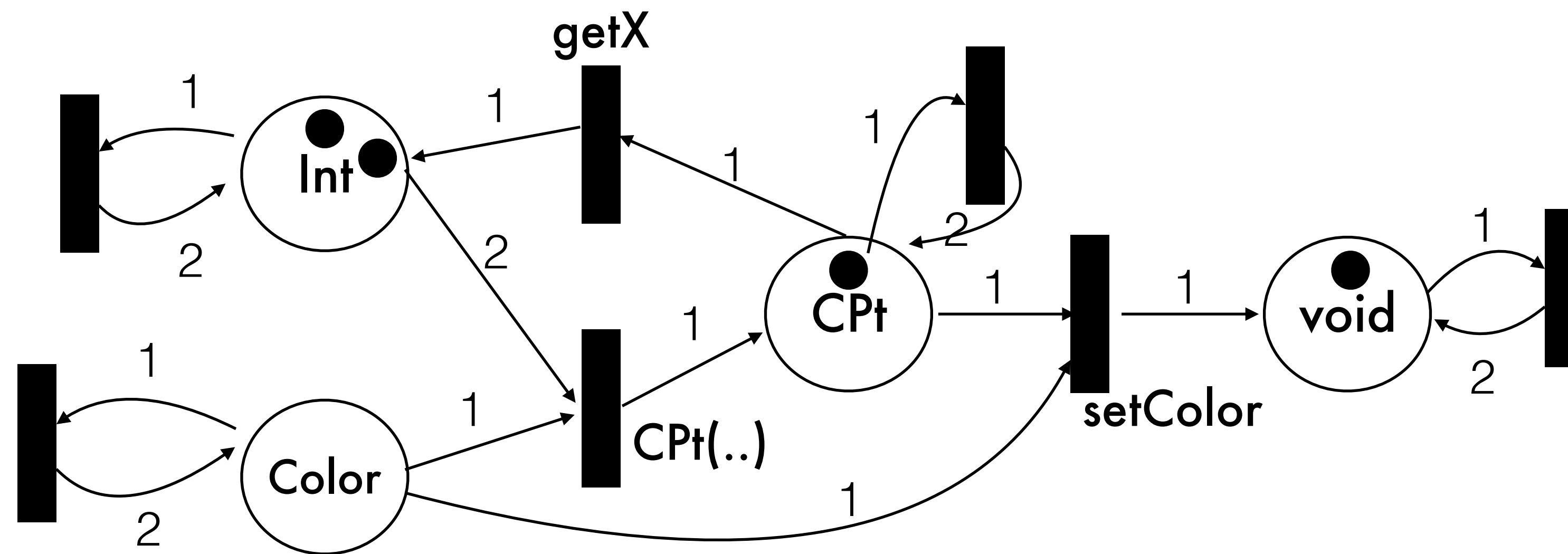




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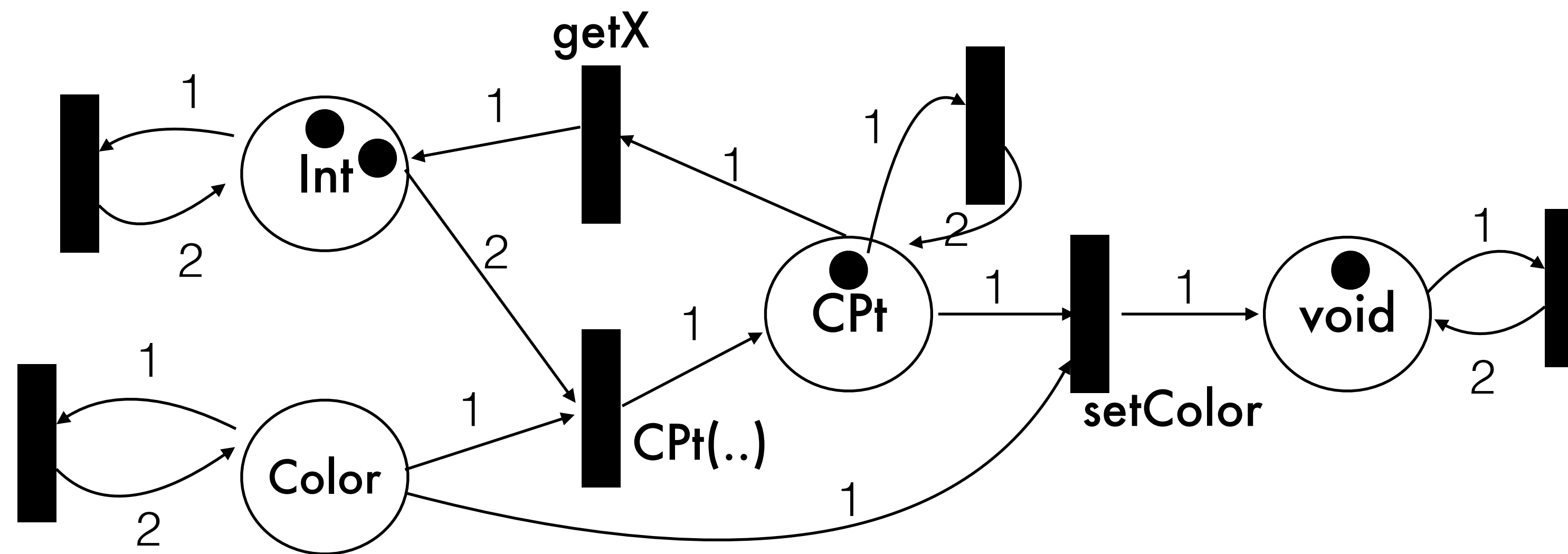


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CPt shift (CPt p, Int shiftX, Int shiftY)

Target marking:



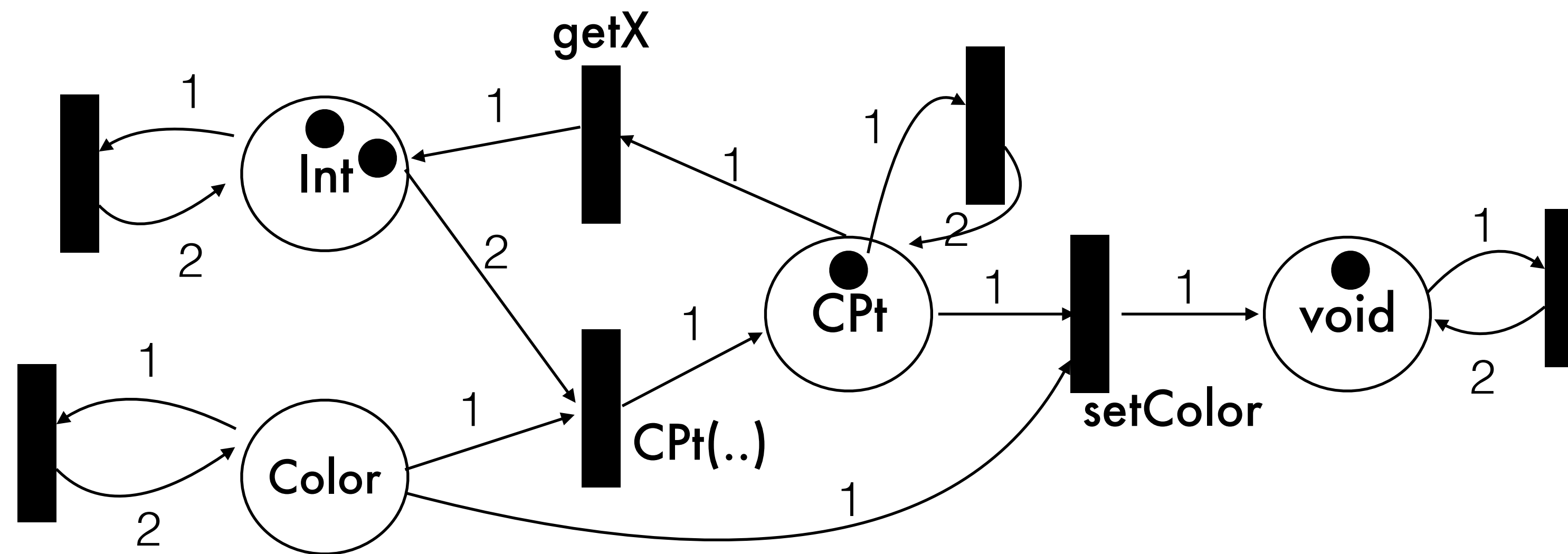
# Initial and Target Markings

Use signature to determine initial and target markings of Petri net

CPt shift (CPt p, Int shiftX, Int shiftY)

Target marking:

Cpt = 1



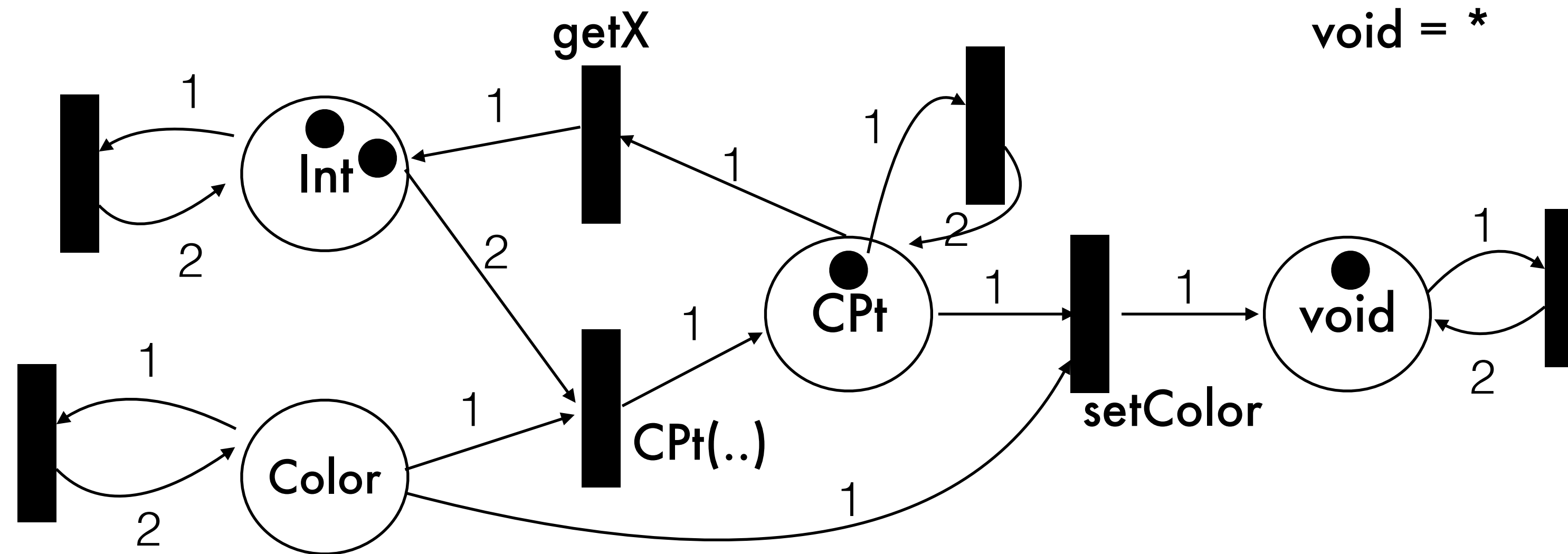
# Initial and Target Markings

Use signature to determine initial and target markings of Petri net

CPt shift (CPt p, Int shiftX, Int shiftY)

Target marking:

Cpt = 1  
void = \*



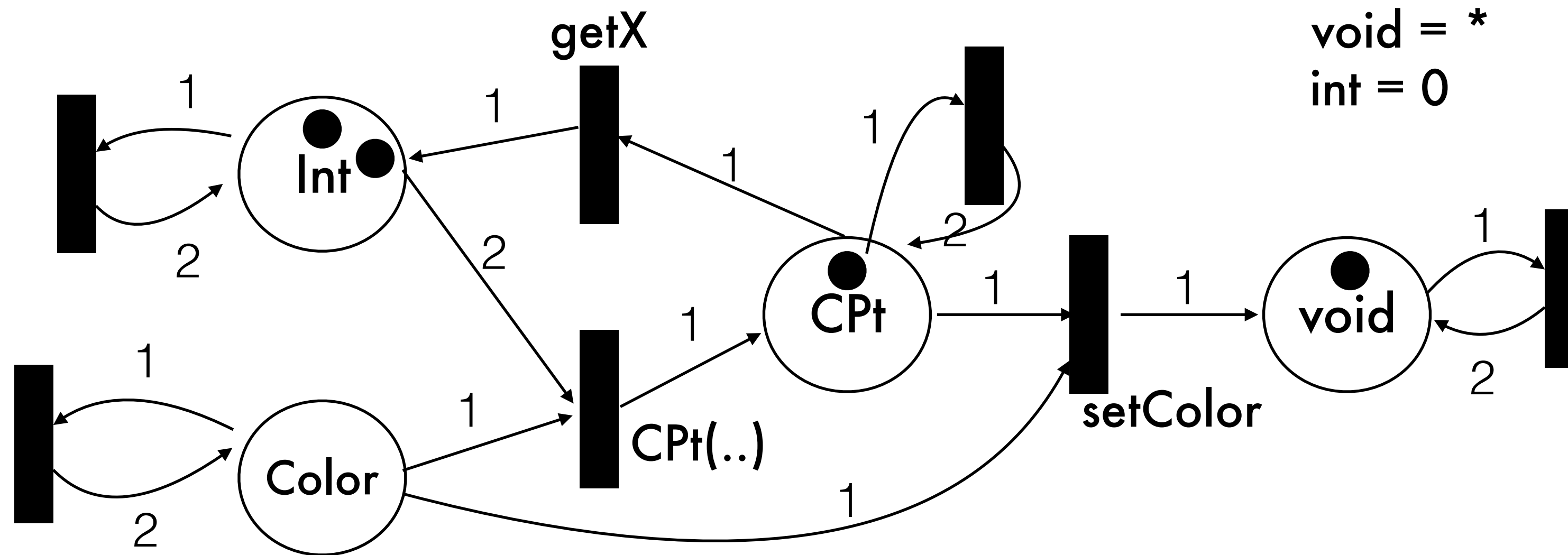
# Initial and Target Markings

Use signature to determine initial and target markings of Petri net

CPt shift (CPt p, Int shiftX, Int shiftY)

Target marking:

Cpt = 1  
void = \*  
int = 0



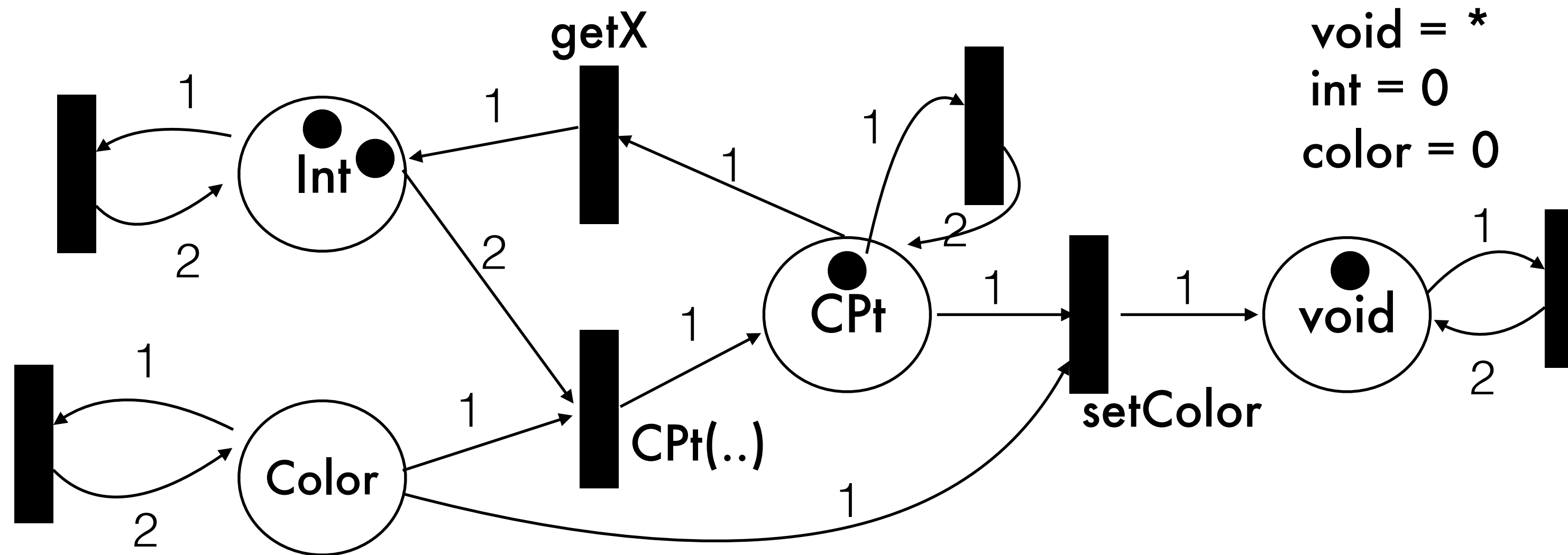
# Initial and Target Markings

Use signature to determine initial and target markings of Petri net

CPt shift (CPt p, Int shiftX, Int shiftY)

Target marking:

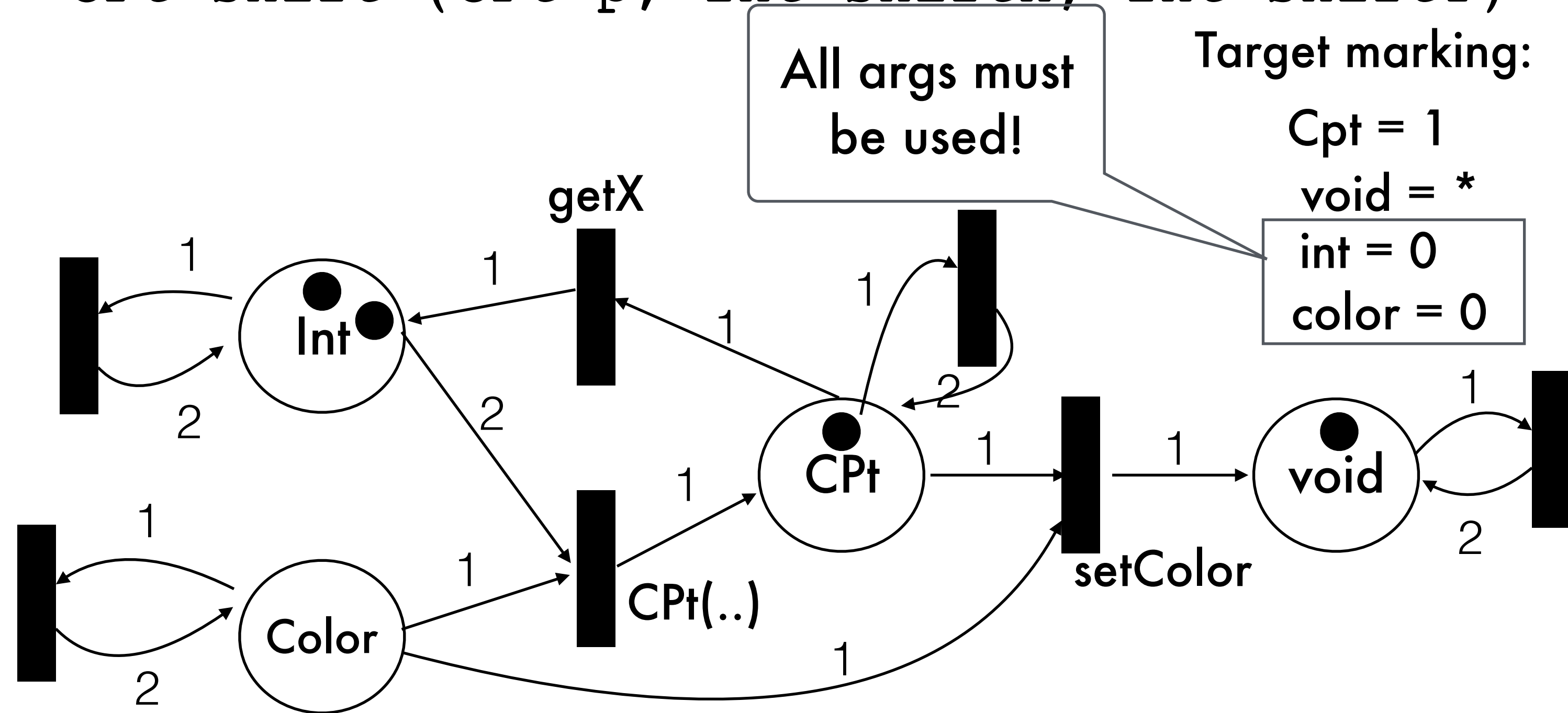
Cpt = 1  
void = \*  
int = 0  
color = 0



# Initial and Target Markings

Use signature to determine initial and target markings of Petri net

`CPt shift (CPt p, Int shiftX, Int shiftY)`



# Building a Petri Net

```
class Point {  
    Point();  
    int getX();  
    int getY();  
    void setX(int);  
    void setY(int);  
}
```

```
class MyPoint {  
    MyPoint(int x, int y);  
    int getX();  
    int getY();  
}
```





# Building a Petri Net

```
class Point {  
    Point();  
    int getX();  
    int getY();  
    void setX(int);  
    void setY(int);  
}
```

```
class MyPoint {  
    MyPoint(int x, int y);  
    int getX();  
    int getY();  
}
```

- What are the **places** (i.e., types)?
- What are the **transitions** (i.e., methods)?

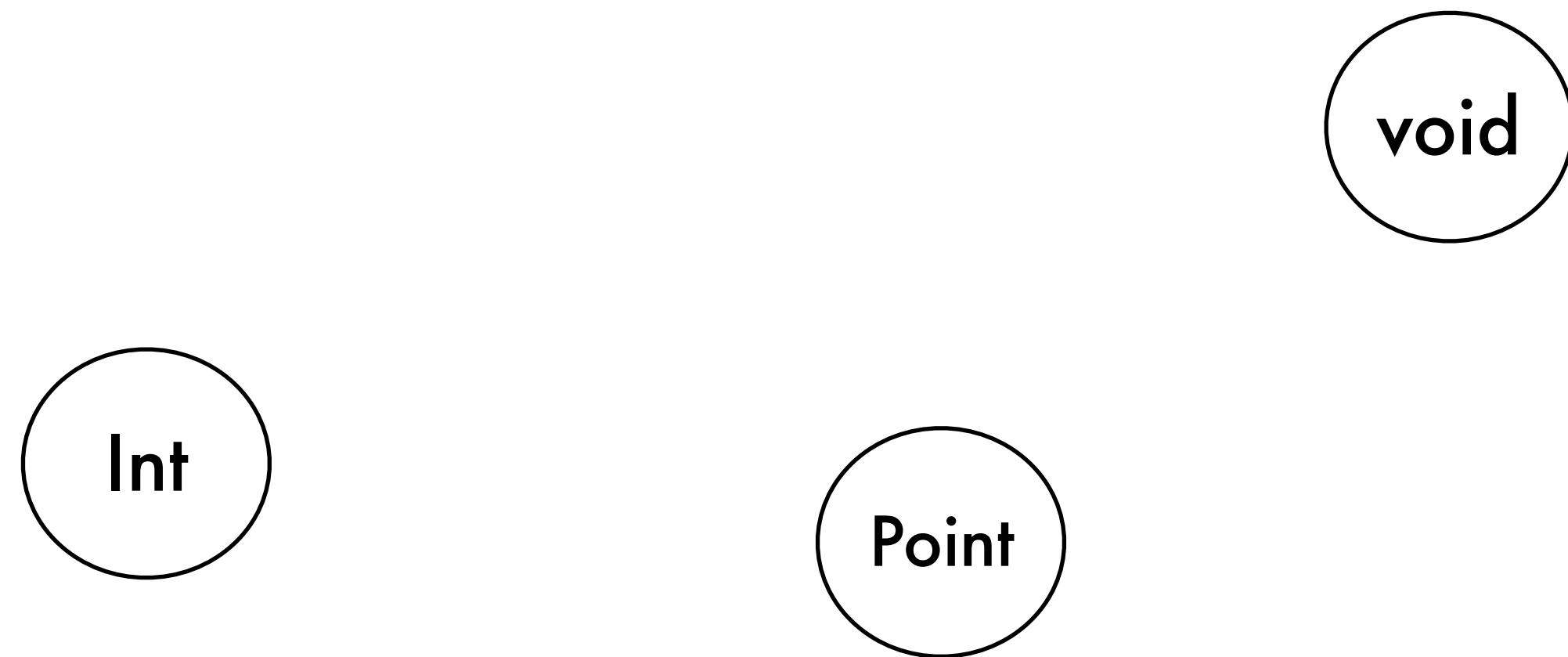


# Building a Petri Net

```
class Point {  
    Point();  
    int getX();  
    int getY();  
    void setX(int);  
    void setY(int);  
}
```



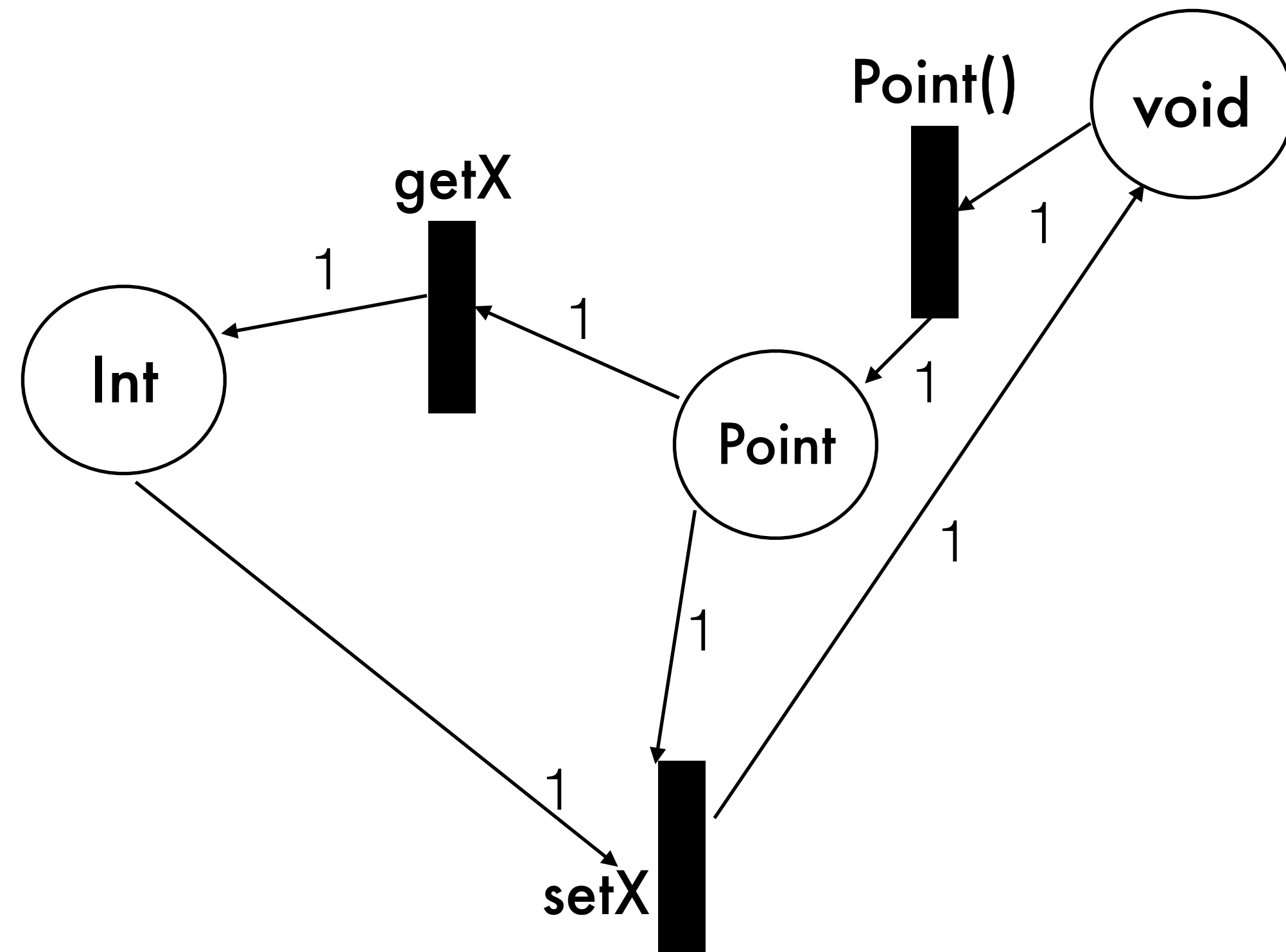
# Building a Petri Net



```
class Point {  
    Point();  
    int getX();  
    int getY();  
    void setX(int);  
    void setY(int);  
}
```



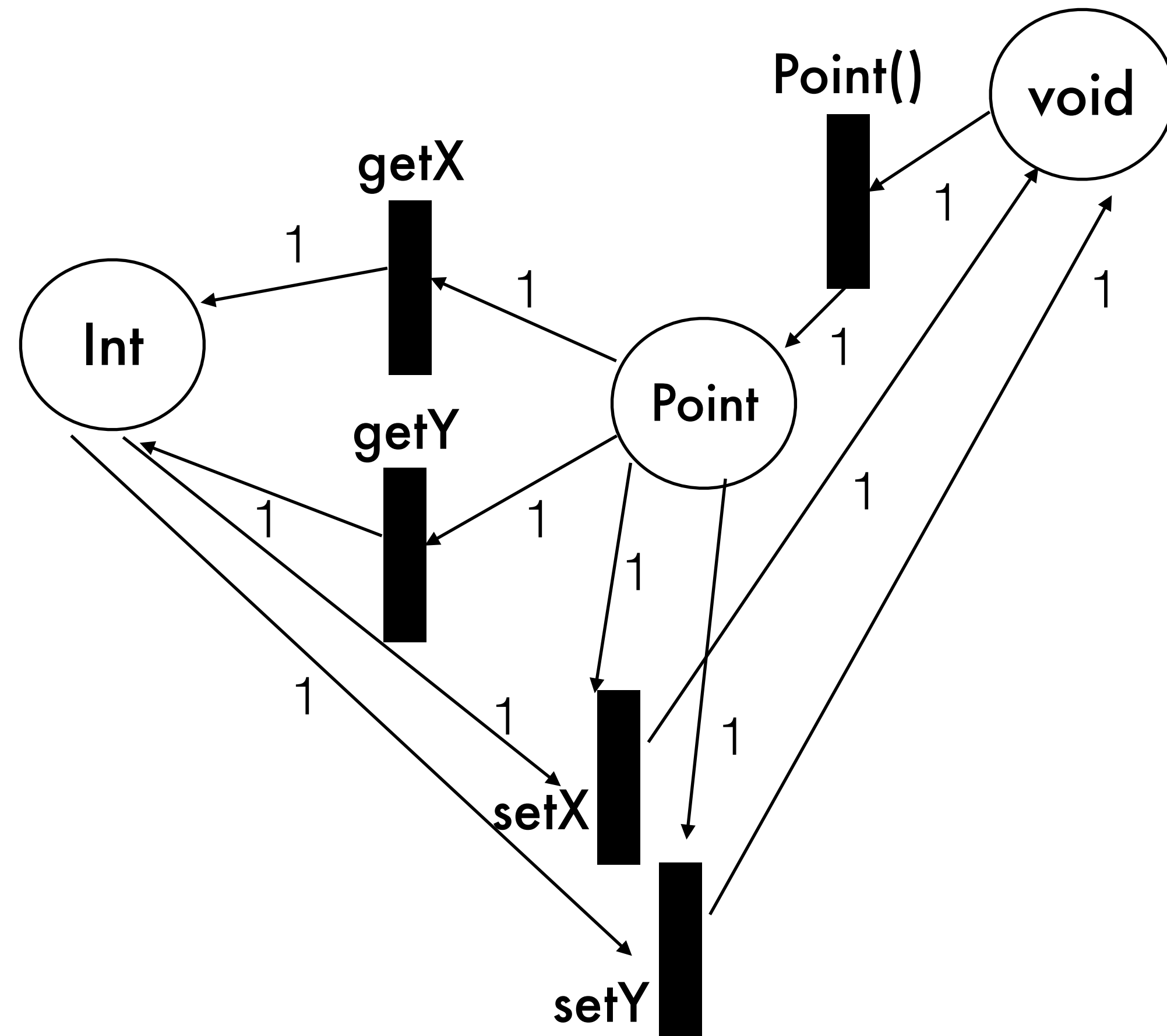
# Building a Petri Net



```
class Point {  
    Point();  
    int getX();  
    int getY();  
    void setX(int);  
    void setY(int);  
}
```



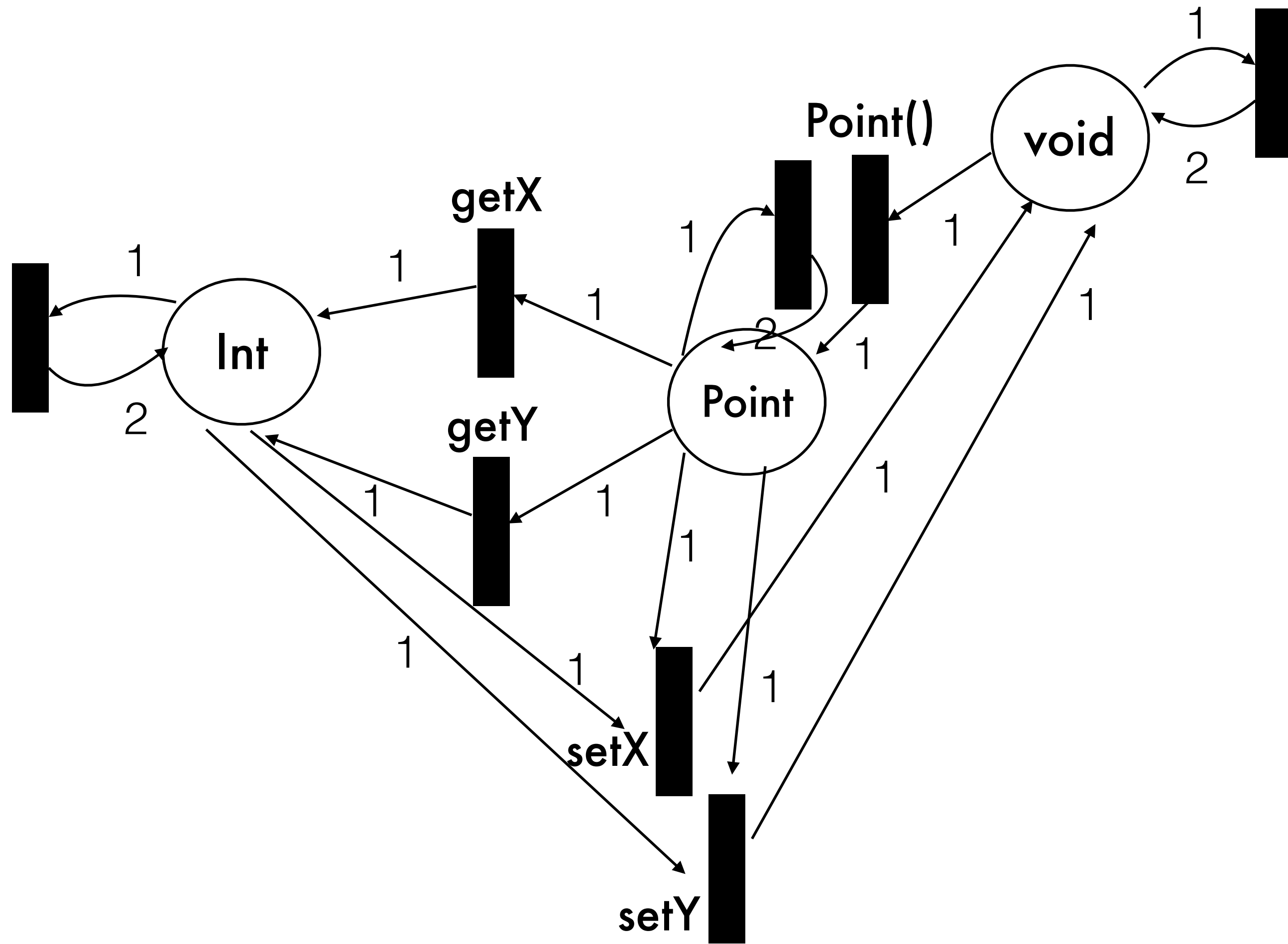
# Building a Petri Net



```
class Point {  
    Point();  
    int getX();  
    int getY();  
    void setX(int);  
    void setY(int);  
}
```



# Building a Petri Net



```
class Point {  
    Point();  
    int getX();  
    int getY();  
    void setX(int);  
    void setY(int);  
}
```

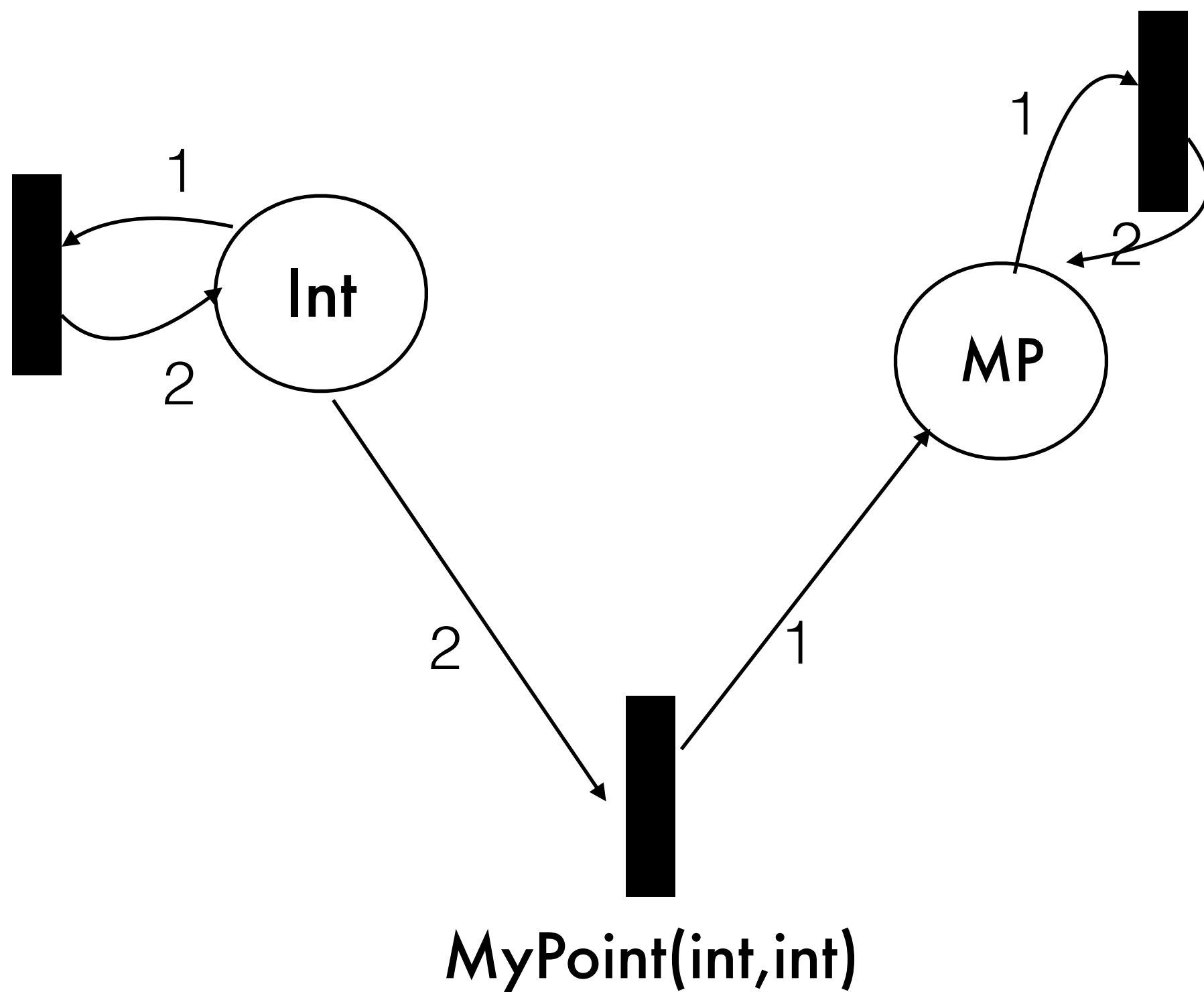


# Building a Petri Net

```
class MyPoint {  
    MyPoint(int x, int y);  
    int getX();  
    int getY();  
}
```



# Building a Petri Net

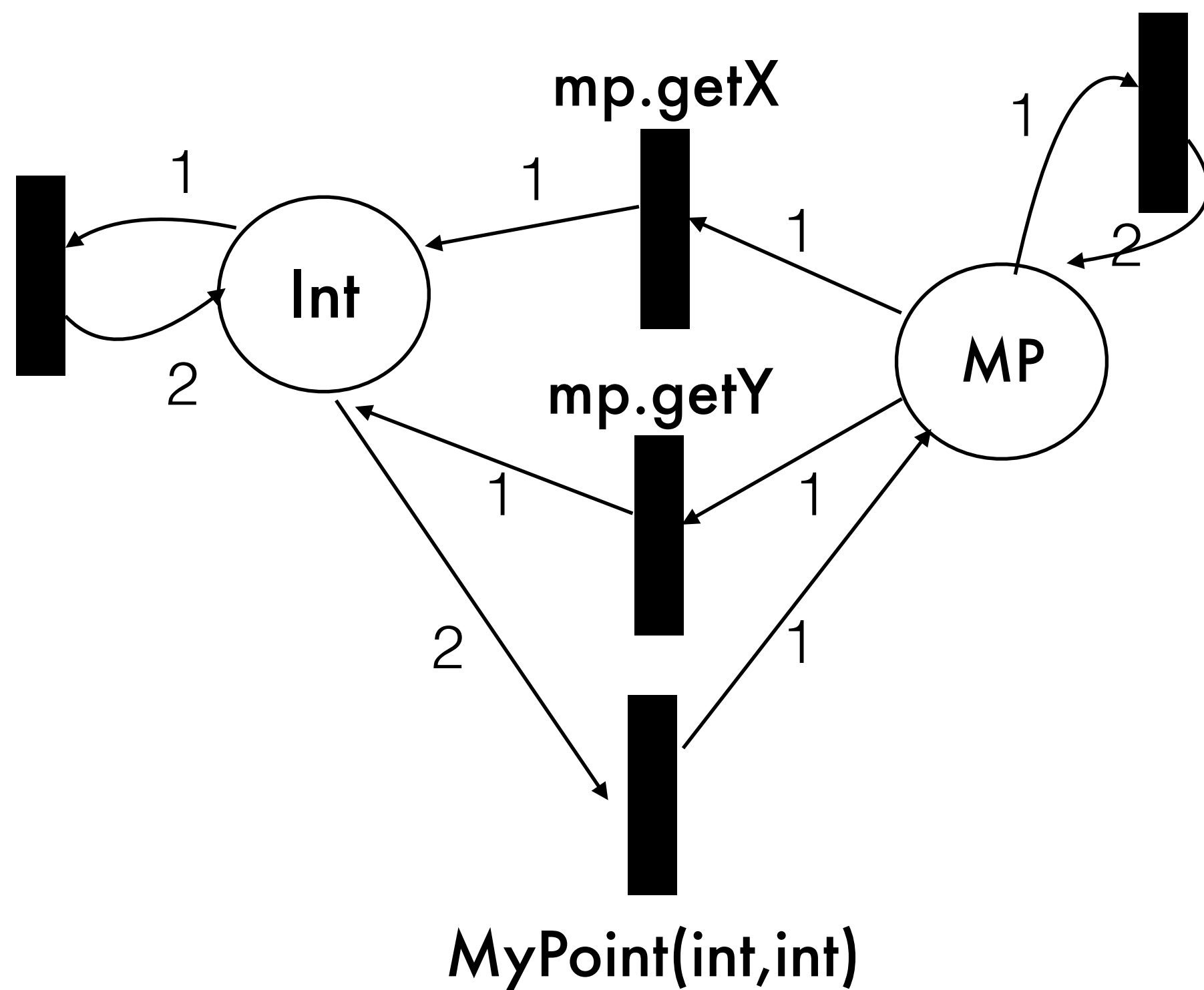


```
class MyPoint {  
    MyPoint(int x, int y);  
    int getX();  
    int getY();  
}
```





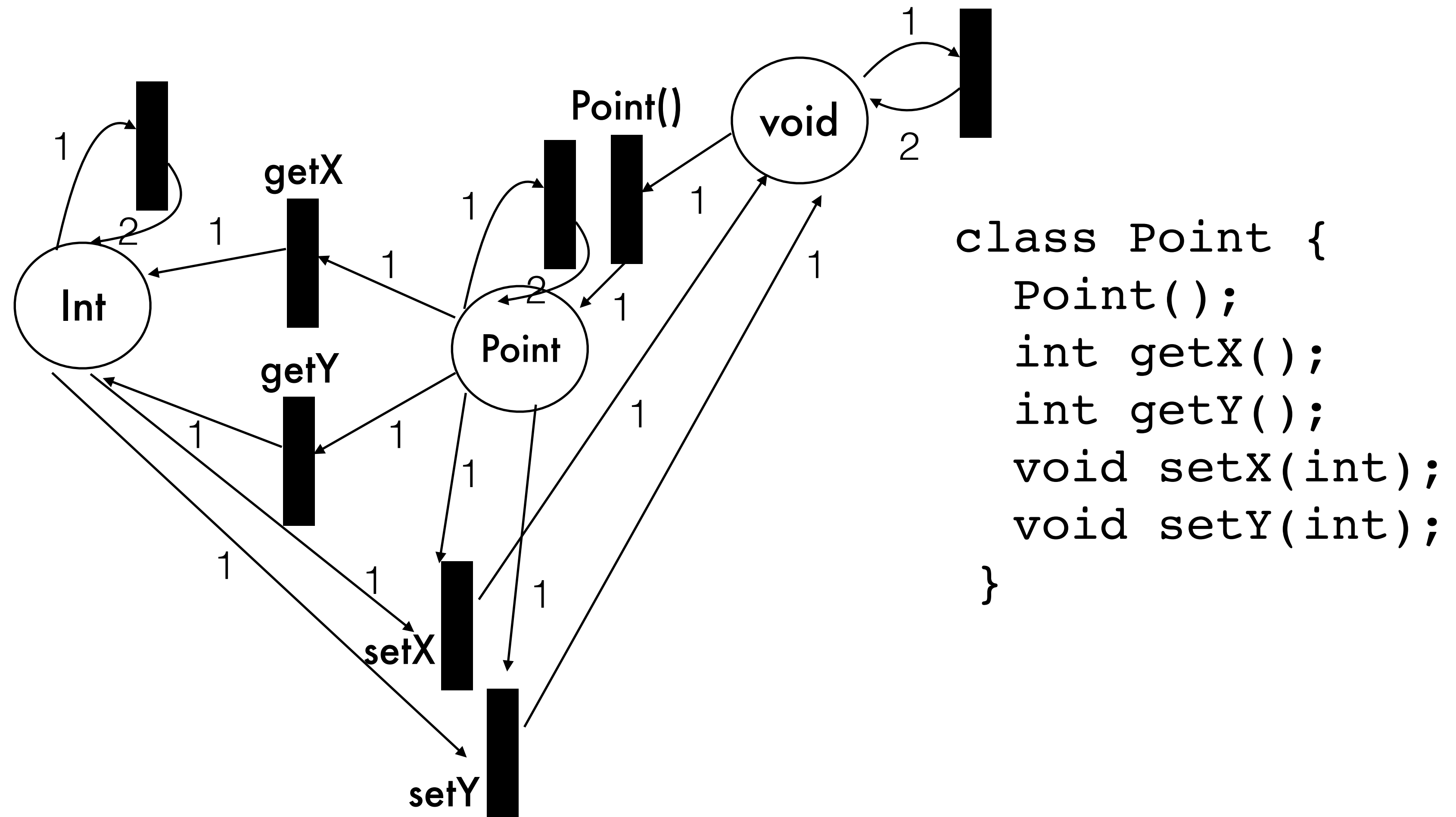
# Building a Petri Net



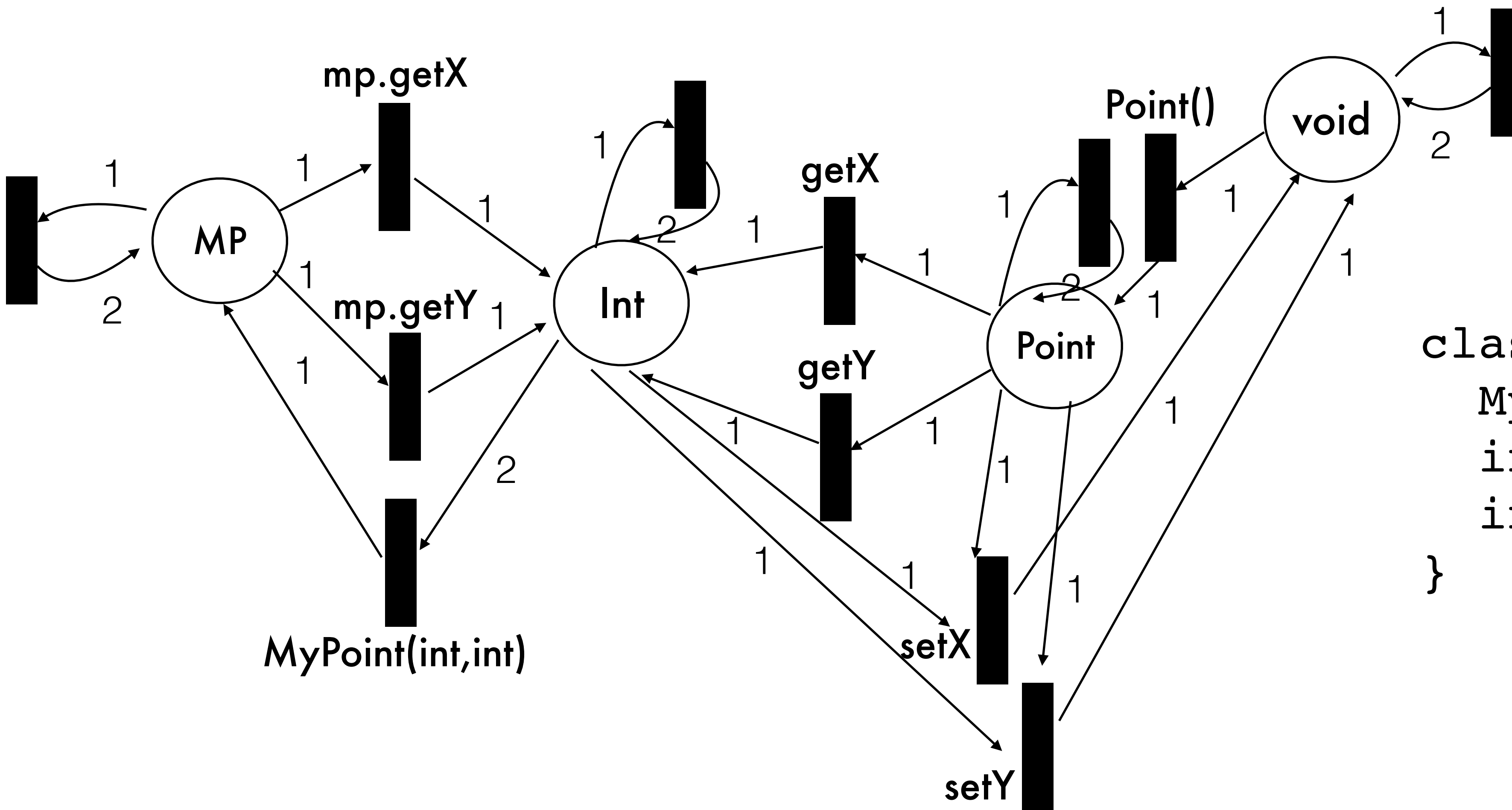
```
class MyPoint {  
    MyPoint(int x, int y);  
    int getX();  
    int getY();  
}
```



# Building a Petri Net



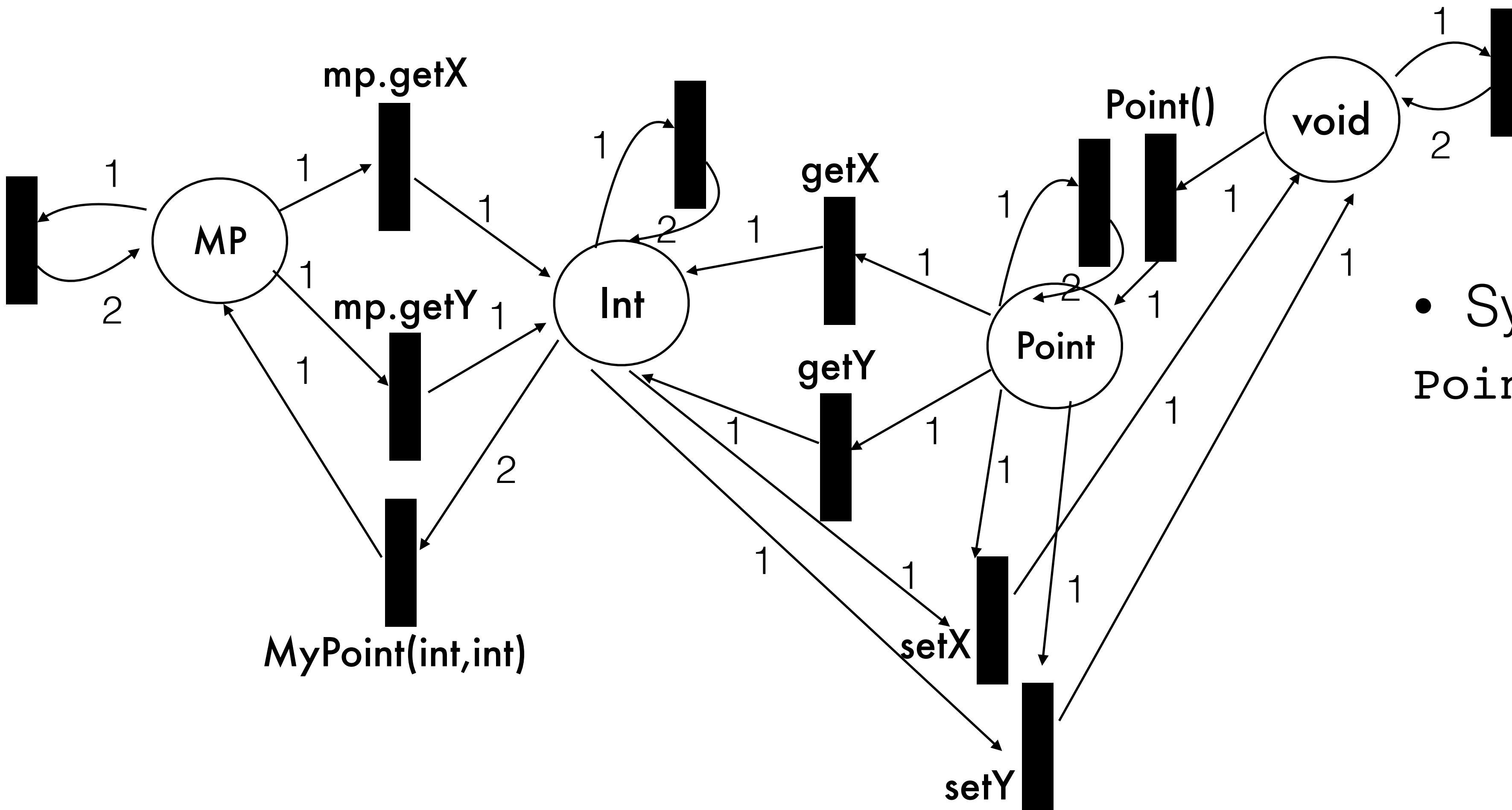
# Building a Petri Net



```
class MyPoint {
    MyPoint(int x, int y);
    int getX();
    int getY();
}
```



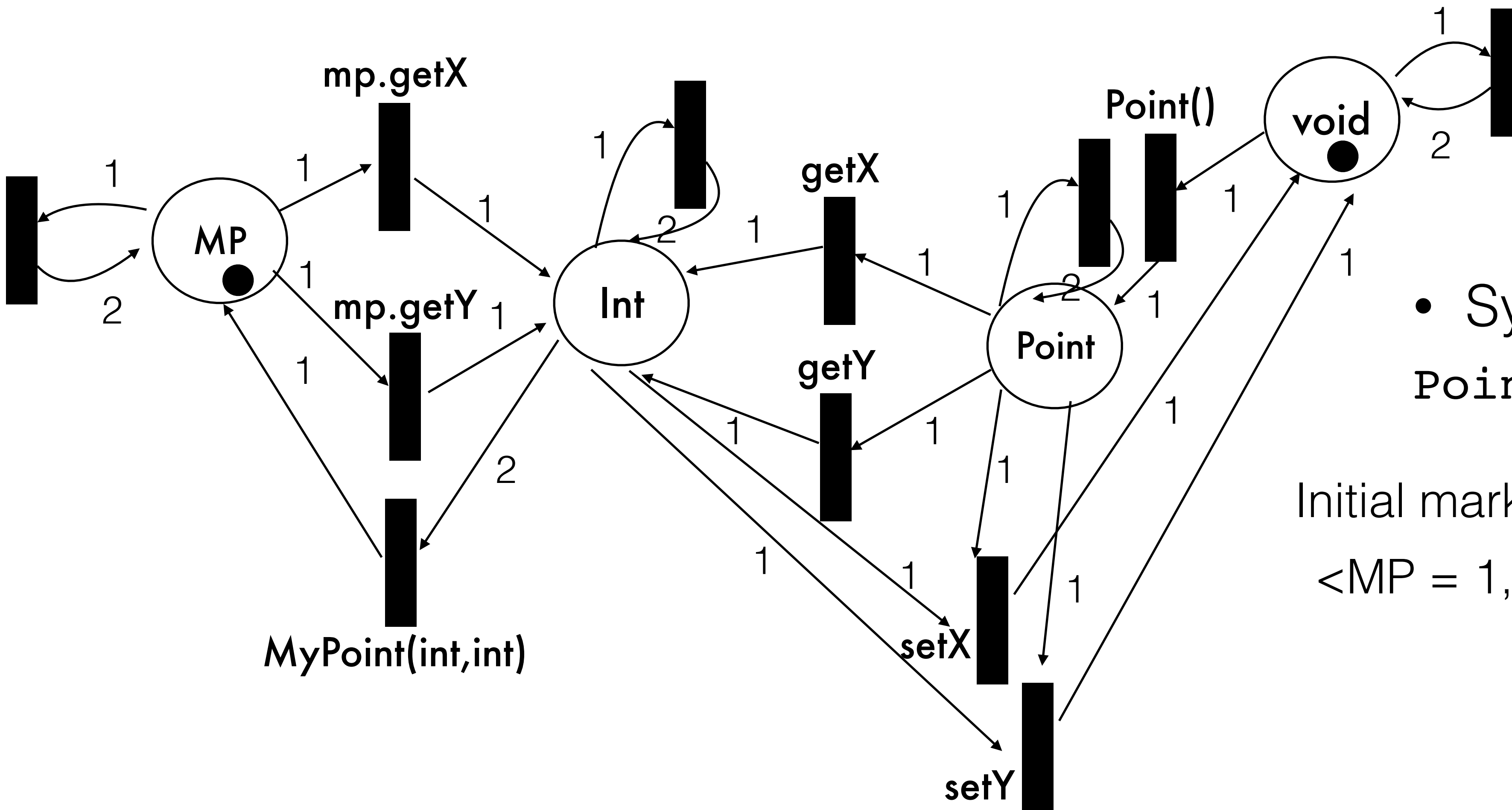
# What is the Initial Marking?



- Synthesize this function:  
`Point convert(MyPoint pt)`



# What is the Initial Marking?



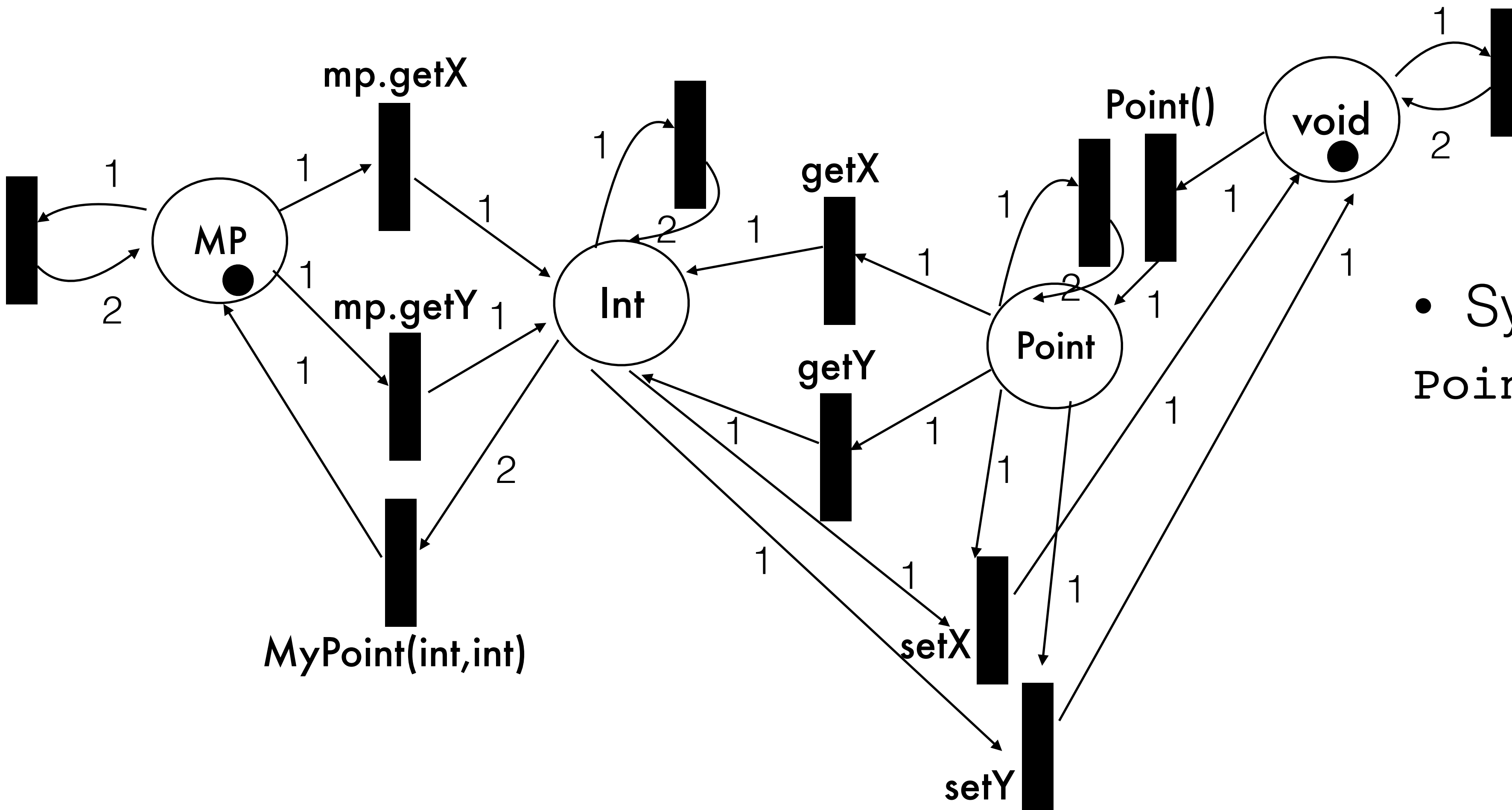
- Synthesize this function:  
`Point convert(MyPoint pt)`

Initial marking:

$\langle \text{MP} = 1, \text{void} = 1, \text{Int} = 0, \text{Point} = 0 \rangle$



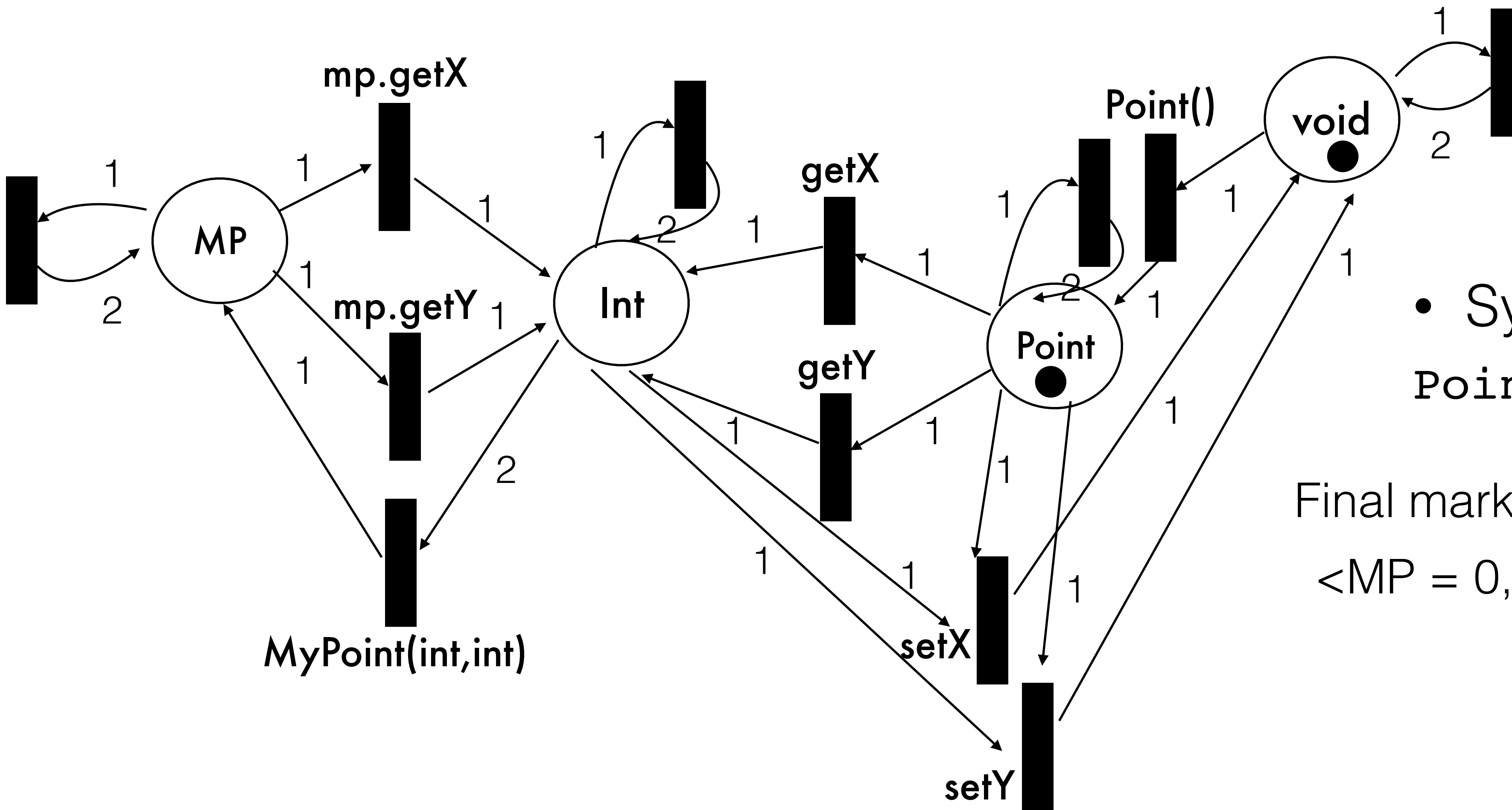
# What is the Final Marking?



- Synthesize this function:  
`Point convert(MyPoint pt)`



# What is the Final Marking?



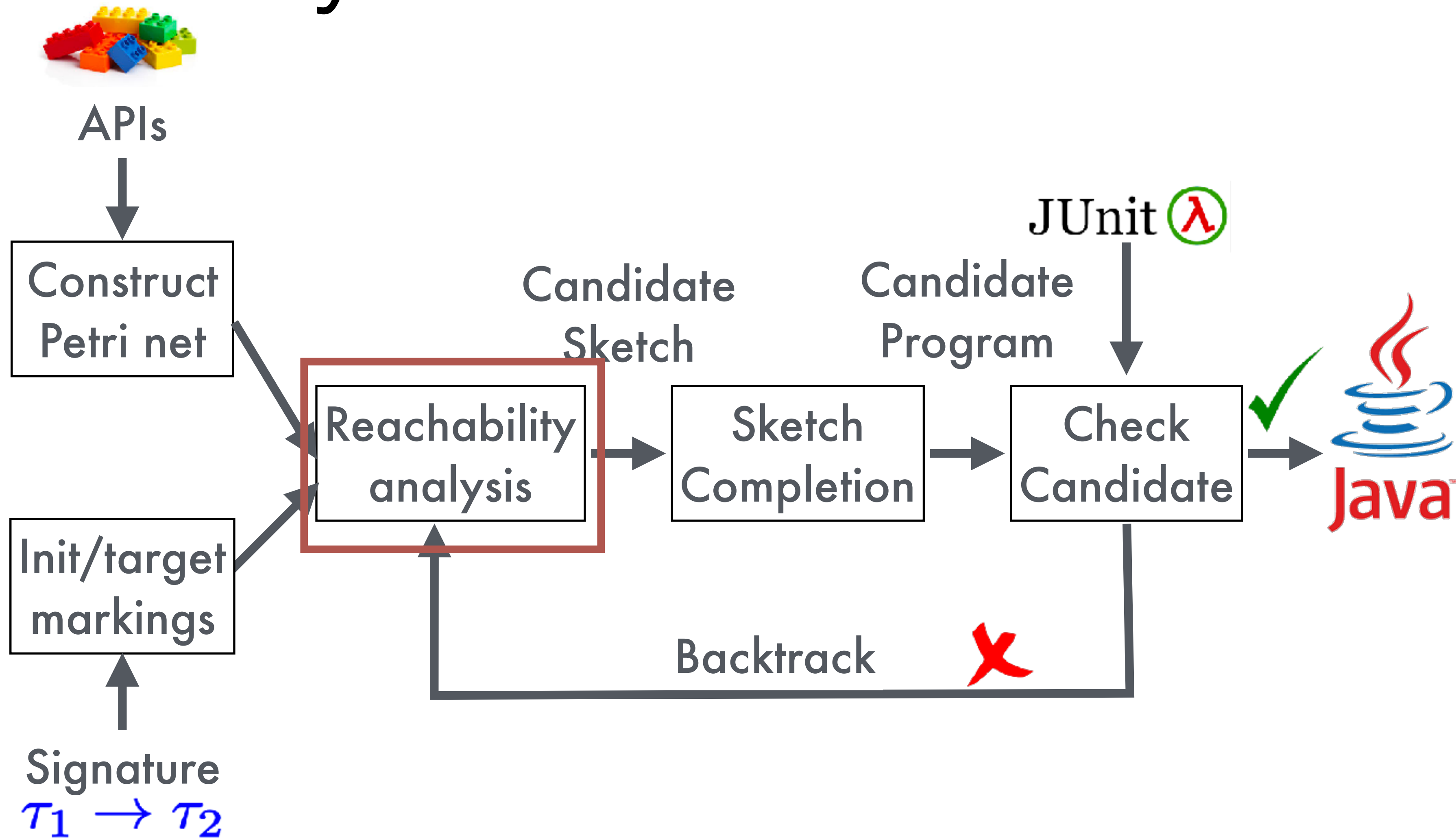
- Synthesize this function:  
`Point convert(MyPoint pt)`

Final marking:

$\langle \text{MP} = 0, \text{void} = *, \text{Int} = 0, \text{Point} = 1 \rangle$



# SyPet Architecture





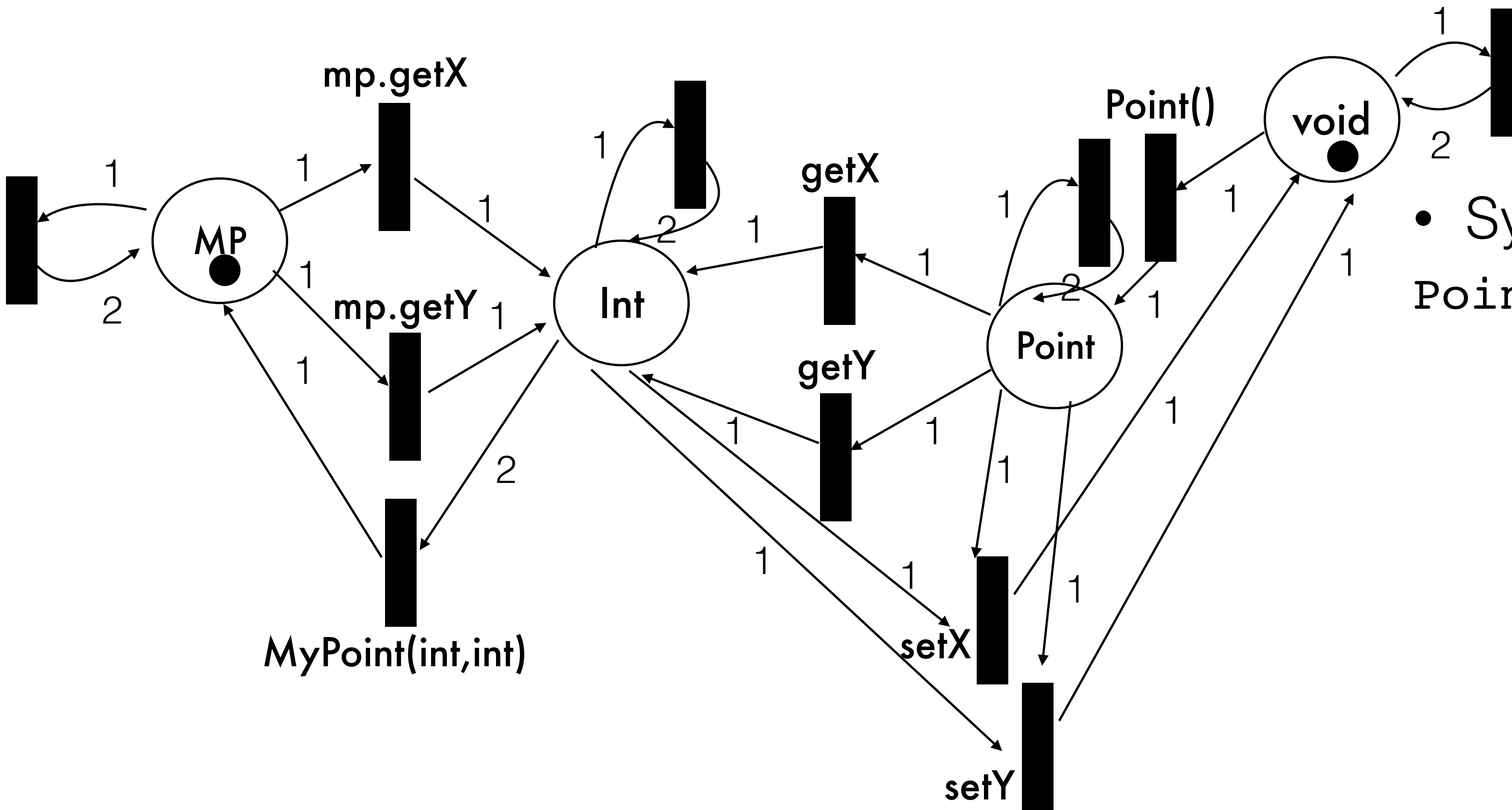
# Reachability Analysis

**All accepting runs of Petri net correspond to method call sequences with desired type signature!**

- Need to perform reachability analysis to identify accepting runs of the Petri net
- Reachability analysis of Petri nets can be encoded to SAT:
  - Find a reachable path of size  $k$
  - Enumerate all reachable paths



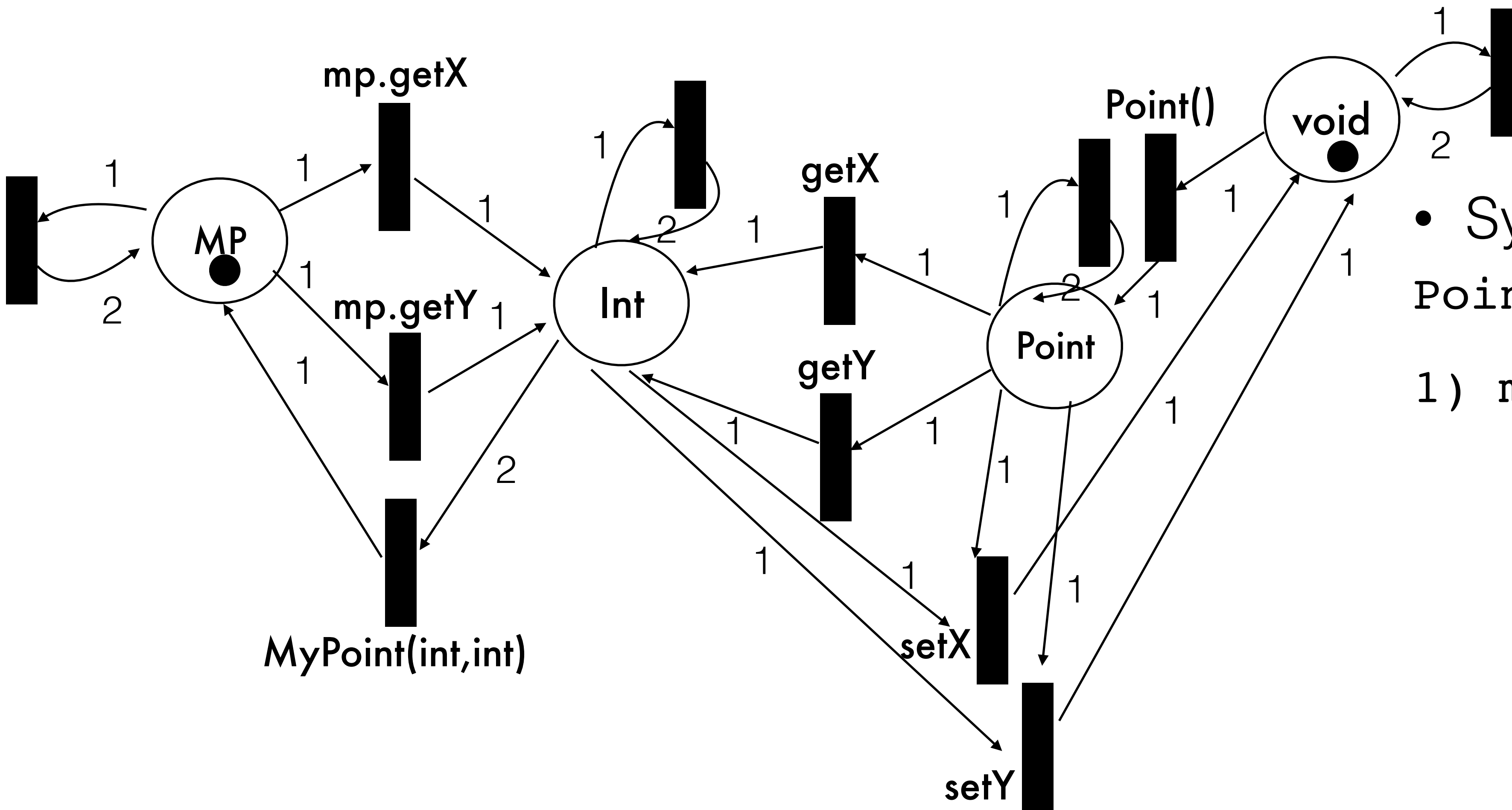
# Reachable Paths



- Synthesize this function:  
`Point convert(MyPoint pt)`



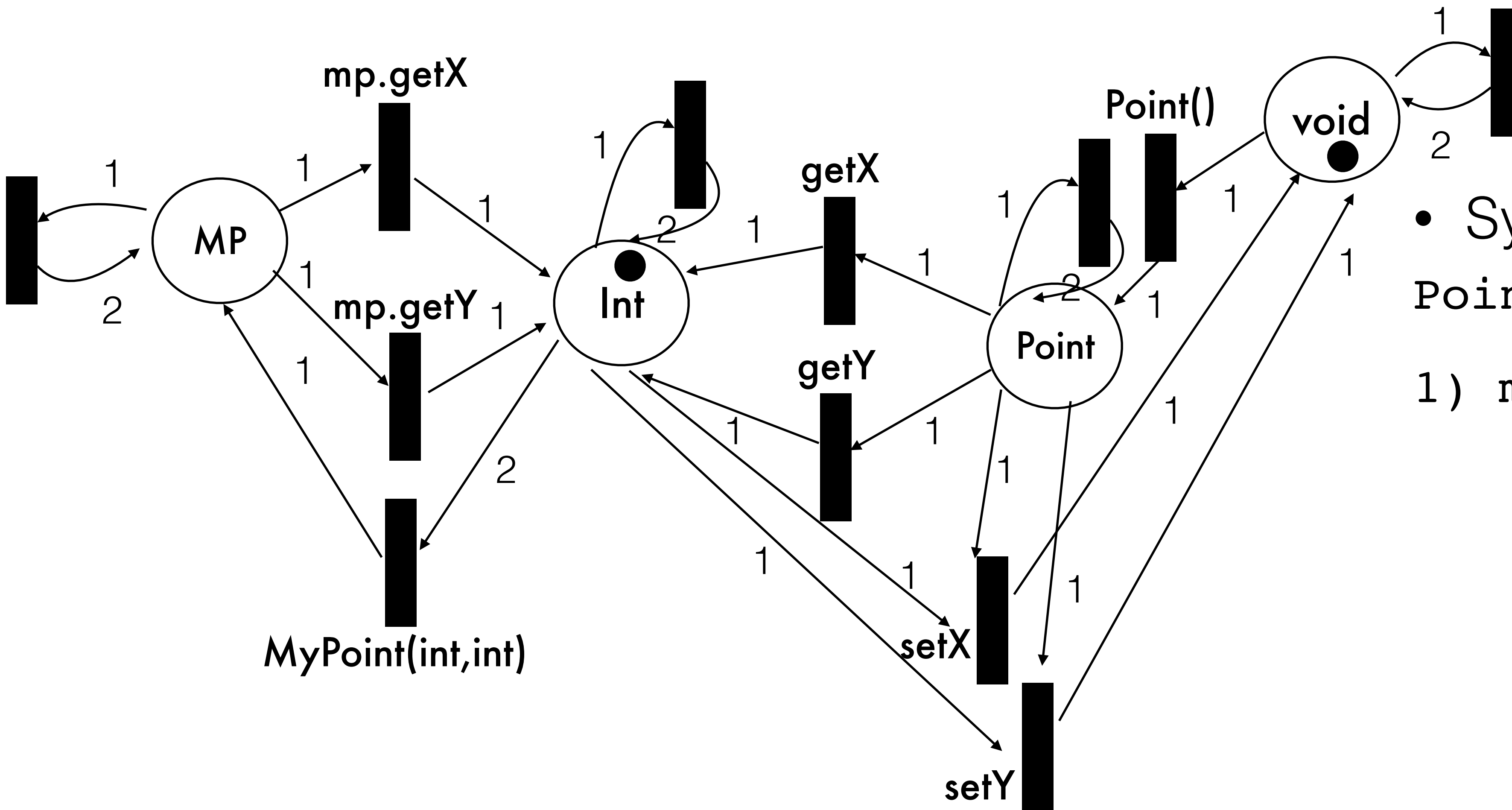
# Not all Reachable Paths are a Solution!



- Synthesize this function:  
`Point convert(MyPoint pt)`  
1) `mp.getX`



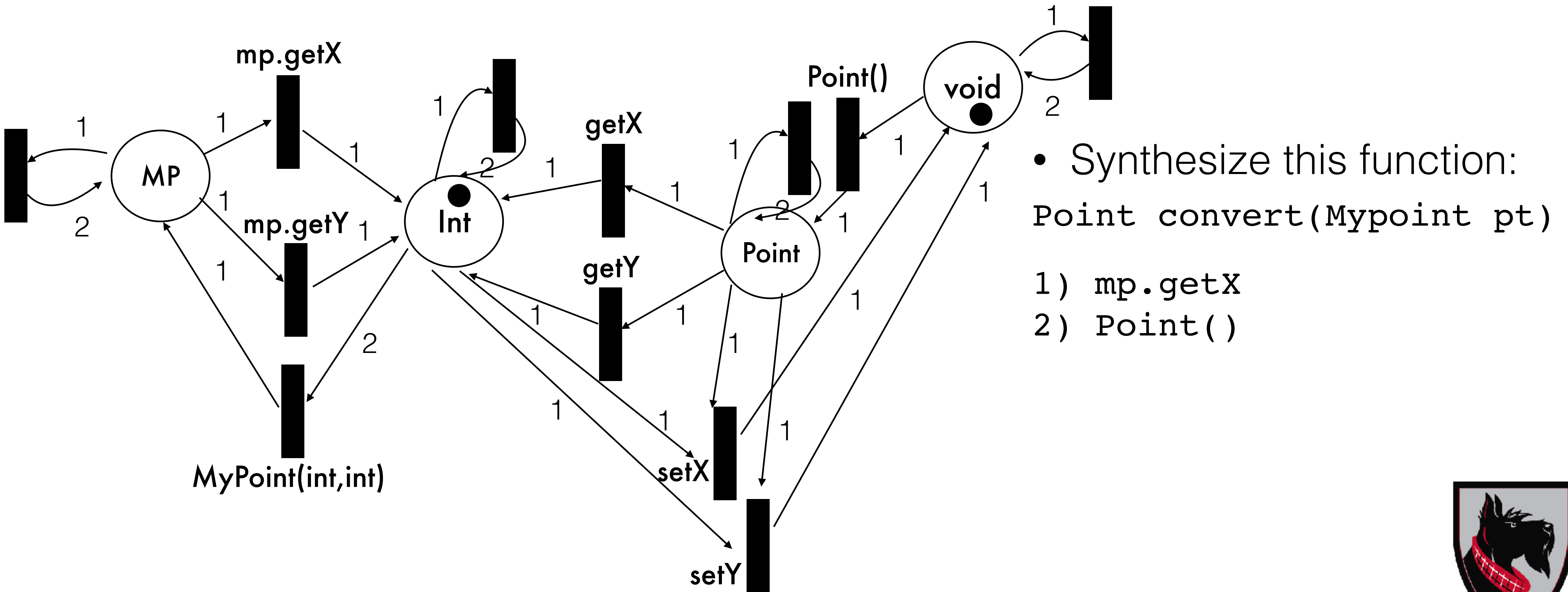
# Not all Reachable Paths are a Solution!



- Synthesize this function:  
`Point convert(MyPoint pt)`  
1) `mp.getX`



# Not all Reachable Paths are a Solution!

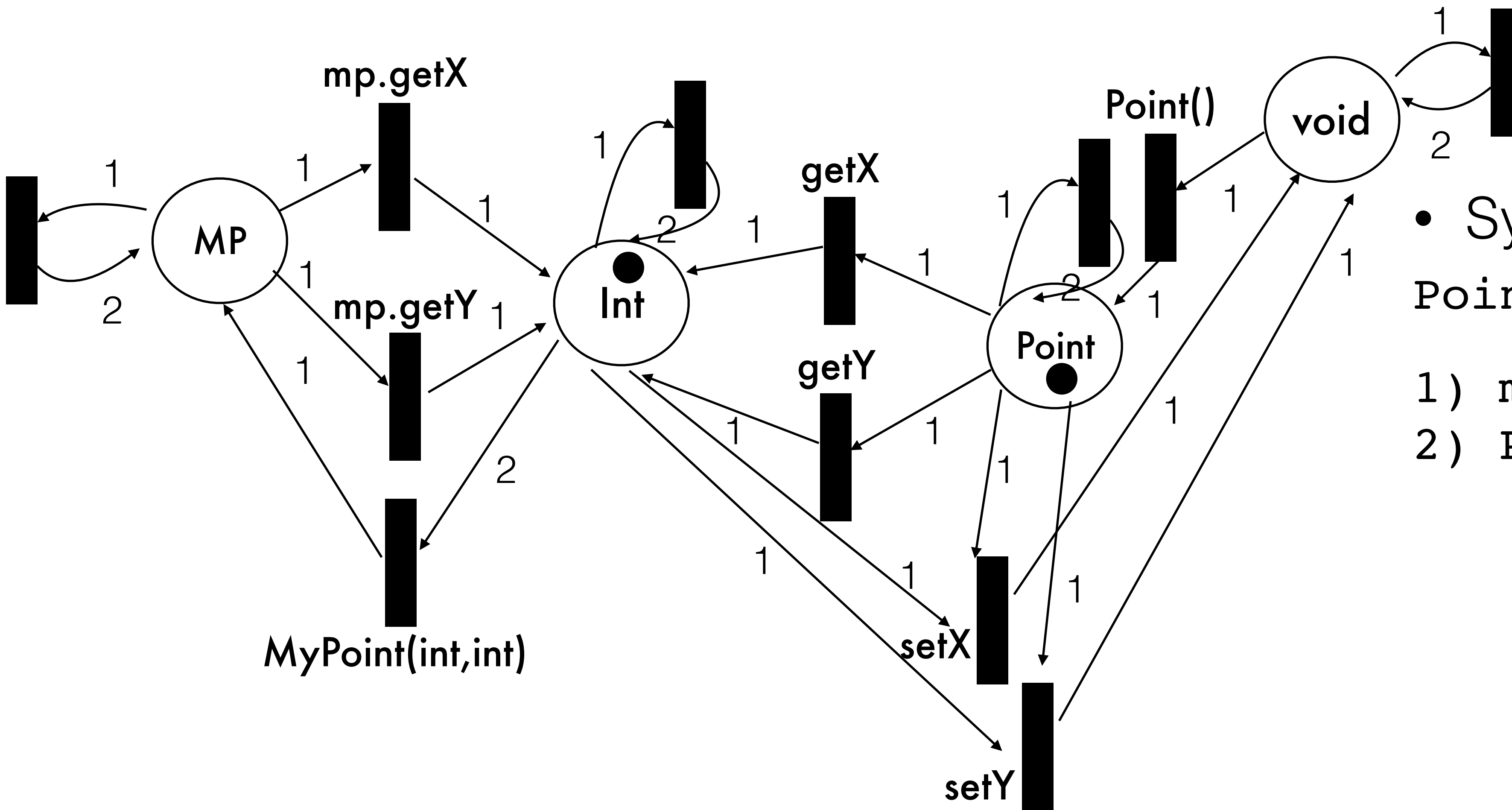


• Synthesize this function:  
`Point convert(MyPoint pt)`

- 1) `mp.getX`
- 2) `Point()`



# Not all Reachable Paths are a Solution!

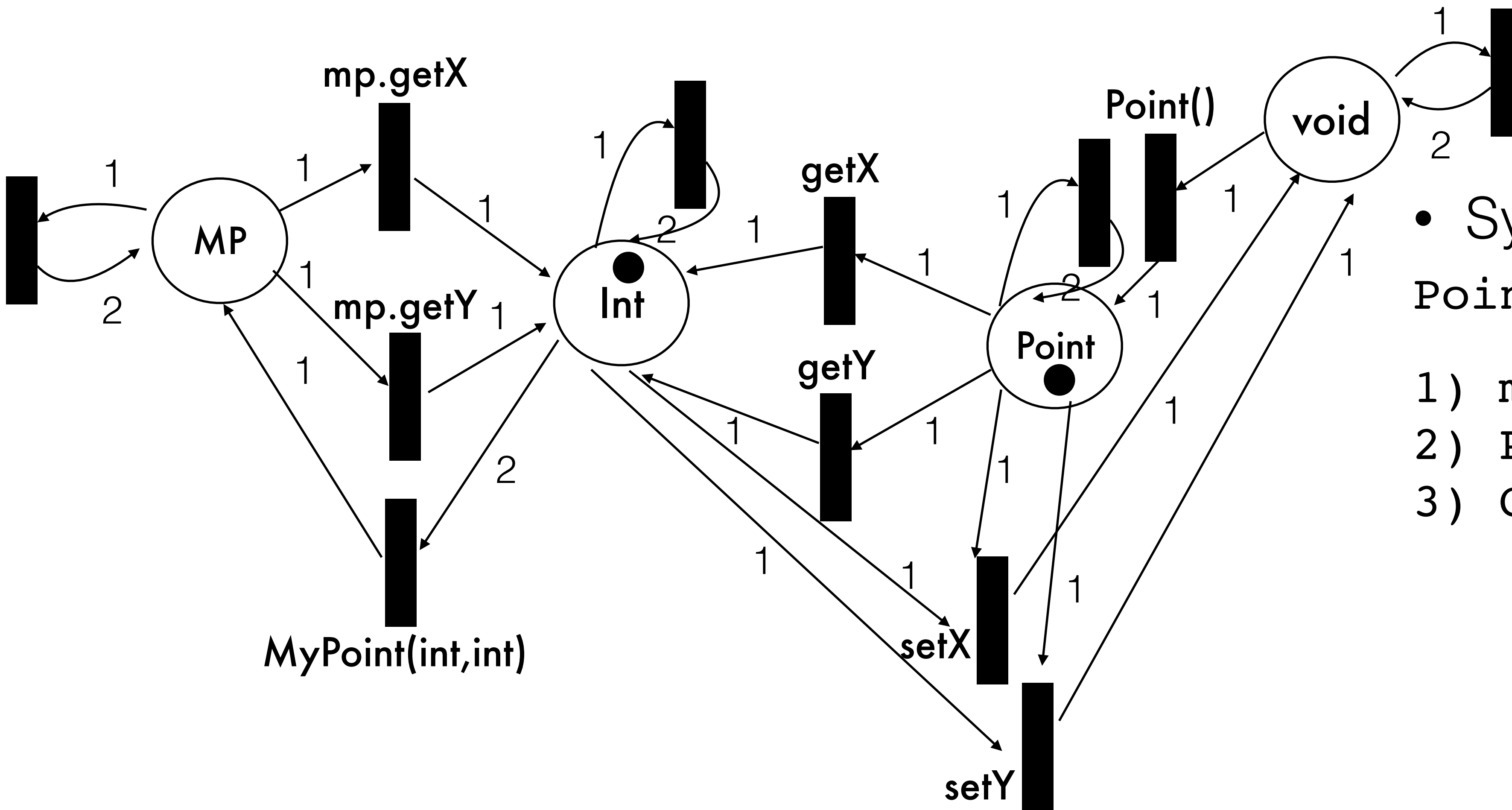


• Synthesize this function:  
`Point convert(MyPoint pt)`

- 1) `mp.getX`
- 2) `Point()`



# Not all Reachable Paths are a Solution!

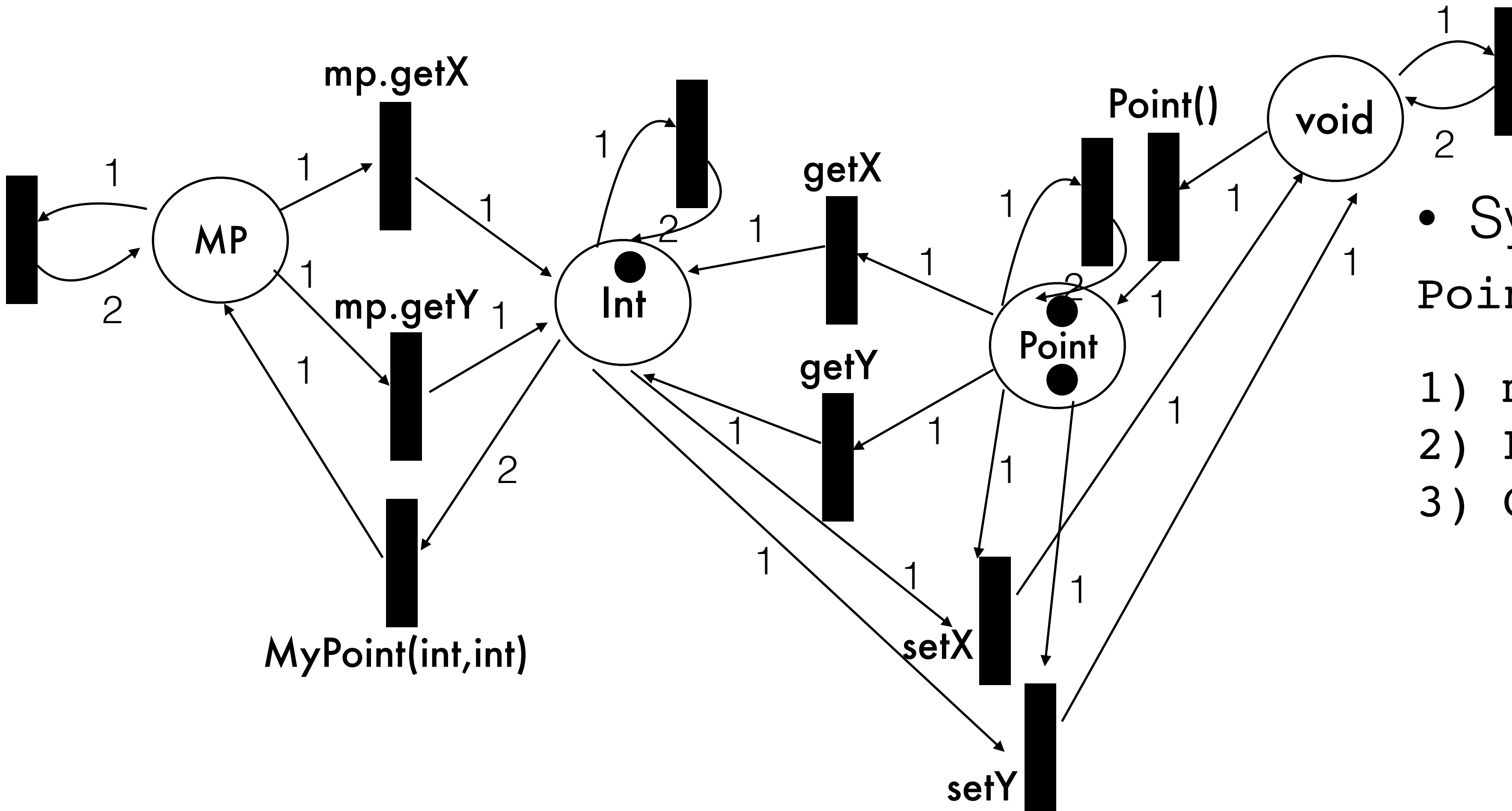


- Synthesize this function:  
`Point convert(MyPoint pt)`

- 1) `mp.getX`
- 2) `Point()`
- 3) `Clone-Point`



# Not all Reachable Paths are a Solution!



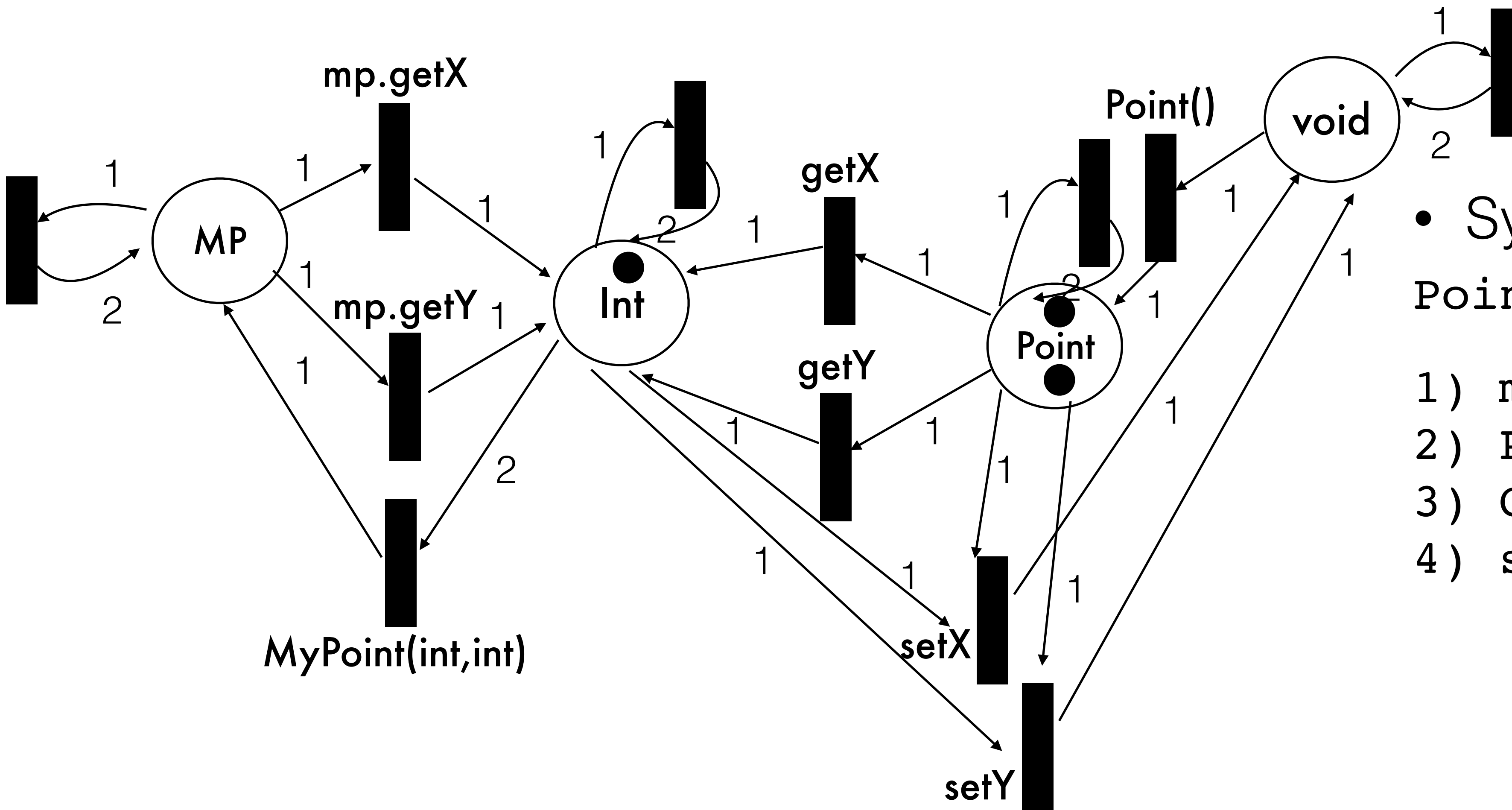
- Synthesize this function:  
`Point convert(MyPoint pt)`

- 1) `mp.getX`
- 2) `Point()`
- 3) `Clone-Point`





# Not all Reachable Paths are a Solution!

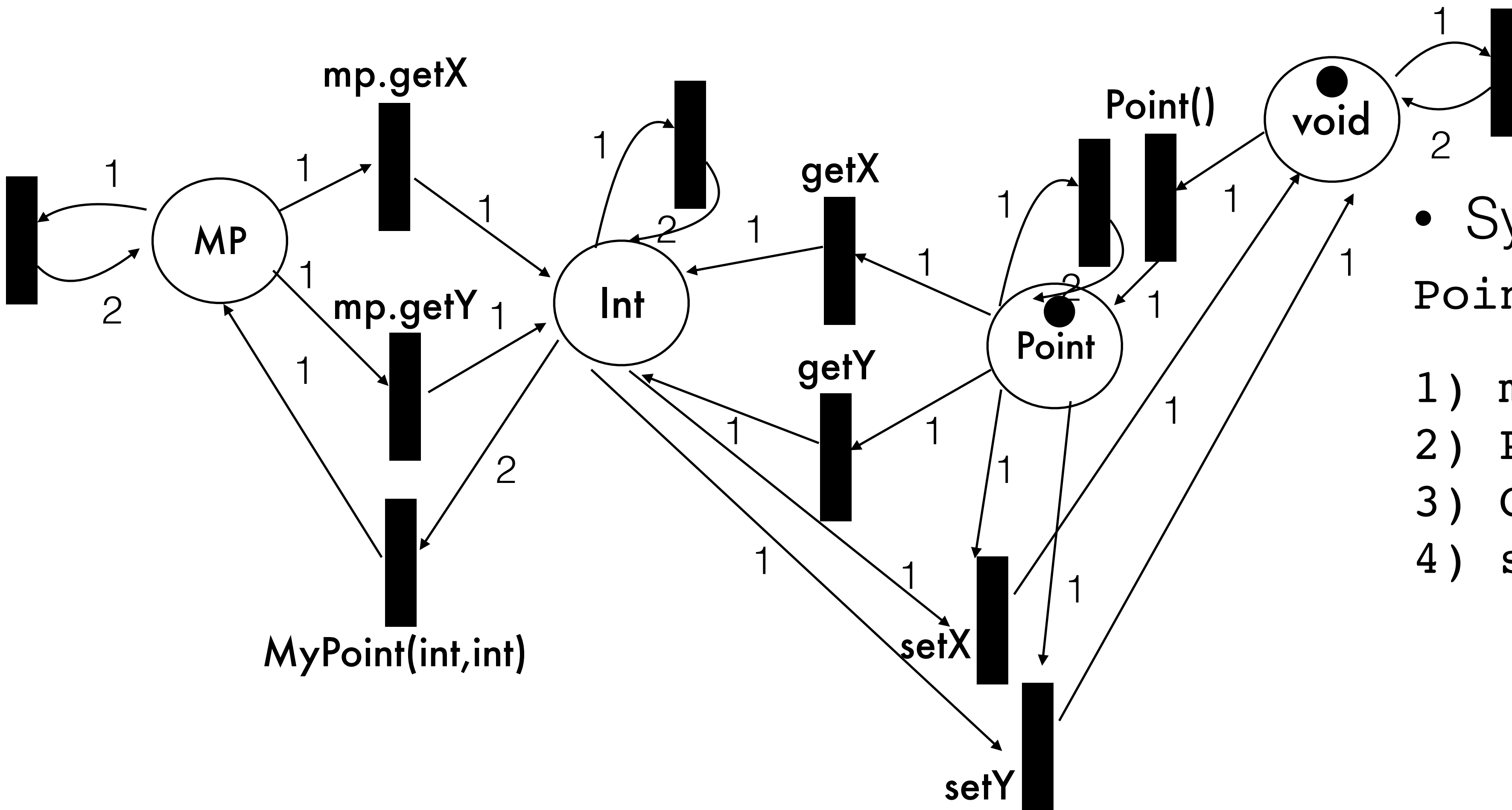


- Synthesize this function:  
`Point convert(MyPoint pt)`

- 1) `mp.getX`
- 2) `Point()`
- 3) `Clone-Point`
- 4) `setX`



# Not all Reachable Paths are a Solution!

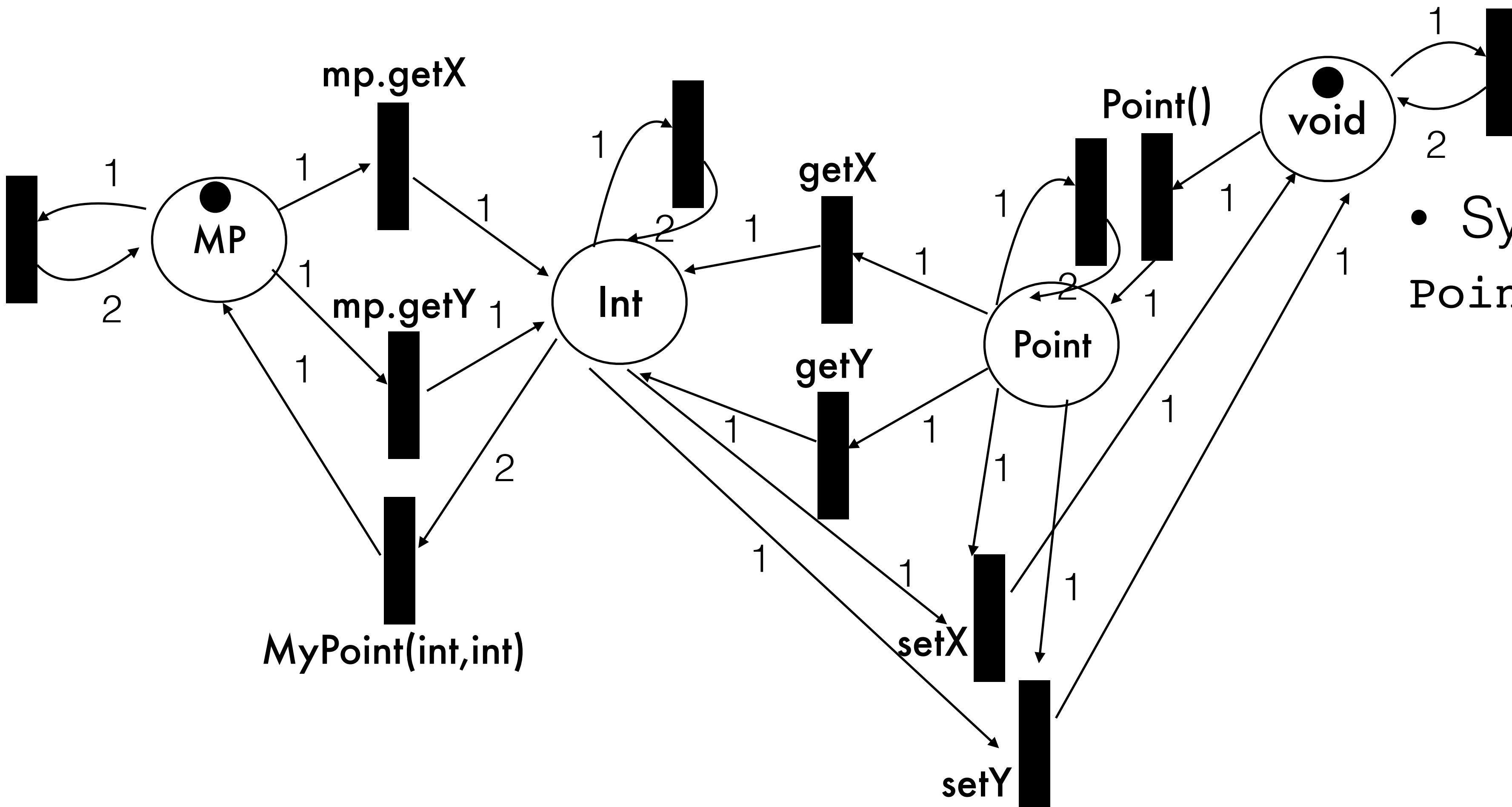


• Synthesize this function:  
Point convert(MyPoint pt)

- 1) mp.getX
- 2) Point()
- 3) Clone-Point
- 4) setX



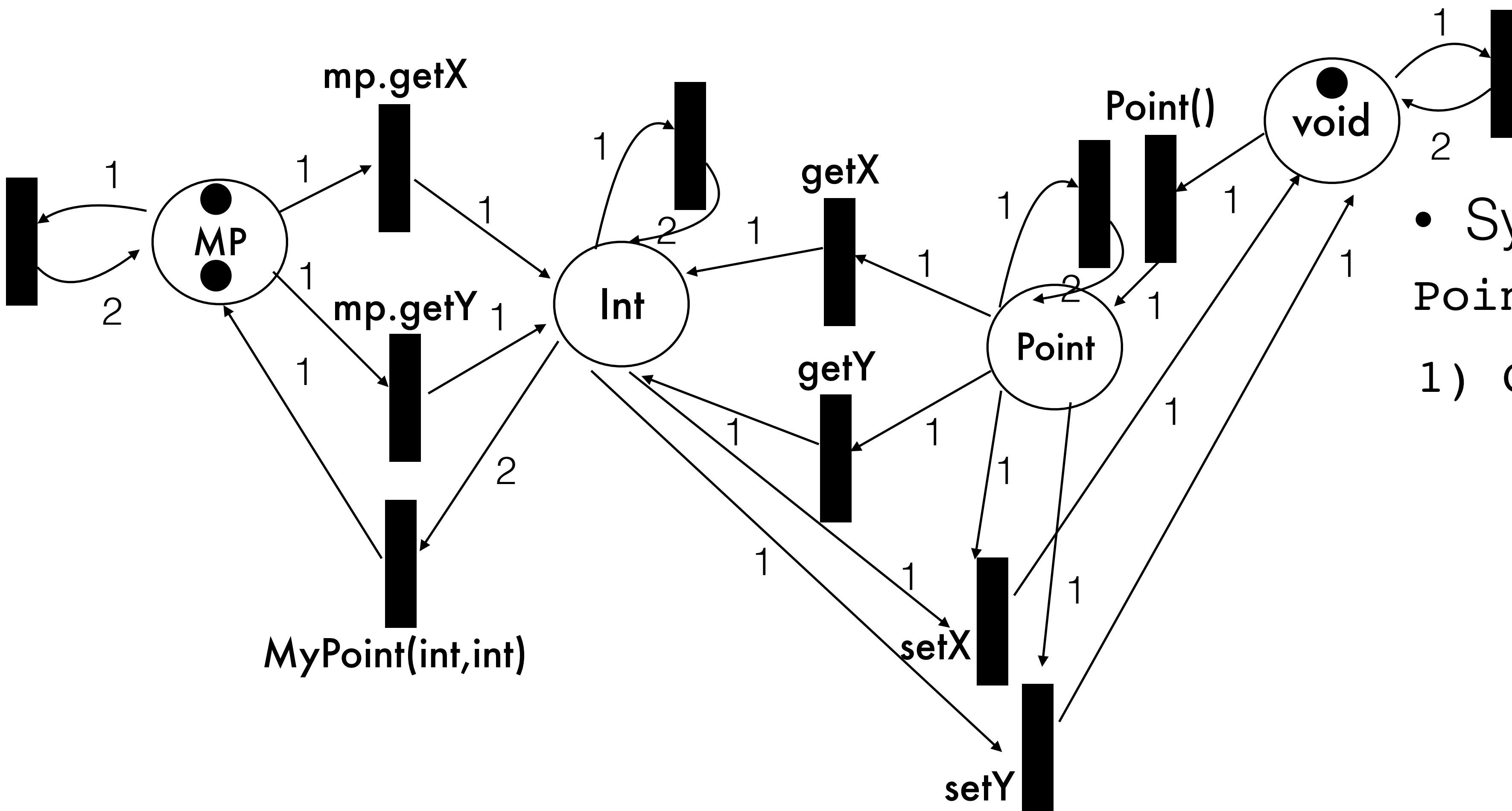
# Reachable Path that Corresponds to a Solution



- Synthesize this function:  
`Point convert(MyPoint pt)`



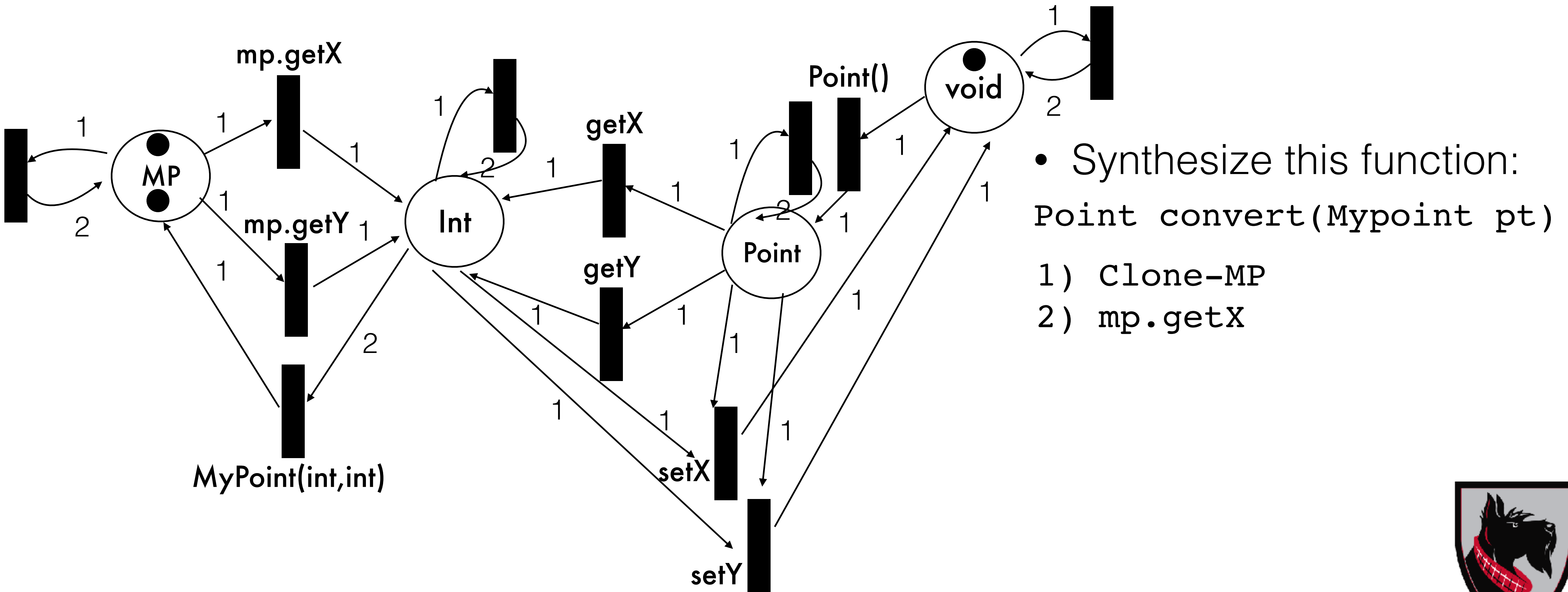
# Reachable Path that Corresponds to a Solution



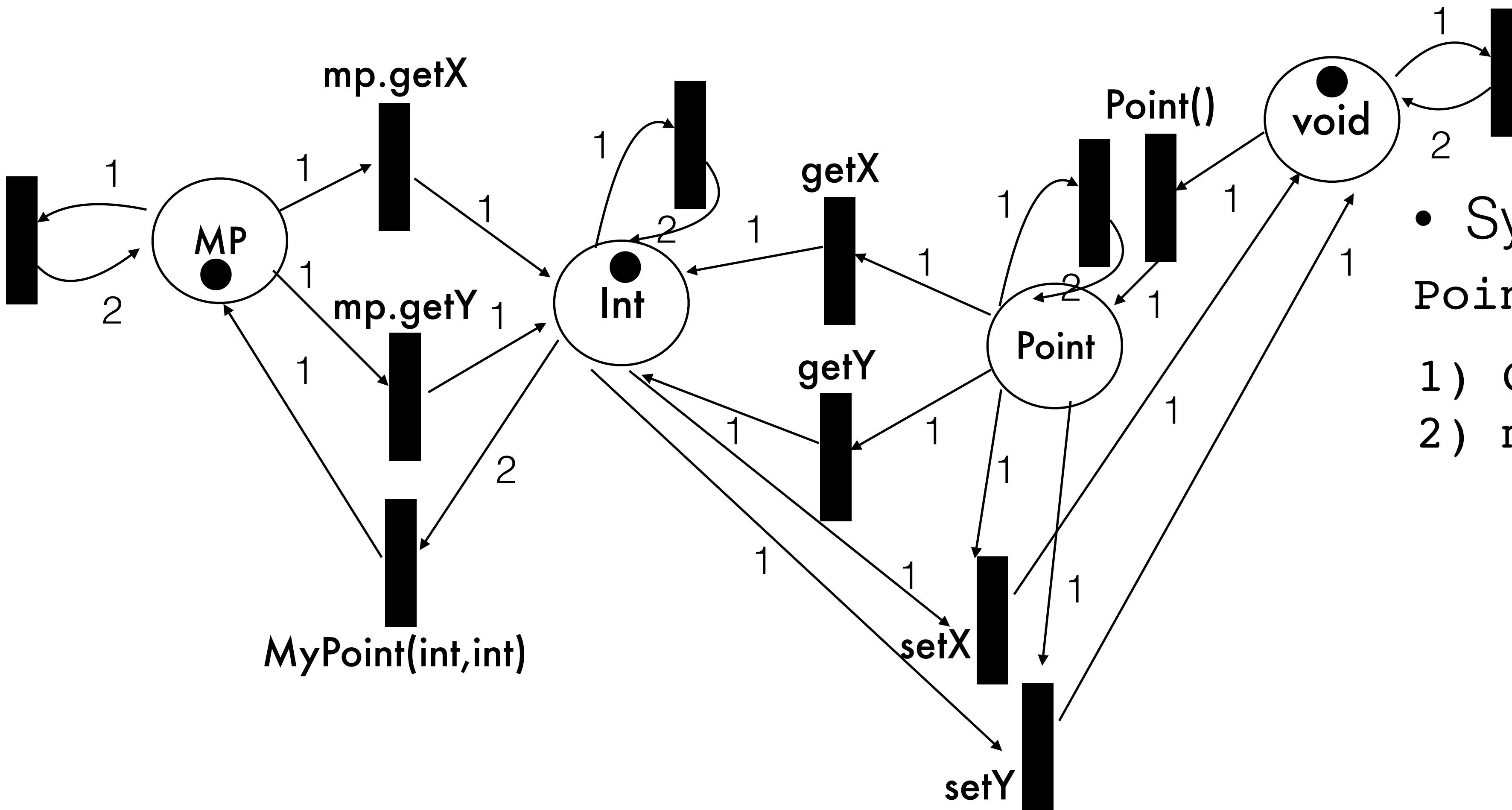
- Synthesize this function:  
`Point convert(MyPoint pt)`  
1) Clone-MP



# Reachable Path that Corresponds to a Solution



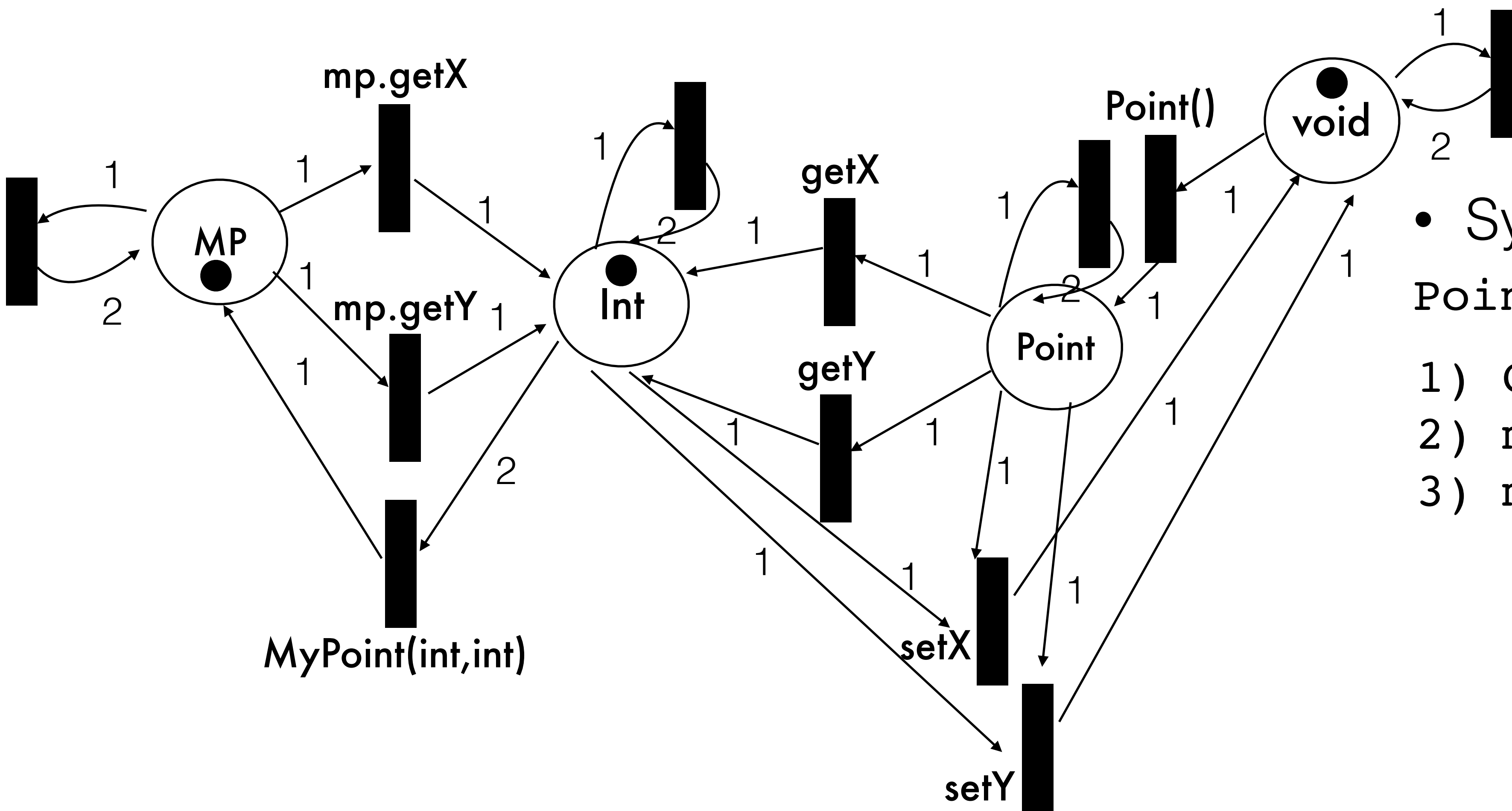
# Reachable Path that Corresponds to a Solution



- Synthesize this function:  
`Point convert(MyPoint pt)`
  - 1) `Clone-MP`
  - 2) `mp.getX`



# Reachable Path that Corresponds to a Solution

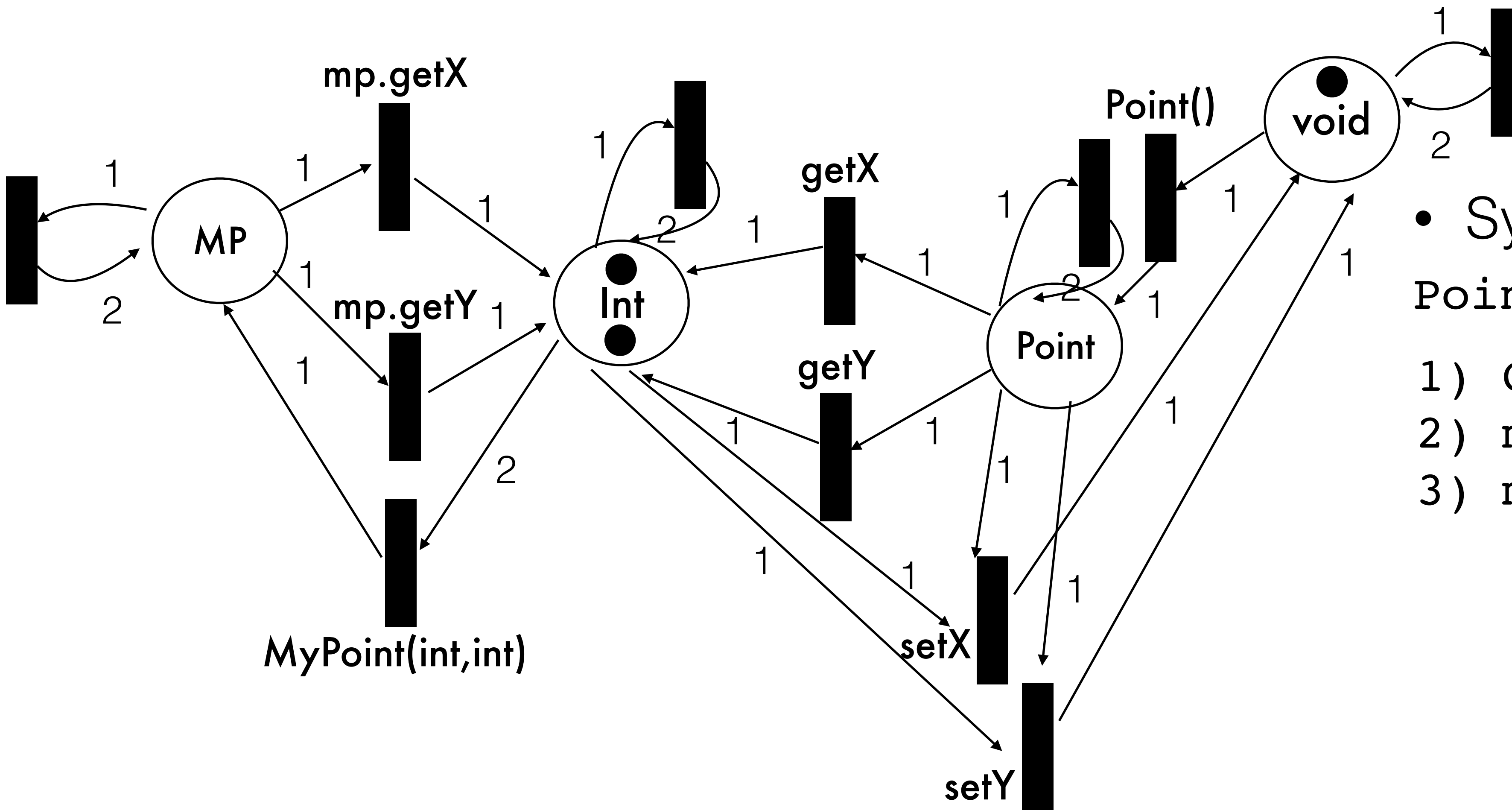


- Synthesize this function:  
Point convert(MyPoint pt)

- 1) Clone-MP
- 2) mp.getX
- 3) mp.getY



# Reachable Path that Corresponds to a Solution



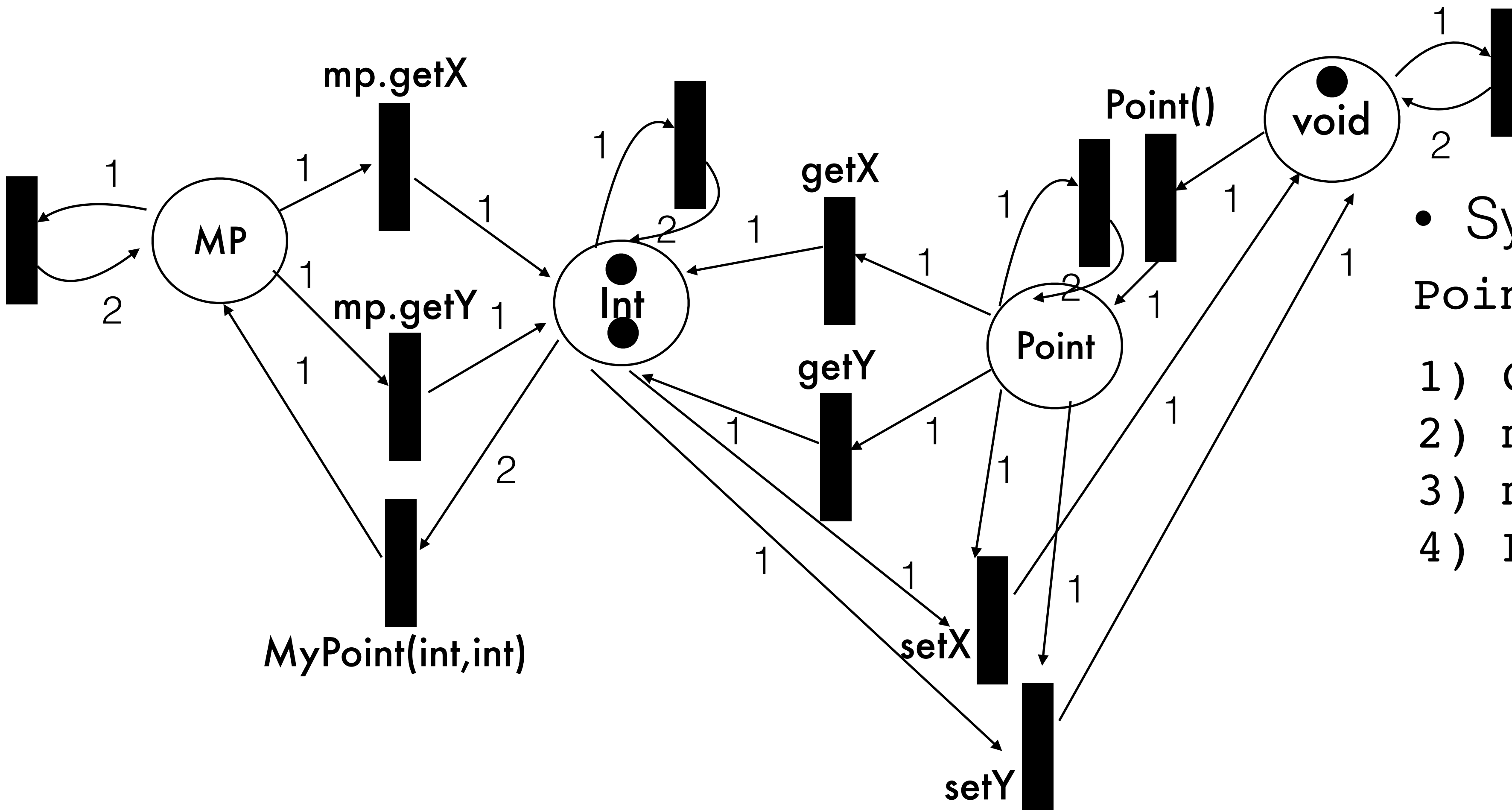
• Synthesize this function:  
`Point convert(MyPoint pt)`

- 1) Clone-MP
- 2) mp.getX
- 3) mp.getY





# Reachable Path that Corresponds to a Solution

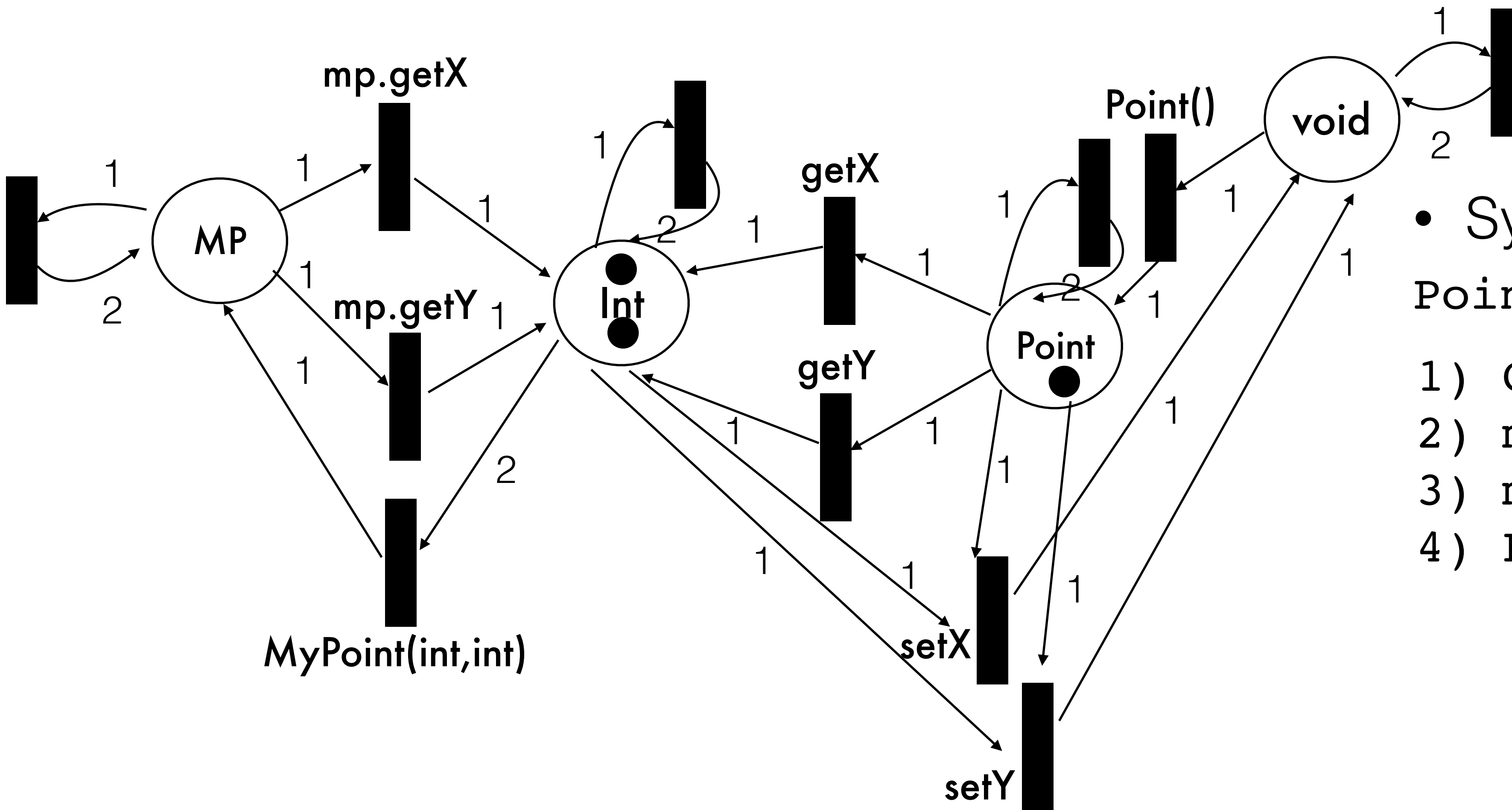


- Synthesize this function:  
`Point convert(MyPoint pt)`

- 1) Clone-MP
- 2) `mp.getX`
- 3) `mp.getY`
- 4) `Point()`



# Reachable Path that Corresponds to a Solution

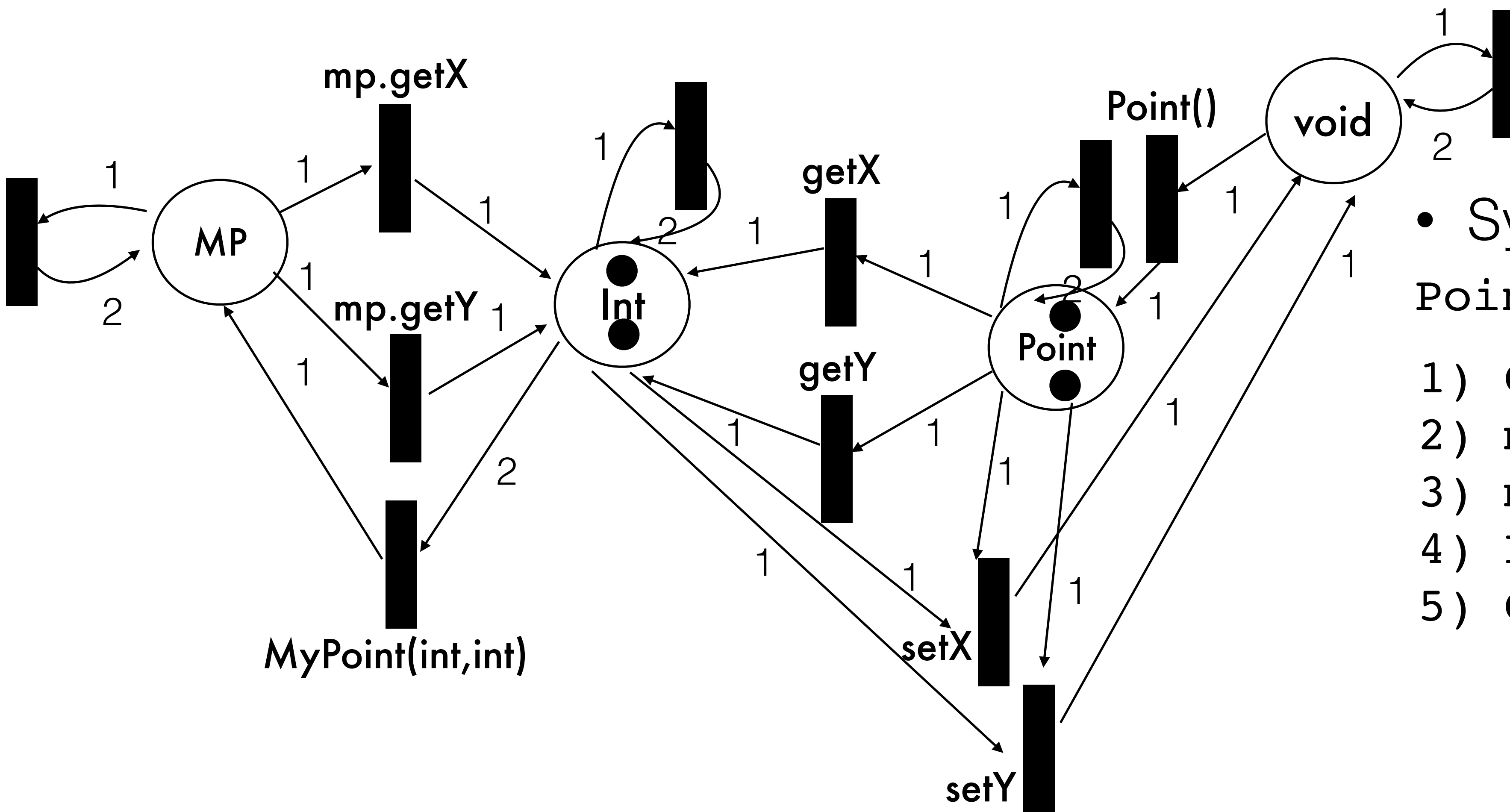


• Synthesize this function:  
`Point convert(MyPoint pt)`

- 1) Clone-MP
- 2) mp.getX
- 3) mp.getY
- 4) Point()



# Reachable Path that Corresponds to a Solution

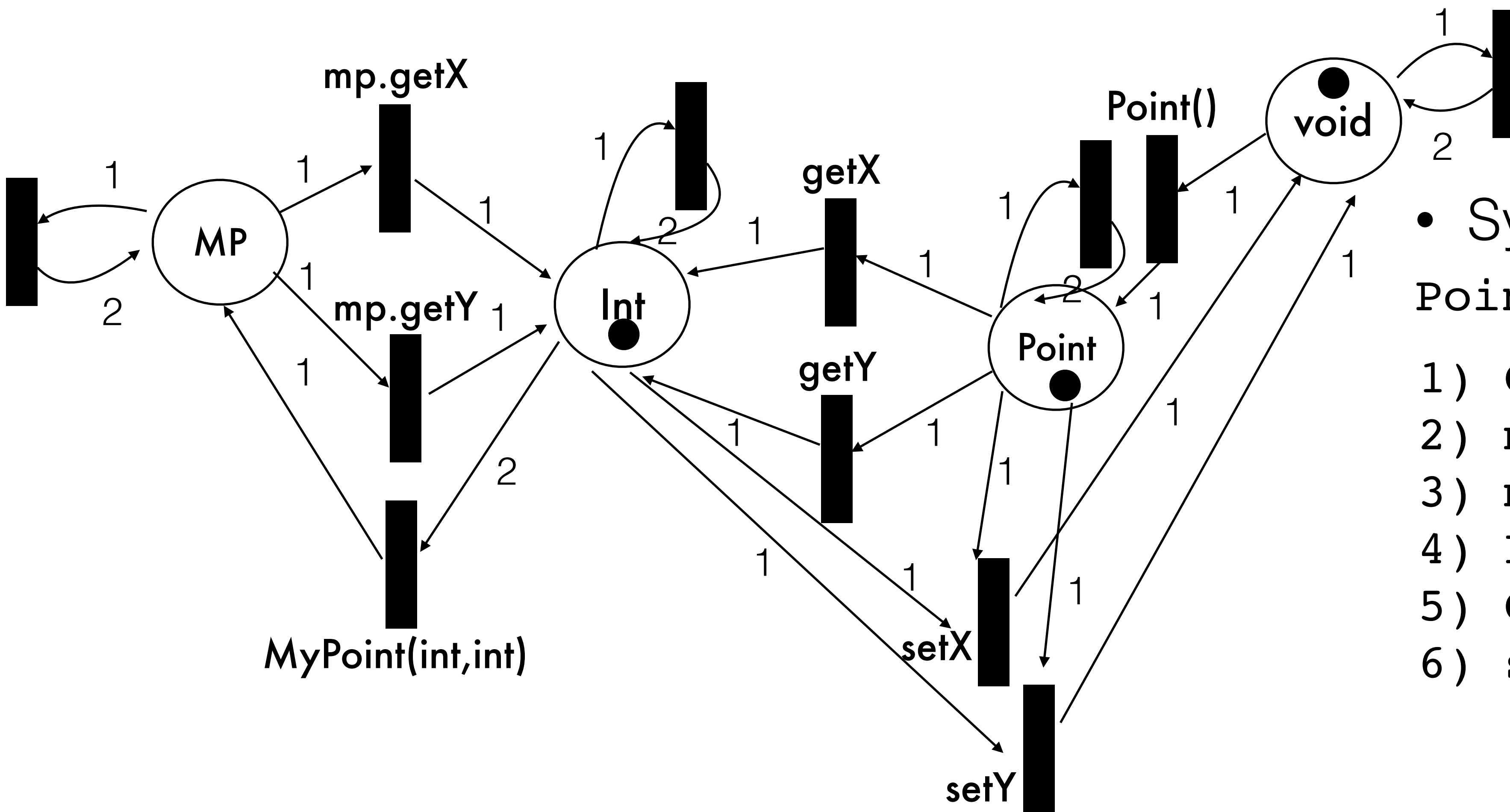


- Synthesize this function:  
`Point convert(MyPoint pt)`

- 1) Clone-MP
- 2) mp.getX
- 3) mp.getY
- 4) Point()
- 5) Clone-Point



# Reachable Path that Corresponds to a Solution

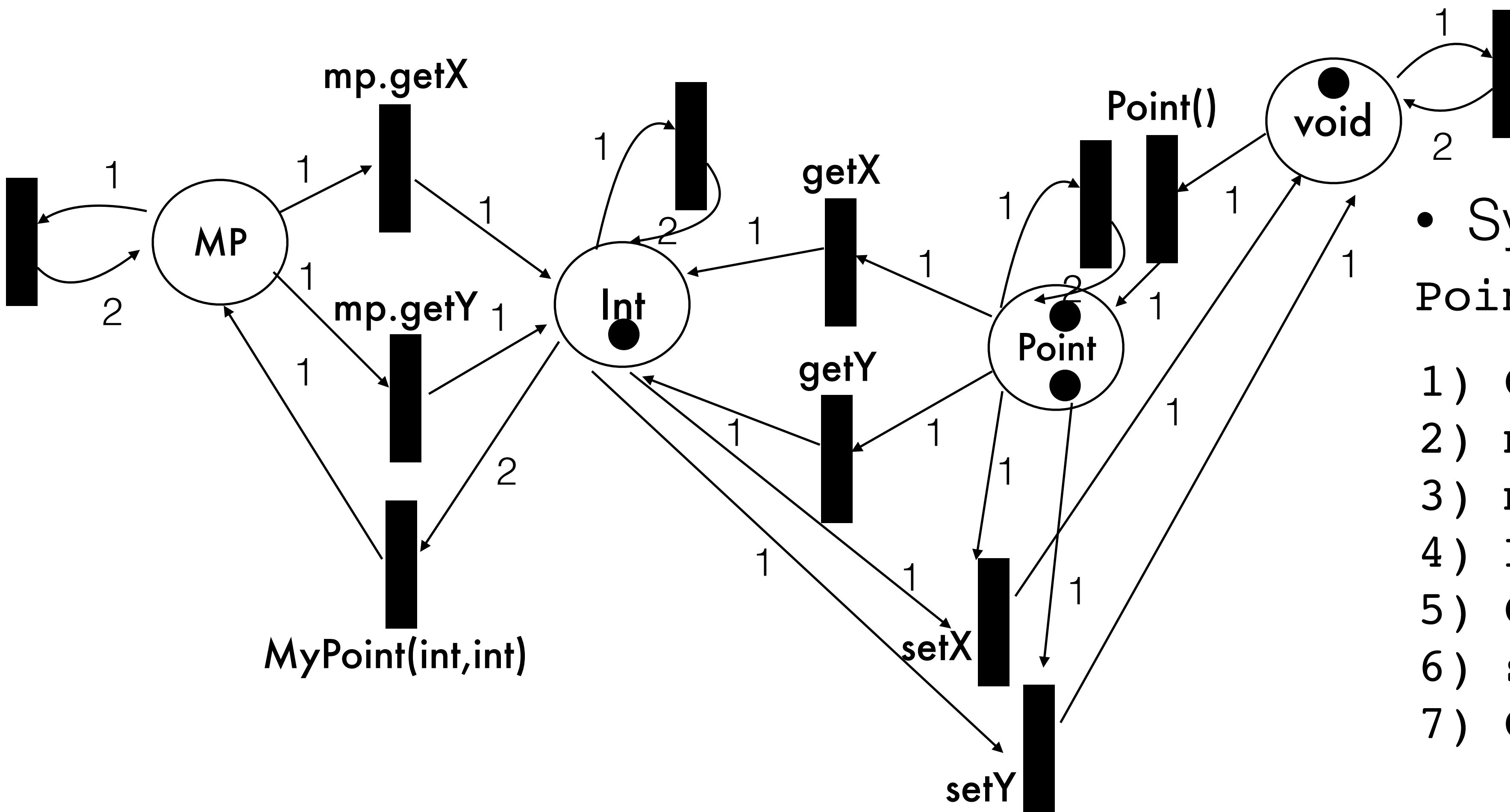


- Synthesize this function:  
`Point convert(MyPoint pt)`

- 1) Clone-MP
- 2) mp.getX
- 3) mp.getY
- 4) Point()
- 5) Clone-Point
- 6) setX



# Reachable Path that Corresponds to a Solution

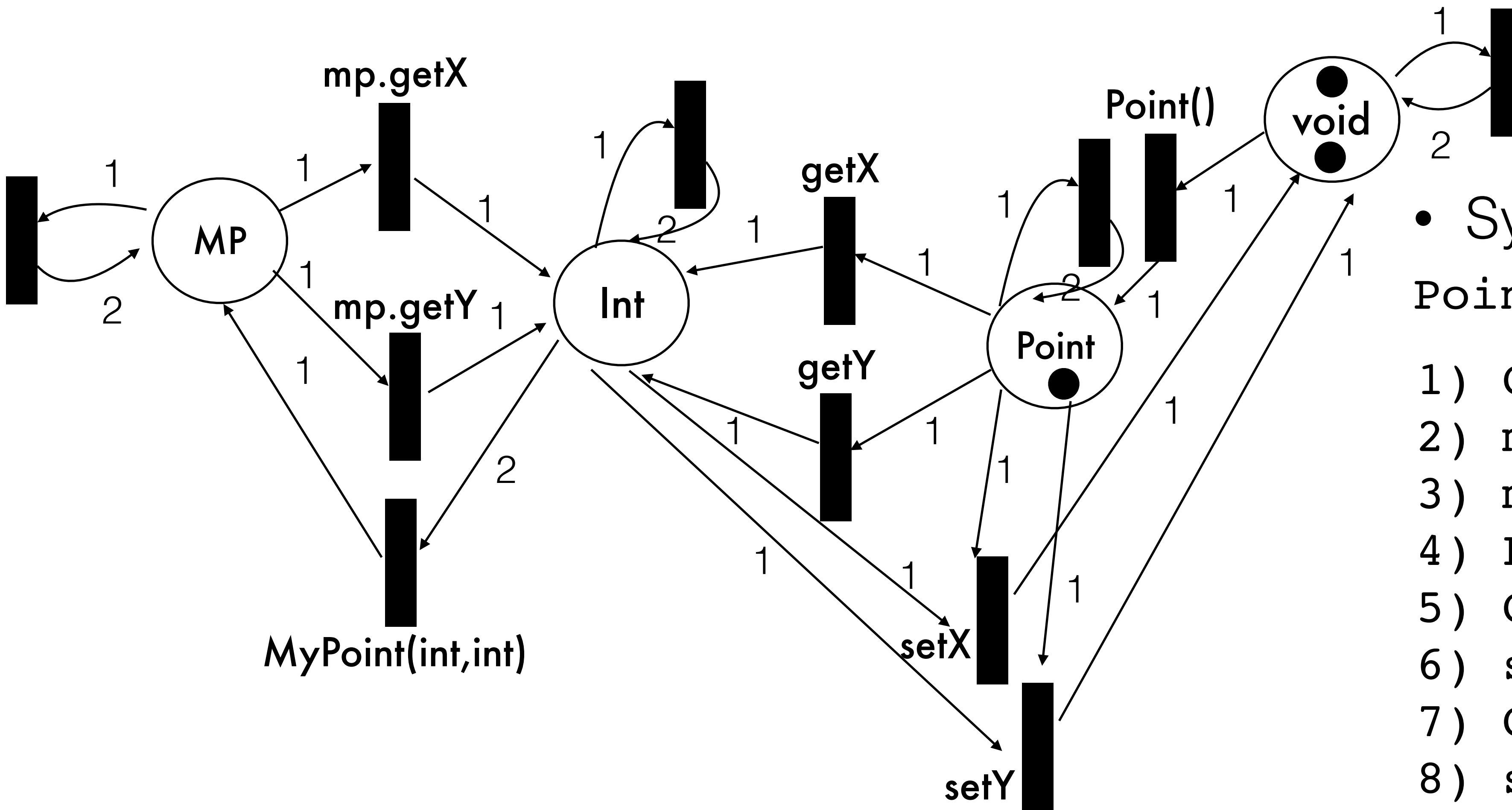


- Synthesize this function:  
`Point convert(MyPoint pt)`

- 1) Clone-MP
- 2) mp.getX
- 3) mp.getY
- 4) Point()
- 5) Clone-Point
- 6) setX
- 7) Clone-Point



# Reachable Path that Corresponds to a Solution

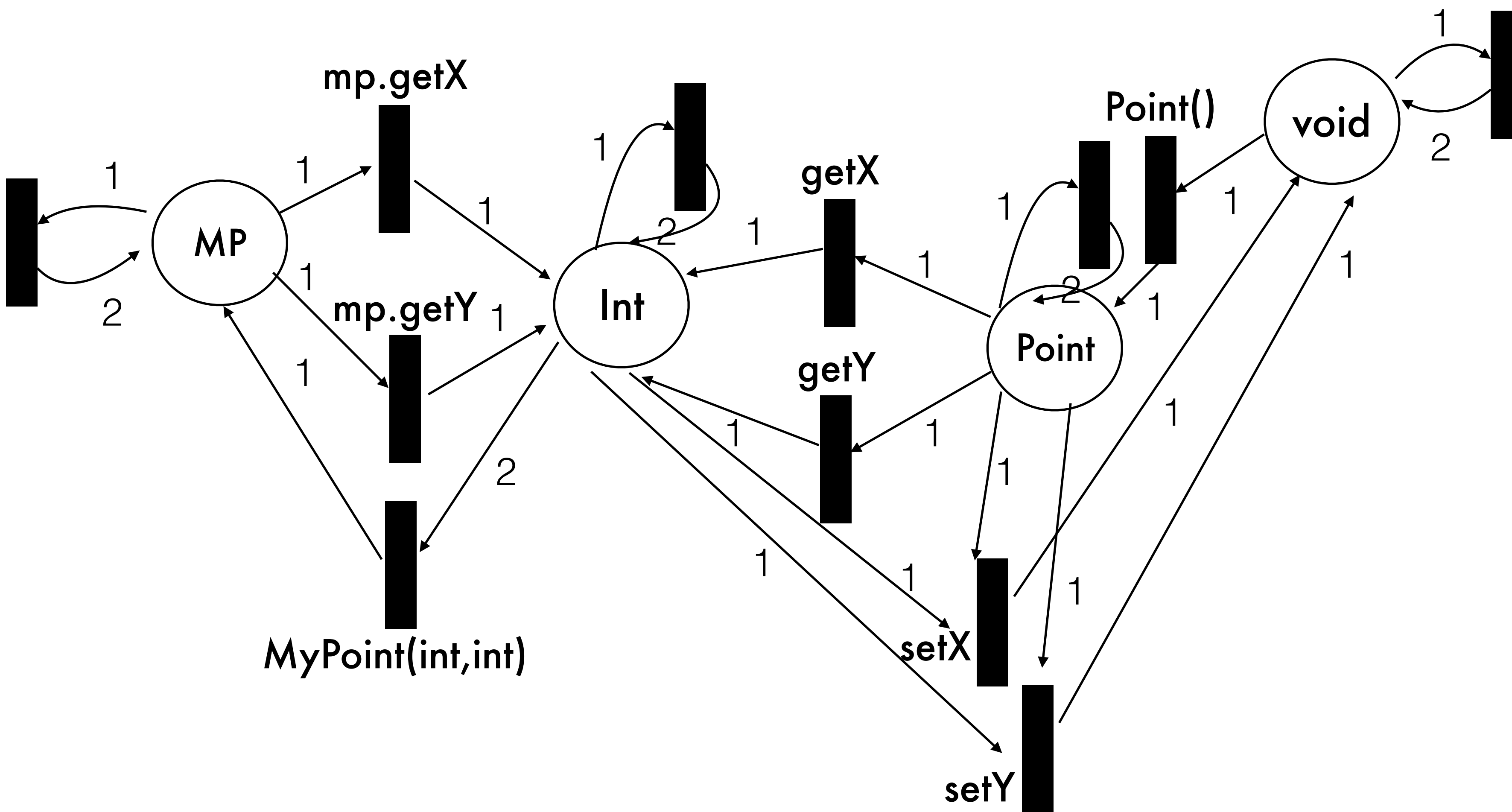


- Synthesize this function:  
`Point convert(MyPoint pt)`

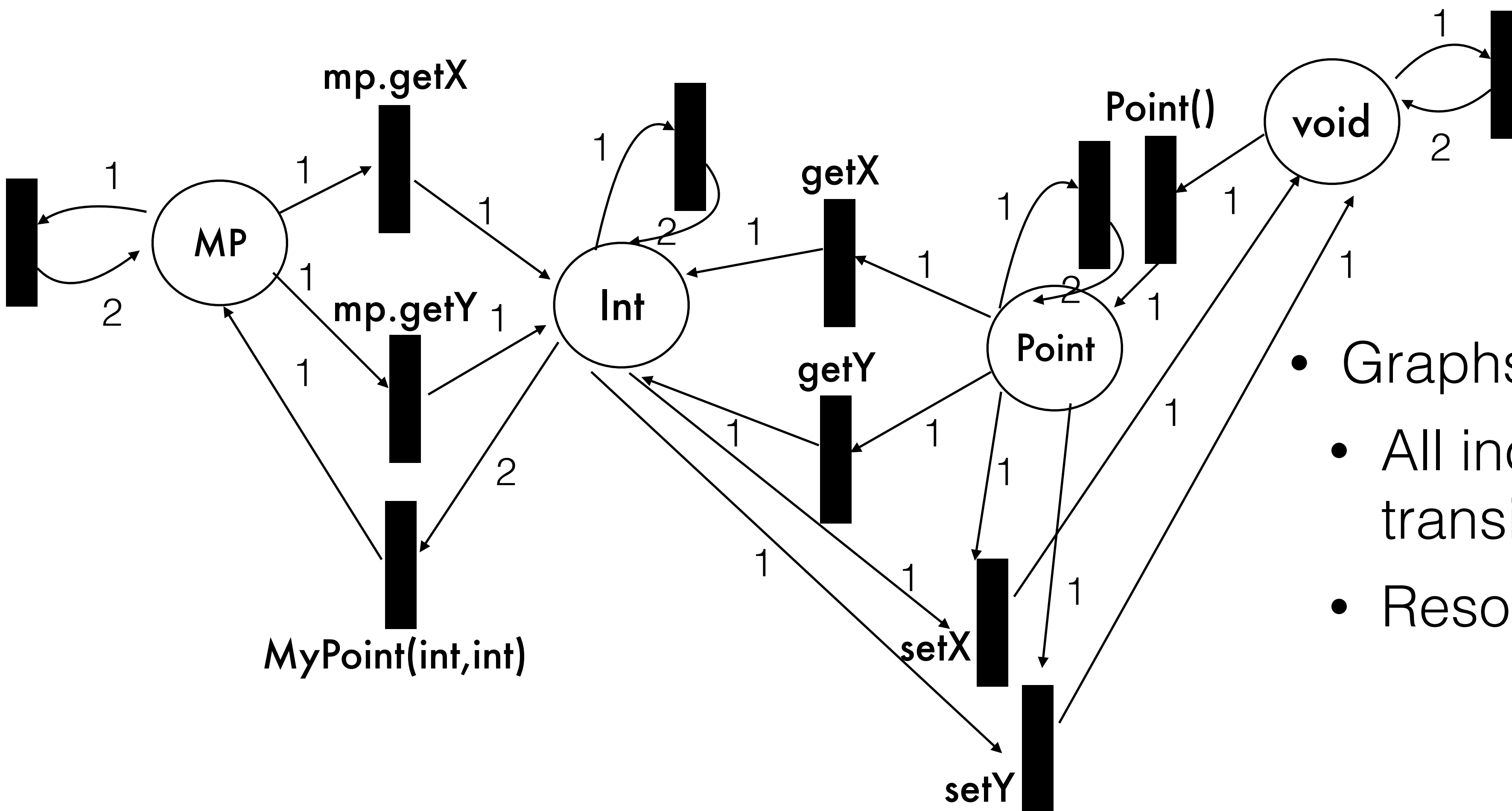
- 1) Clone-MP
- 2) `mp.getX`
- 3) `mp.getY`
- 4) `Point()`
- 5) Clone-Point
- 6) `setX`
- 7) Clone-Point
- 8) `setY`



# Why a Petri Net and not a Graph?



# Why a Petri Net and not a Graph?

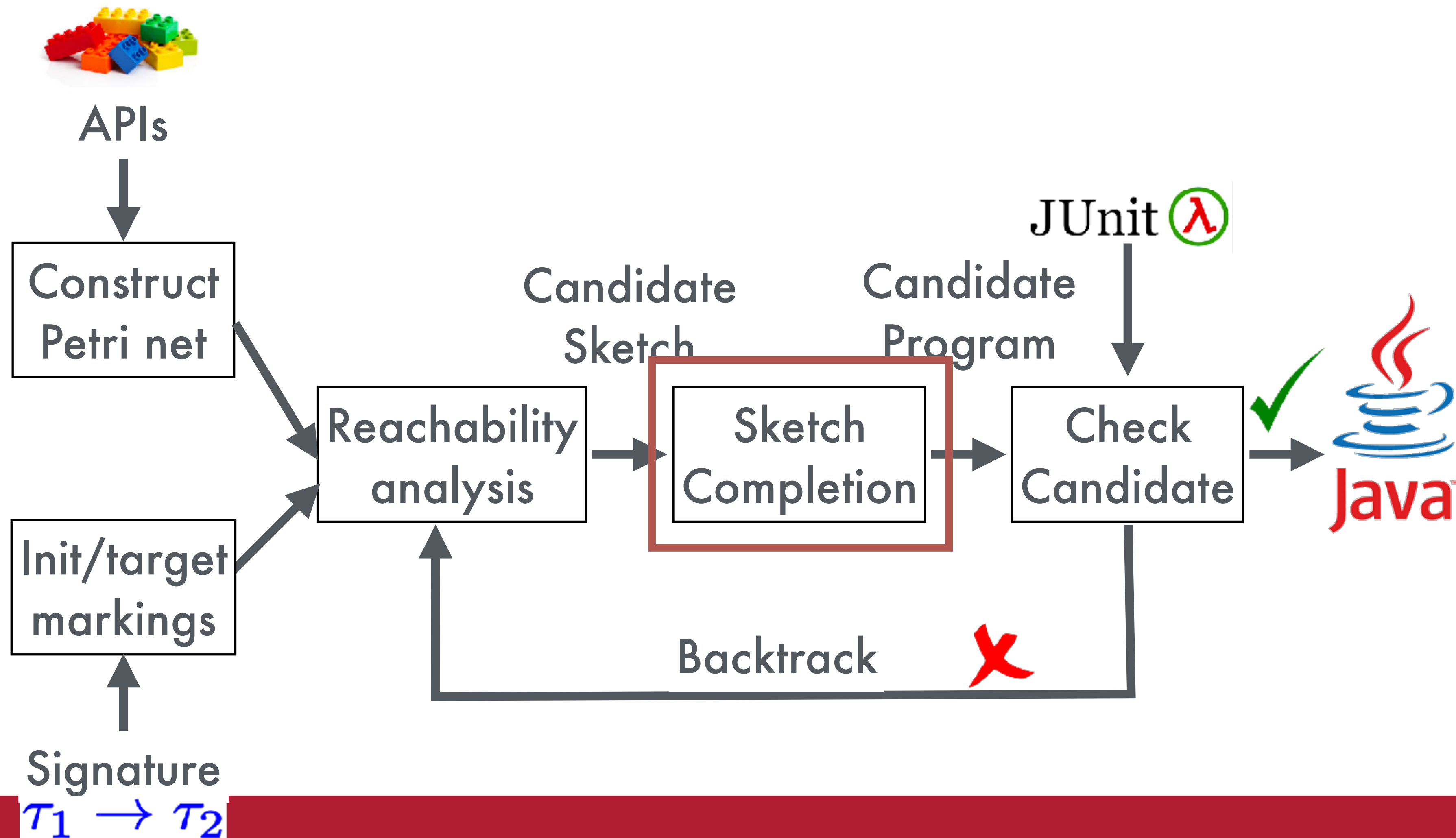


- Graphs do not support:
  - All incoming edges to a transition are part of the path
  - Resource consumption

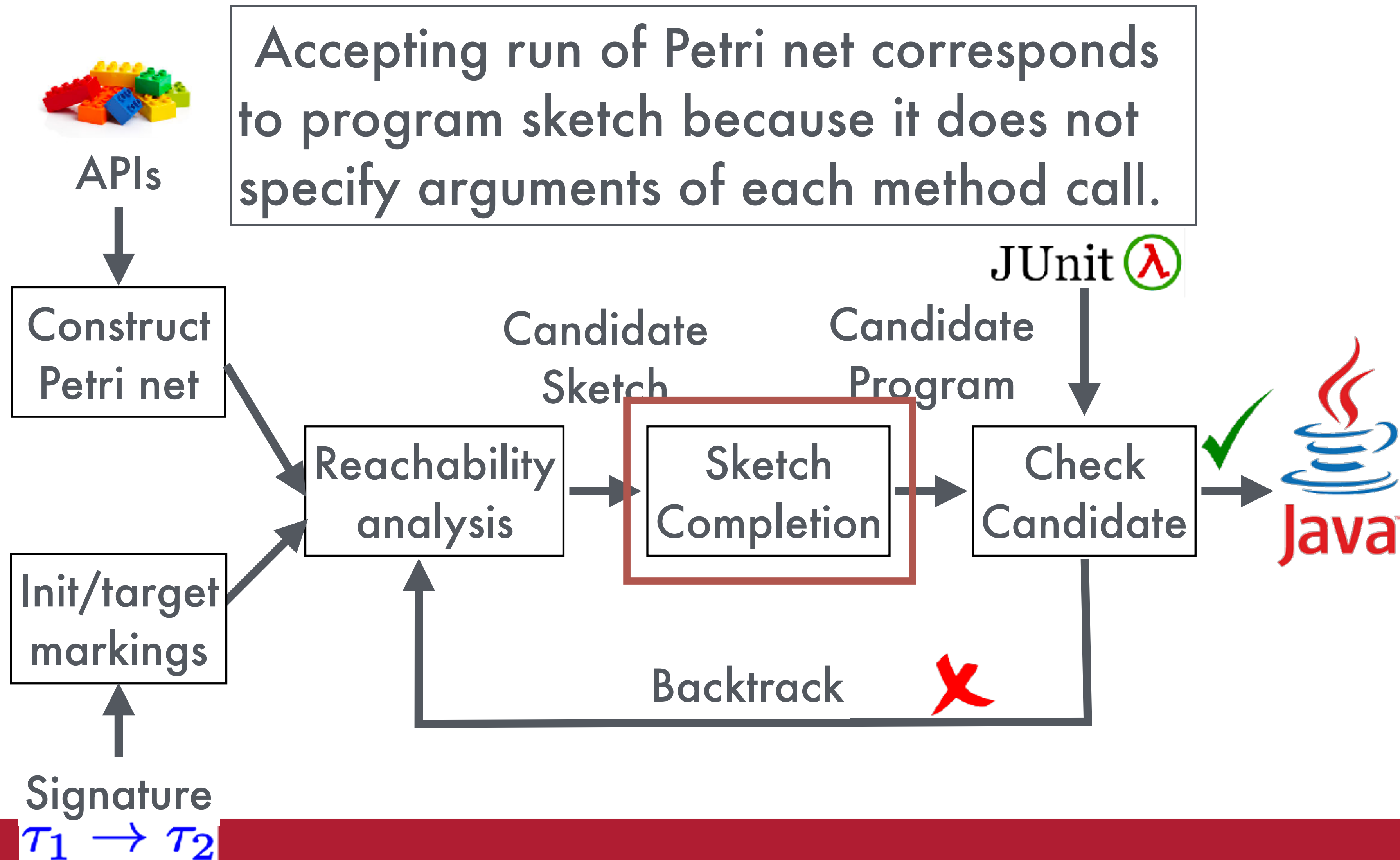




# Accepting Run as Program Sketch



# Accepting Run as Program Sketch



# Sketch Completion

- 1) Clone-MP
- 2) mp.getX
- 3) mp.getY
- 4) Point()
- 5) Clone-Point
- 6) setX
- 7) Clone-Point
- 8) setY

```
Point convert(MyPoint pt) {
```

```
}
```

- Remove the Clone transitions



# Sketch Completion

2) mp.getX  
3) mp.getY  
4) Point()  
6) setX  
8) setY

```
Point convert(MyPoint pt) {
```

```
}
```

- What is the code with holes?



# Sketch Completion

- 2) mp.getX
- 3) mp.getY
- 4) Point()
- 6) setX
- 8) setY

```
Point convert(MyPoint pt) {  
  
    int x = #1.getX();  
    int y = #2.getY();  
    Point p = new Point();  
    p.setX(#3);  
    p.setY(#4);  
    return #5;  
  
}
```

- What is the code with holes?
- Find the arguments that should be used in each hole such that the program type checks



# Sketch Completion

2) mp.getX  
3) mp.getY  
4) Point()  
6) setX  
8) setY

```
Point convert(MyPoint pt) {  
  
    int x = pt.getX();  
    int y = pt.getY();  
    Point p = new Point();  
    p.setX(#3);  
    p.setY(#4);  
    return p;  
  
}
```

- What is the code with holes?
- Find the arguments that should be used in each hole such that the program type checks



# Sketch Completion

- 2) mp.getX
- 3) mp.getY
- 4) Point()
- 6) setX
- 8) setY

```
Point convert(MyPoint pt) {  
  
    int x = pt.getX();  
    int y = pt.getY();  
    Point p = new Point();  
    p.setX(y);  
    p.setY(x);  
    return p;  
  
}
```

- What is the code with holes?
- Find the arguments that should be used in each hole such that the program type checks



# Sketch Completion

- 2) mp.getX
- 3) mp.getY
- 4) Point()
- 6) setX
- 8) setY

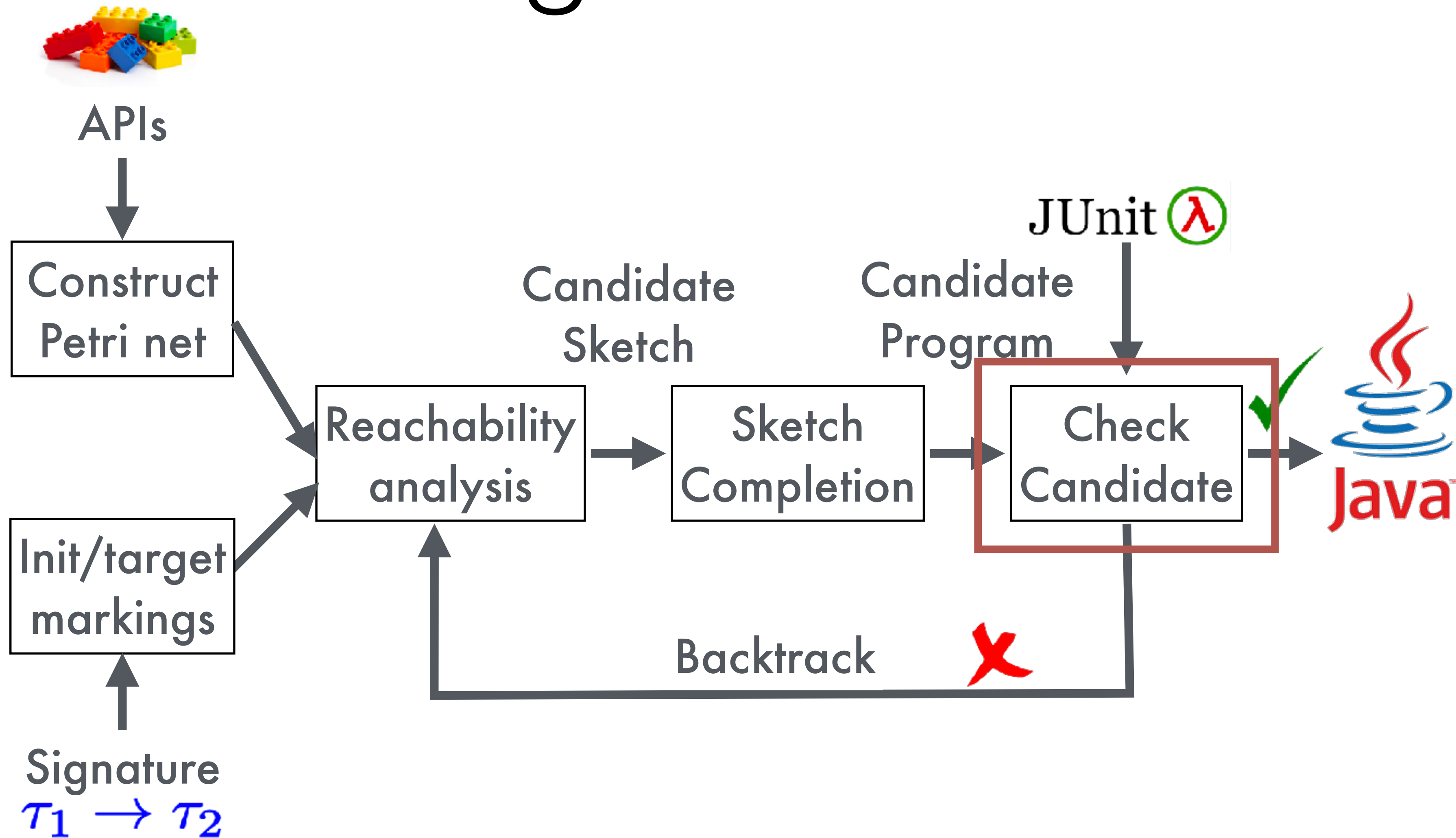
```
Point convert(MyPoint pt) {  
  
    int x = pt.getX();  
    int y = pt.getY();  
    Point p = new Point();  
    p.setX(x);  
    p.setY(y);  
    return p;  
  
}
```

- What is the code with holes?
- Find the arguments that should be used in each hole such that the program type checks





# Checking the Candidate



# Testing

```
Point convert(MyPoint pt) {
```

```
    int x = pt.getX();  
    int y = pt.getY();  
    Point p = new Point();  
    p.setX(x);  
    p.setY(y);  
    return p;
```

```
}
```

- Test case to check the conversion:



# Testing

```
Point convert(MyPoint pt) {
```

```
    int x = pt.getX();  
    int y = pt.getY();  
    Point p = new Point();  
    p.setX(x);  
    p.setY(y);  
    return p;
```

```
}
```

- Test case to check the conversion:

```
bool test() {
```

```
    MyPoint mp = new MyPoint(1,2);  
    Point p = convert(mp);  
    return (p.getX() == 1 &&  
            p.getY() == 2);
```

```
}
```



# For more information

## SyPet

Program synthesis tool for Java libraries that automatically constructs programs by composing APIs.

GITHUB

DOWNLOAD

<https://utopia-group.github.io/sypet/>



# Outline

- Introduction to Syntax-Guided Synthesis (SyGus)
- Synthesis of Java code
- Conflict-driven Synthesis



# How do Program Synthesizers Work?



**Enumerative Search**



**Stochastic Search**



**Constraint Solving**



# How do Program Synthesizers Work?



**Enumerative Search**



**Stochastic Search**



**Constraint Solving**



Can we **learn** from **past mistakes**?



# Learning from Mistakes

- Input:  $x = [1, 2, 3]$  • Output:  $y = [1, 2]$

- $\lambda x. \text{map}(x, \dots)$

This program will not satisfy the input-output specification since `map` **preserves** the size of the list!





# Learning from Mistakes

- Input:  $x = [1, 2, 3]$  • Output:  $y = [1, 2]$



This program will not satisfy the input-output specification since `map` **preserves** the size of the list!

If  $f$  **preserves** or **increases** the size of the list then  $f$  will also be infeasible!



# Learning from Mistakes

- Input:  $x = [1, 2, 3]$  • Output:  $y = [1, 2]$



This program will not satisfy the input-output specification since `map` **preserves** the size of the list!

If  $f$  **preserves** or **increases** the size of the list then  $f$  will also be infeasible!

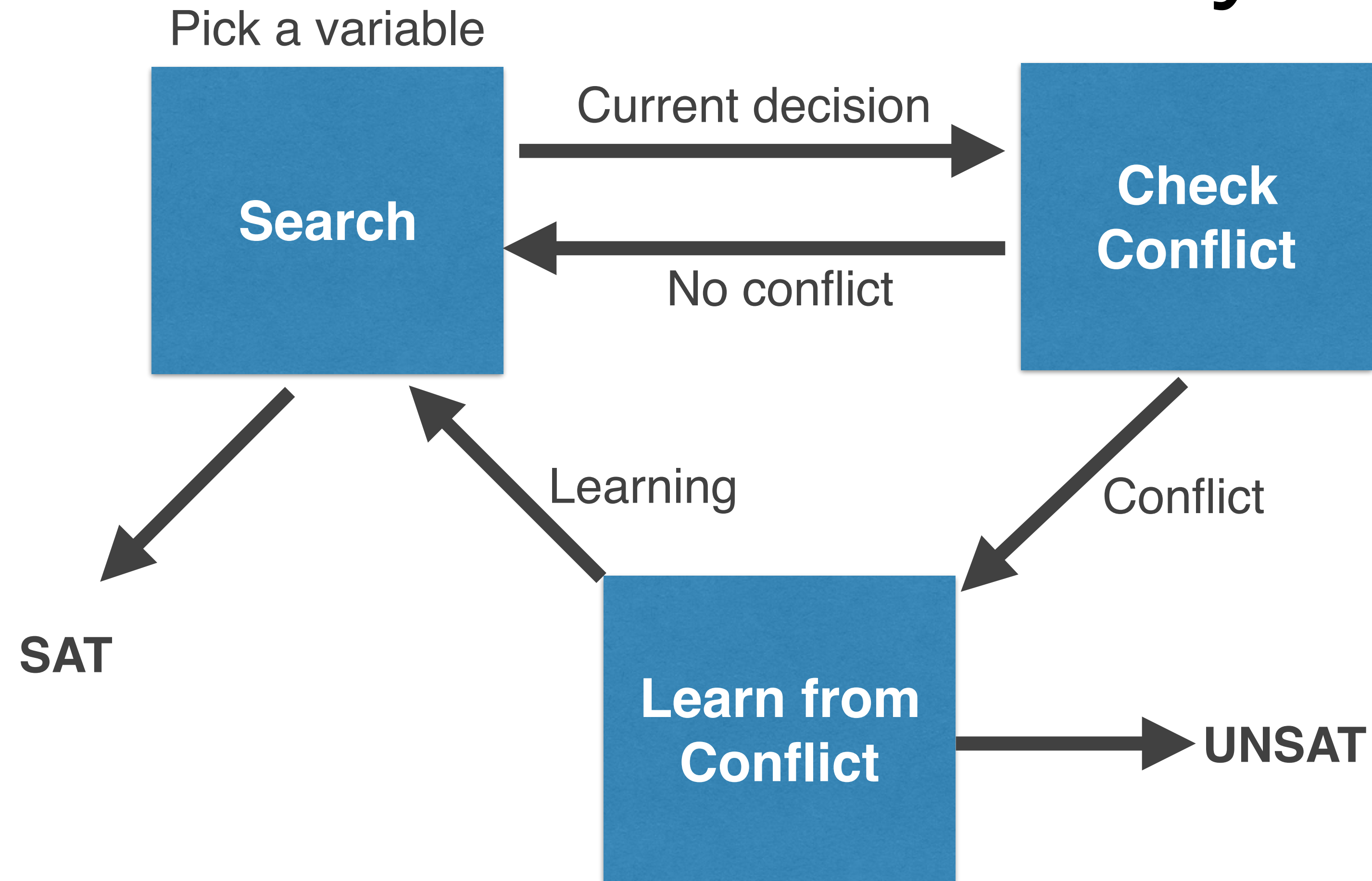


Can we **learn** from **past mistakes**?

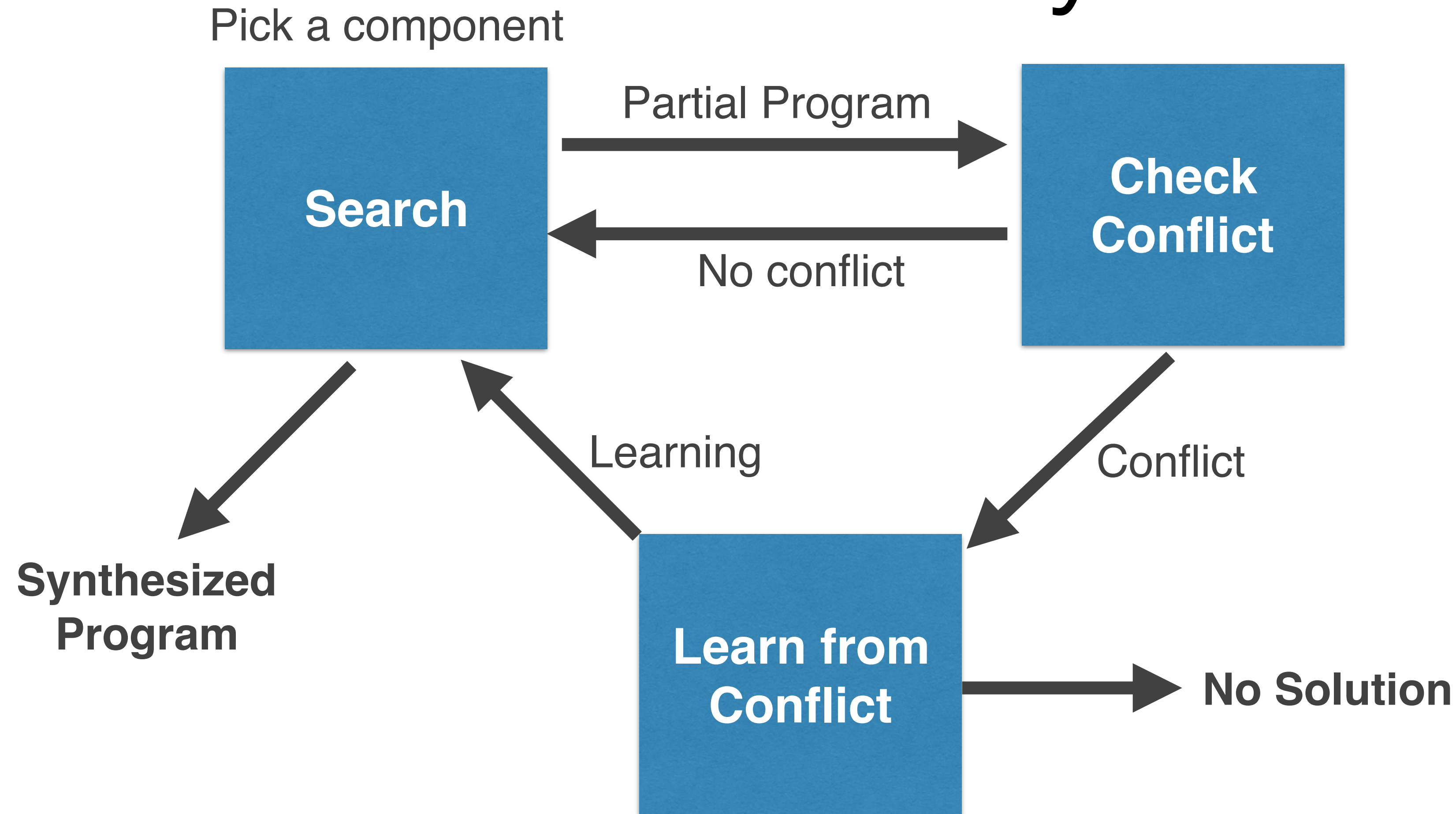
If  $\lambda x.\text{map}(x, \dots)$  is in an infeasible program then we can rule out many other erroneous programs such as  $\lambda x.\text{reverse}(x)$  or  $\lambda x.\text{sort}(x)$



# From SAT solvers to Synthesis



# Conflict-Driven Synthesis



- Program Synthesis using **Conflict-Driven Learning**. PLDI'18



# Running Example

- Compute the **scores** of the **best k** teams of a soccer league



# Running Example

- Compute the **scores** of the **best k** teams of a soccer league

- **computeKsum:: List -> Int -> Int**
- **computeKSum x1 x2 =**
- Inputs:
  - $x1 = [49, 62, 82, 54, 76]$
  - $x2 = 2$
- Output:
  - $158 (82 + 76)$



# Sample Domain Specific Language

- **computeKsum:: List -> Int -> Int**
- `computeKSum ( [49, 62, 82, 54, 76] , 2) = 158`

N->                    0 | ... | 10 | X | last(L) | head(L) |  
                         sum(L) | maximum(L) | minimum(L)

L->                    take(L,N) | filter(L,T) | sort(L) | reverse(L) | X

T->                    geqz | leqz | eqz



# Complete Programs

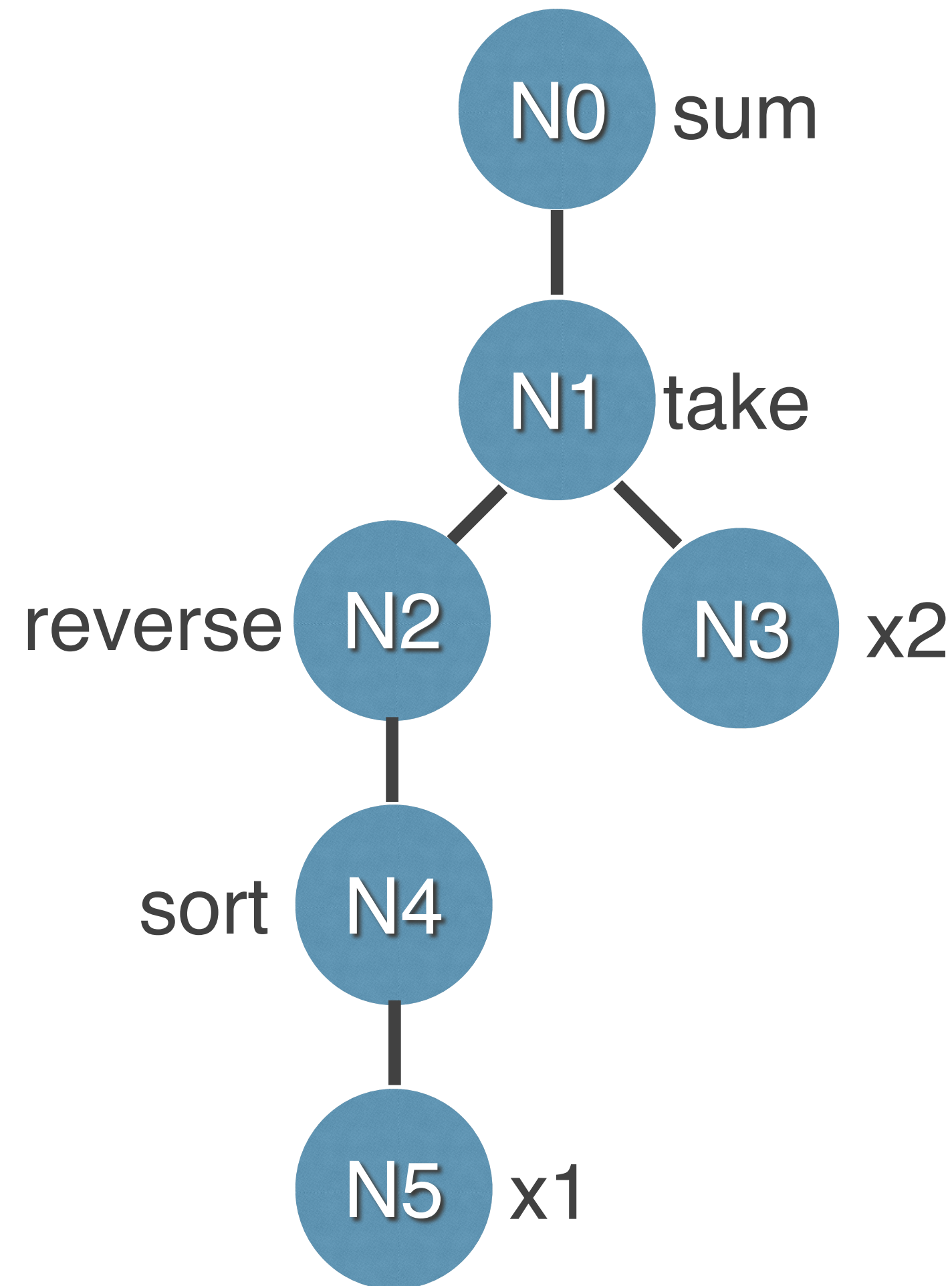
- **computeKsum:: List -> Int -> Int**
- **computeKSum x1 x2 =**
  - - sort x1 in ascending order
  - L1 <- sort x1**
  - - L2 is x1 in descending order
  - L2 <- reverse L1**
  - - Take L2's first x2 entries
  - L3 <- take L2 x2**
  - - Compute sum of all elements in L3
  - sum L3**





# Complete Programs

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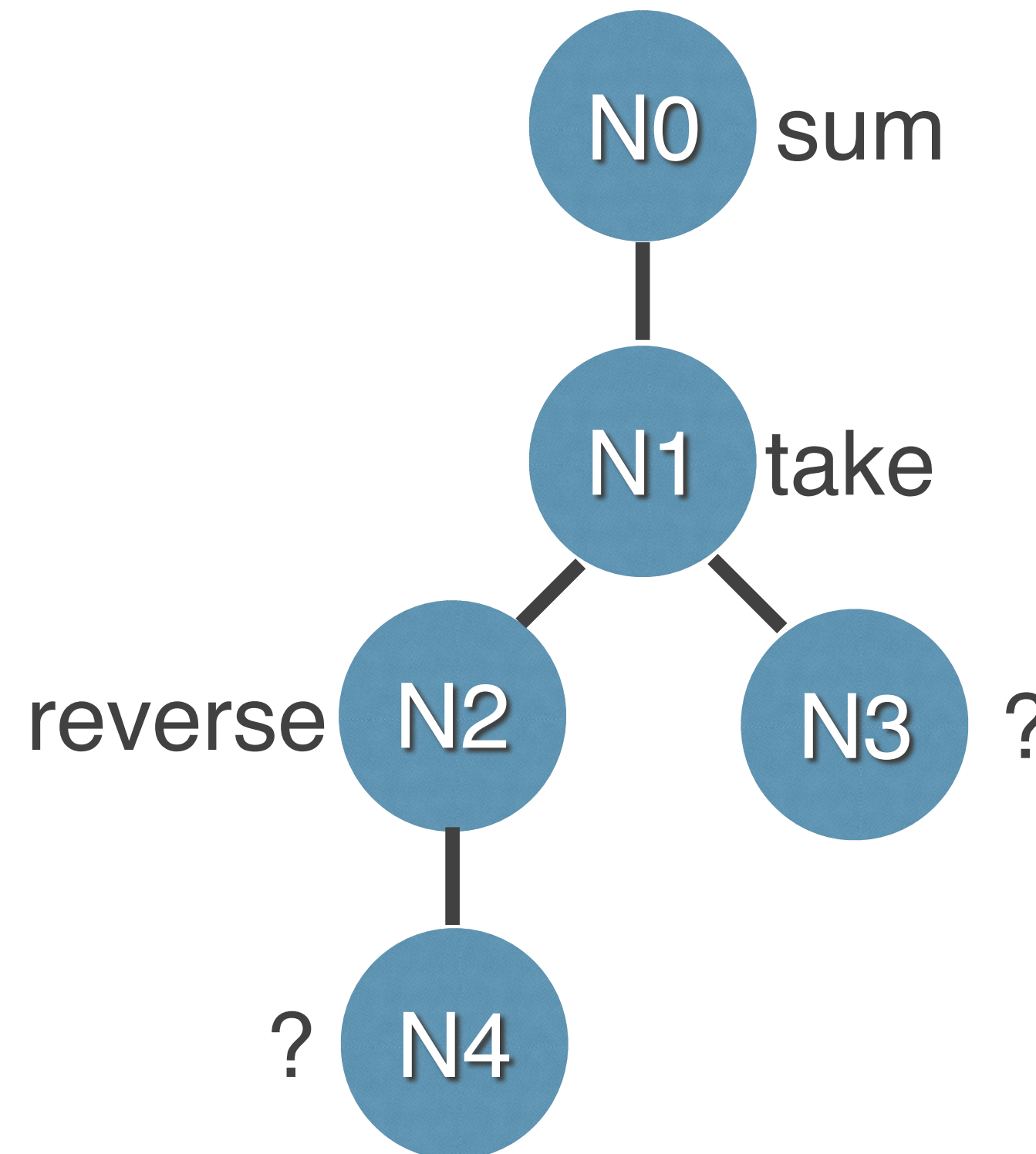


- **Program:**
  - Abstract Syntax Trees (ASTs)



# Partial Programs

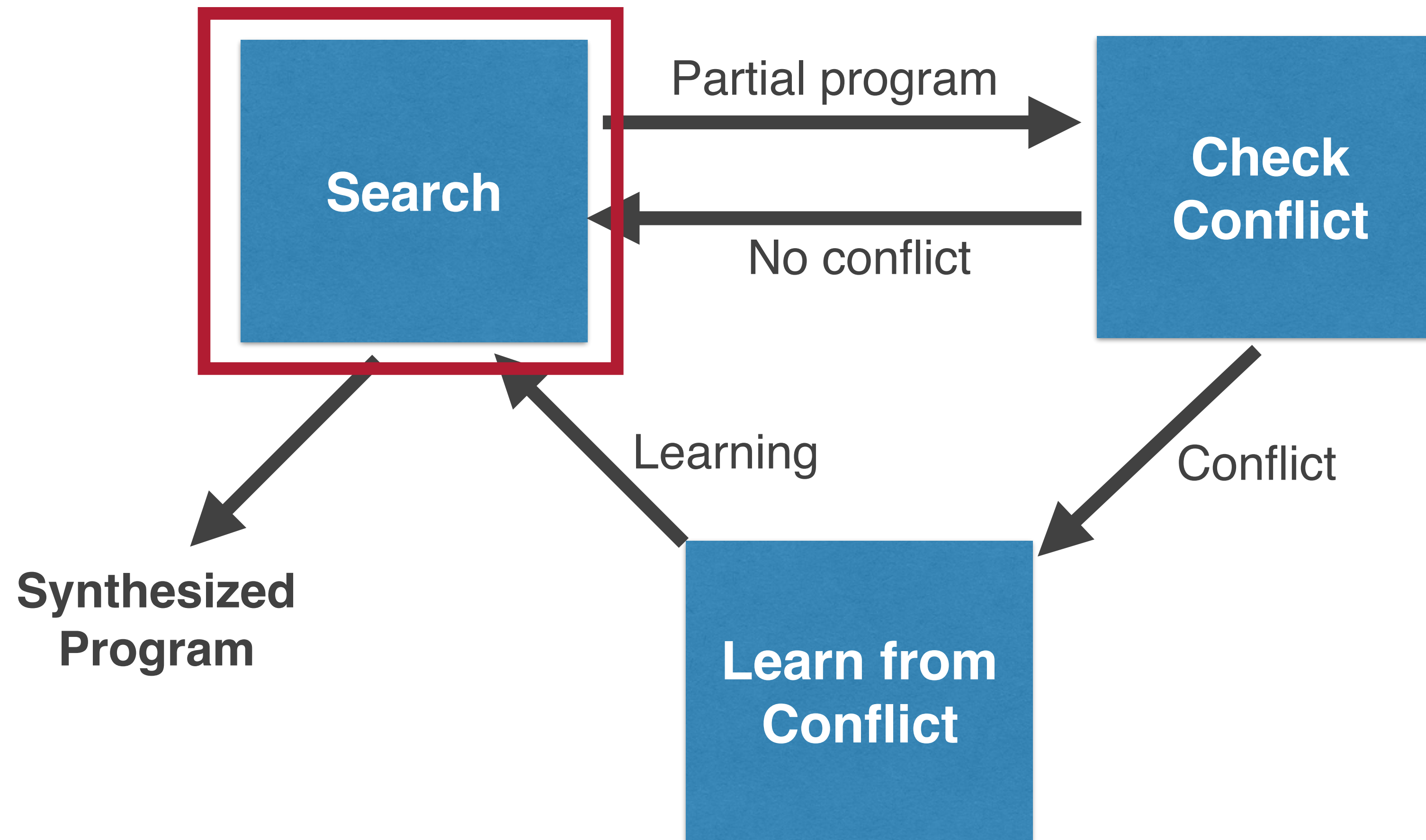
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- **Partial Program:**
  - Abstract Syntax Trees (ASTs)
  - Some nodes are unknown



# Conflict-Driven Synthesis



# Guiding the Search

- **Goal:** Choose a component to each node of the program



# Guiding the Search

- **Goal:** Choose a component to each node of the program
- Machine learning (ML):
  - N-grams
  - Neural Networks
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# Guiding the Search

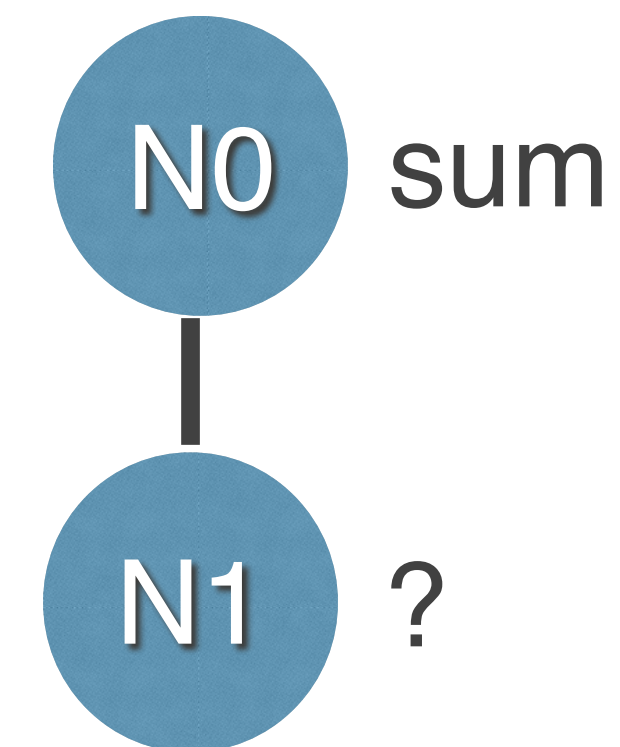
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NO ?



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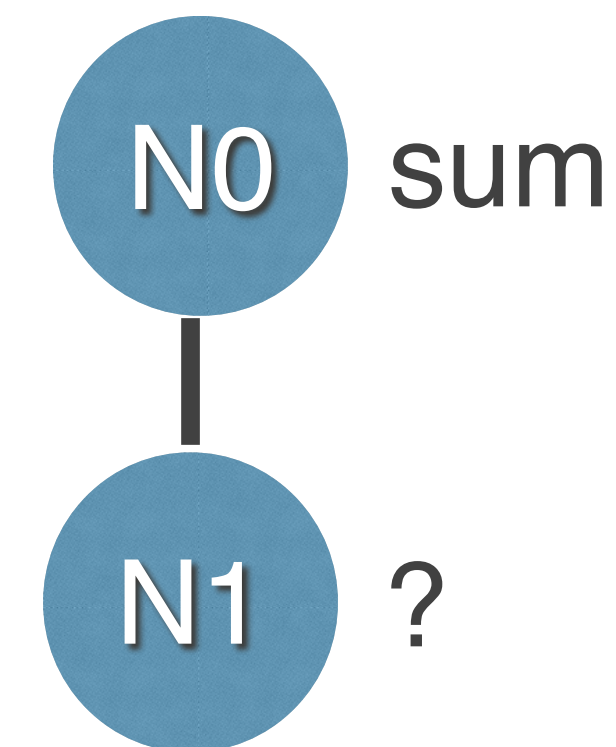


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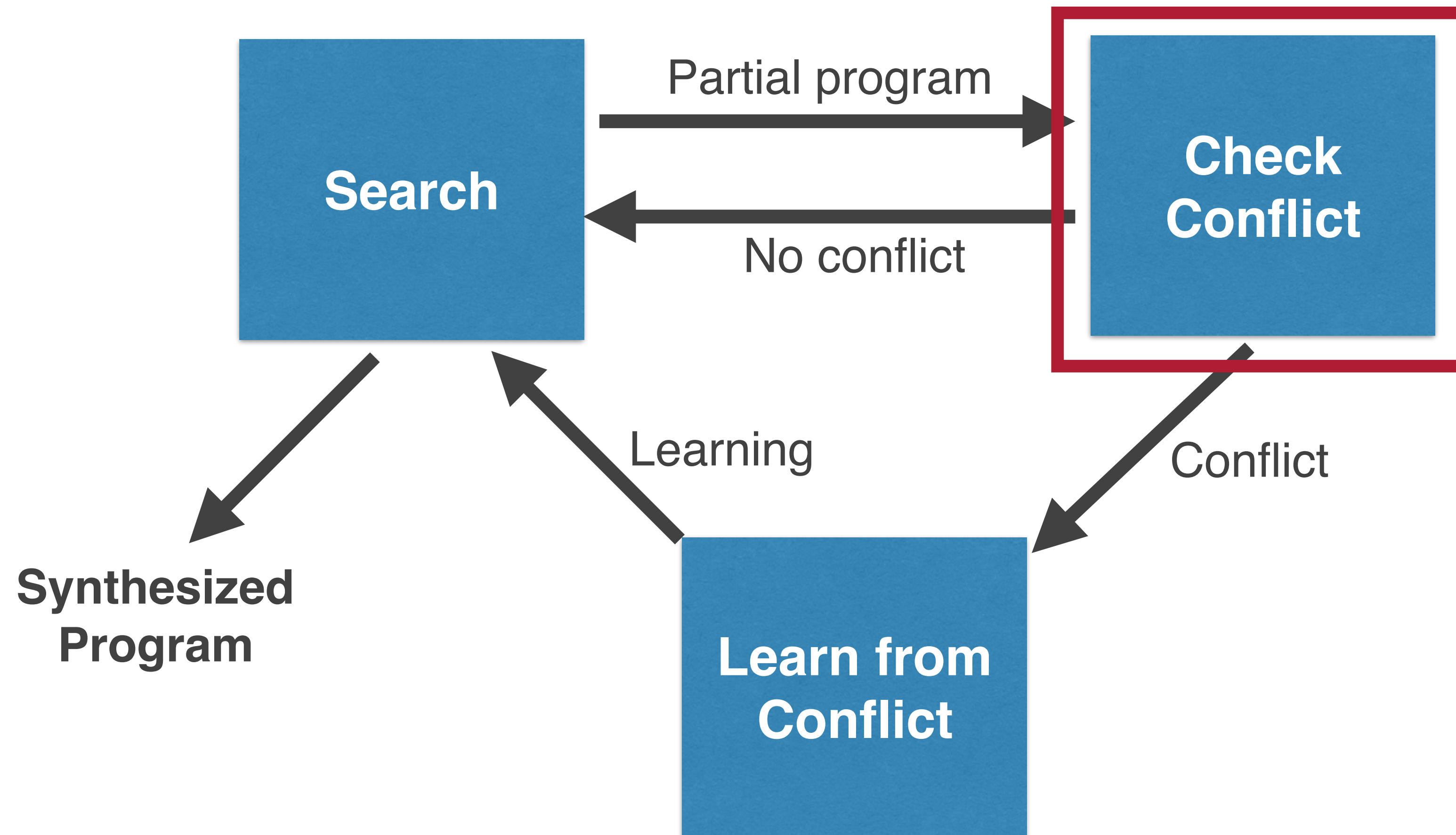


We can only check if the program is correct once we have a **complete program!**





# Conflict-Driven Synthesis



# Imprecise Specifications

- **Goal:** Prune the search space with imprecise specifications



# Imprecise Specifications

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- Precisely describing a component can be challenging



# Imprecise Specifications

- **Goal:** Prune the search space with imprecise specifications
  - Precisely describing a component can be challenging
  - Use simple properties that **over-approximate** the behavior of a component:
    - List properties: size, maximum, etc.





# Pruning the Search Space

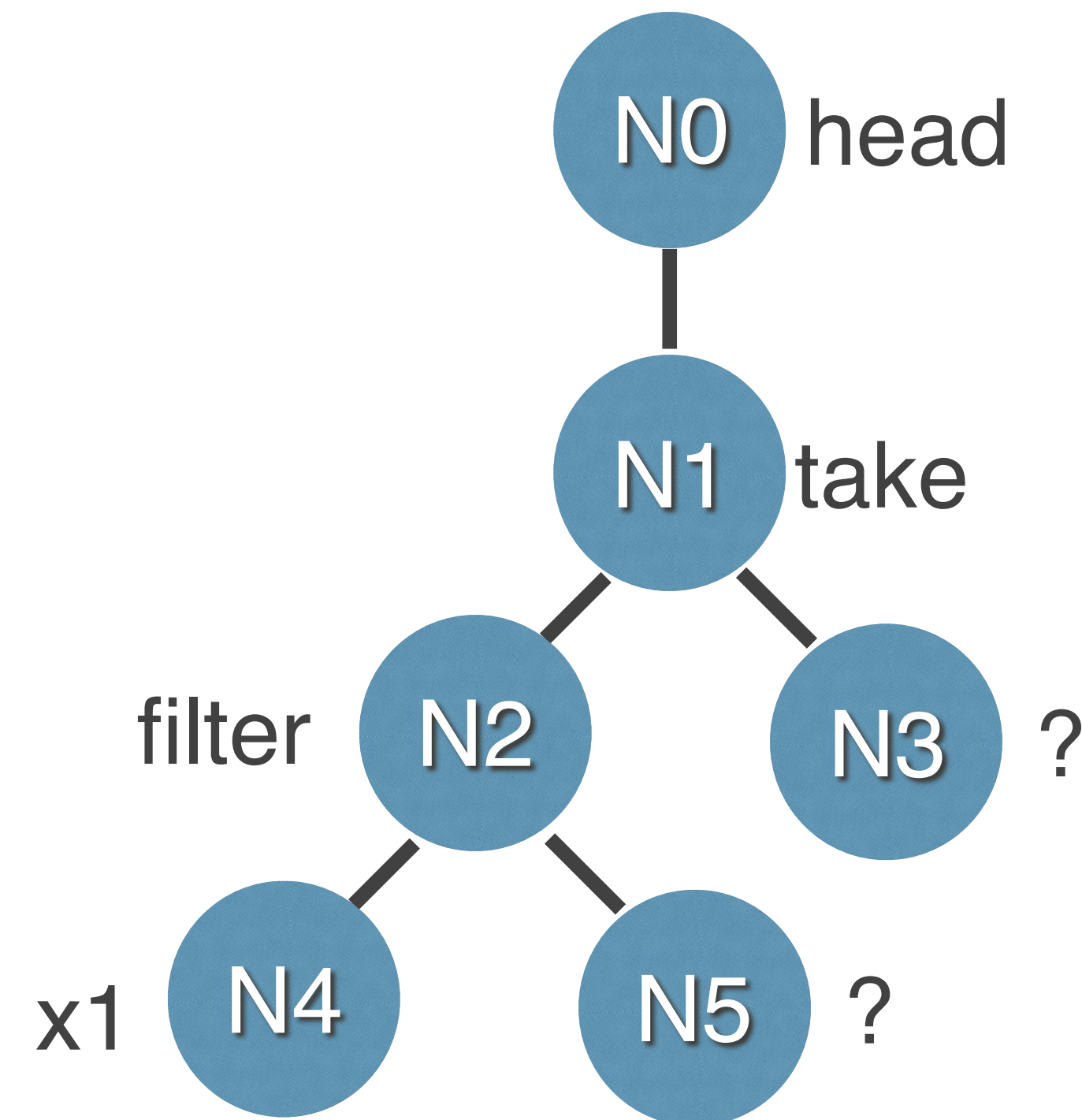
- $x1 = [49, 62, 82, 54, 76]$
- $y = 158$

N0 ->  
(head)

N1 ->  
(take)

N2 ->  
(filter)

N4 ->  
(x1)



# Pruning the Search Space

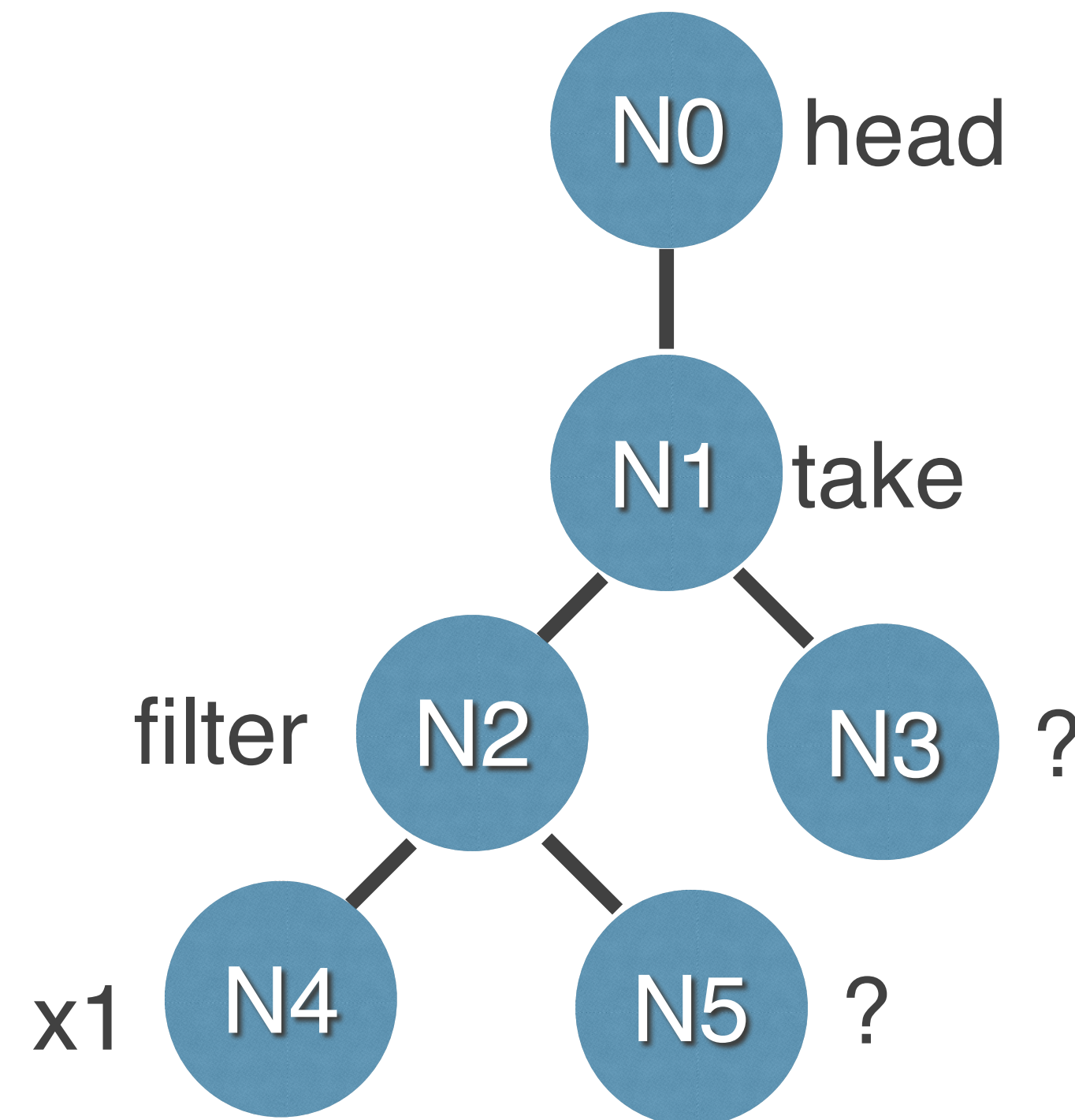
- $x1 = [49, 62, 82, 54, 76]$
- $y = 158$

N0 ->  
(head)  $y \leq n1.max$

N1 ->  
(take)  $n1.max \leq n2.max$   
 $n1.size \leq n2.size$   
 $n1.size = n3$

N2 ->  
(filter)  $n2.size \leq n4.size$   
 $n2.max \leq n4.max$

N4 ->  
(x1)  $n4 = x1$



# Pruning the Search Space

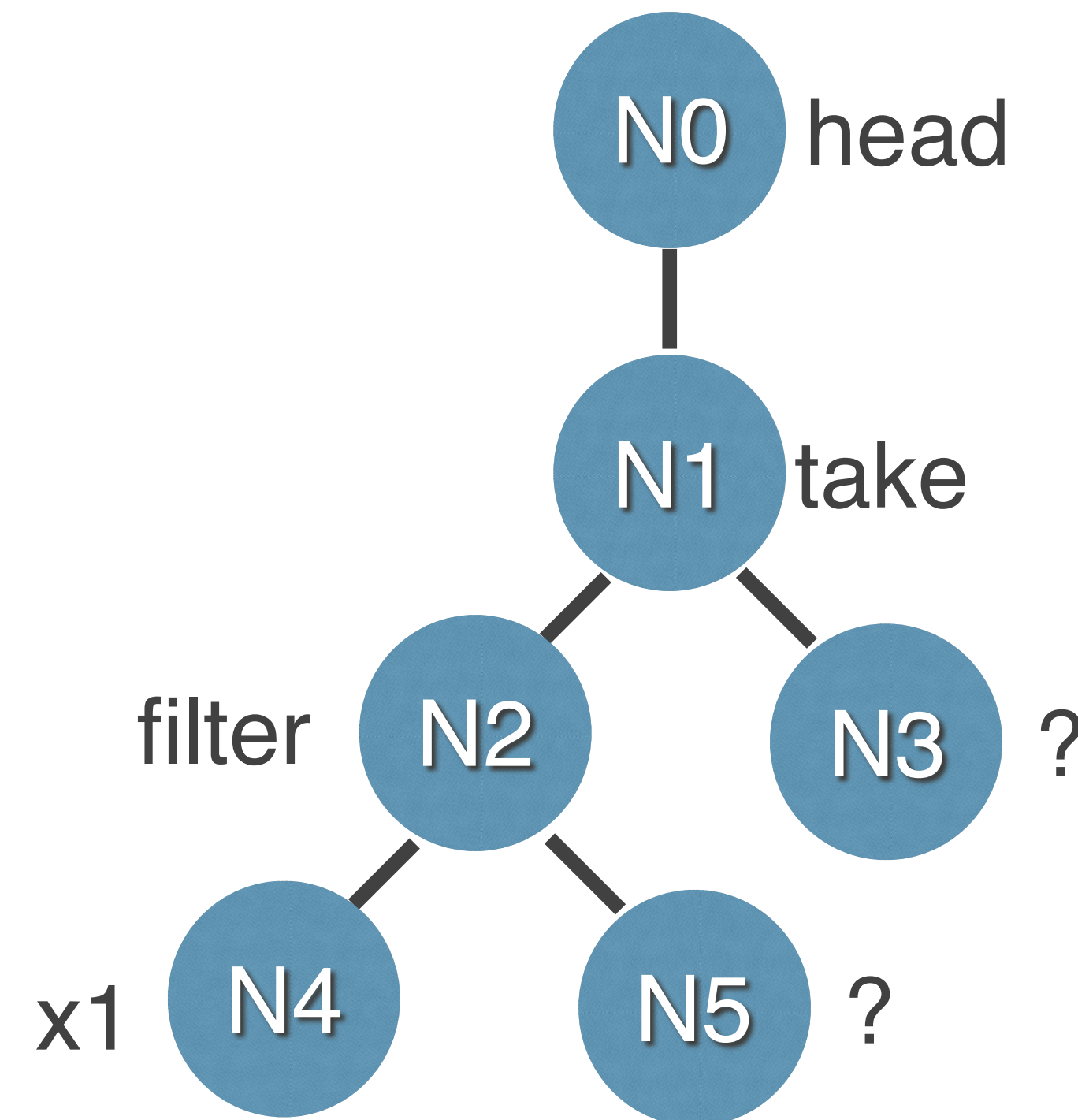
- $x1 = [49, 62, 82, 54, 76]$
- $y = 158$

N0 ->  **$y \leq n1.max$**   
(head)  **$(158 \leq 82)$**  💣

N1 ->  **$n1.max \leq n2.max$**   
(take)  $n1.size \leq n2.size$   
 $n1.size = n3$

N2 ->  $n2.size \leq n4.size$   
(filter)  **$n2.max \leq n4.max$**

N4 ->  **$n4 = x1$**   
(x1)



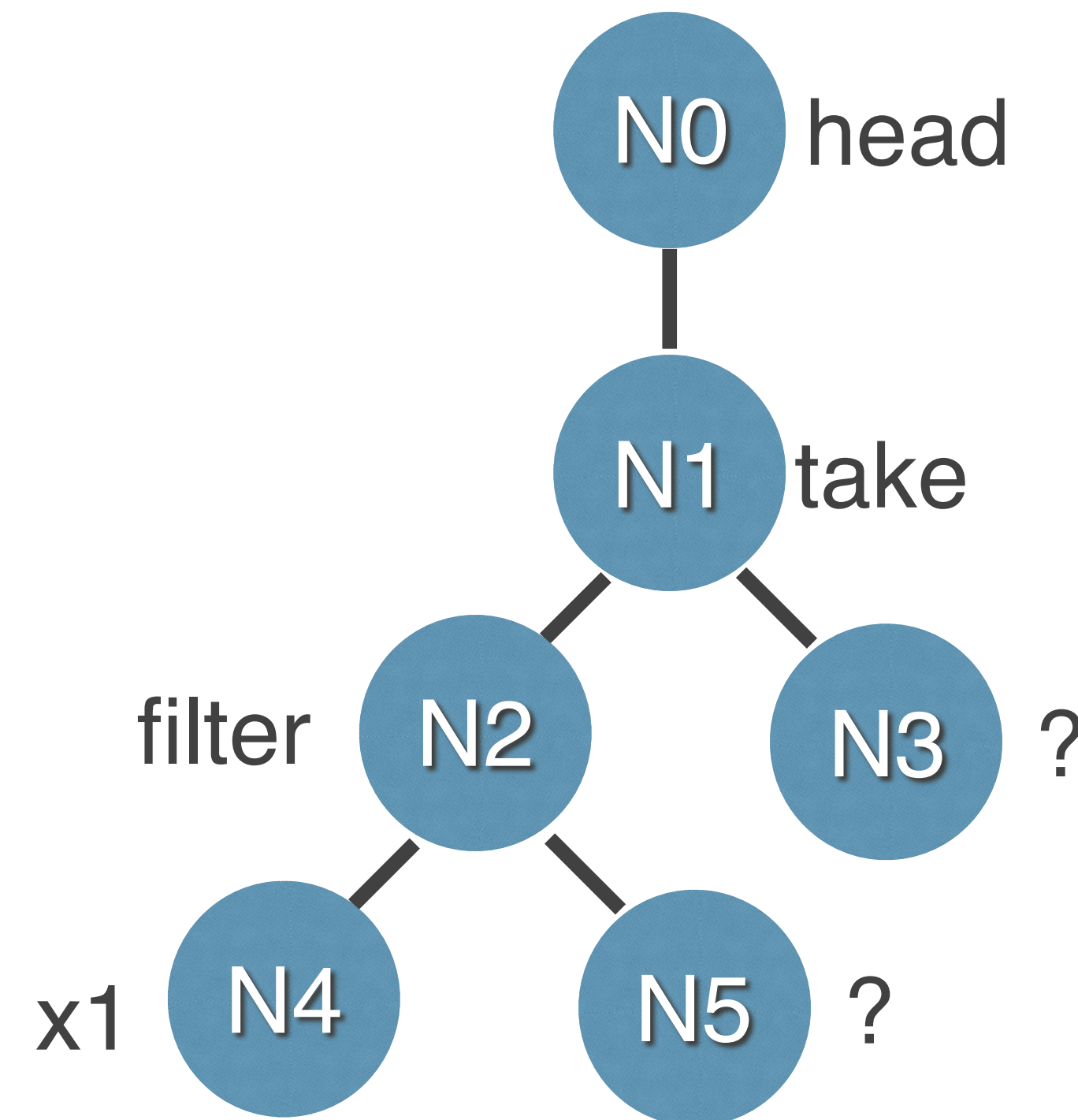


# Pruning the Search Space

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A partial program represents **many** complete programs!



# Pruning the Search Space

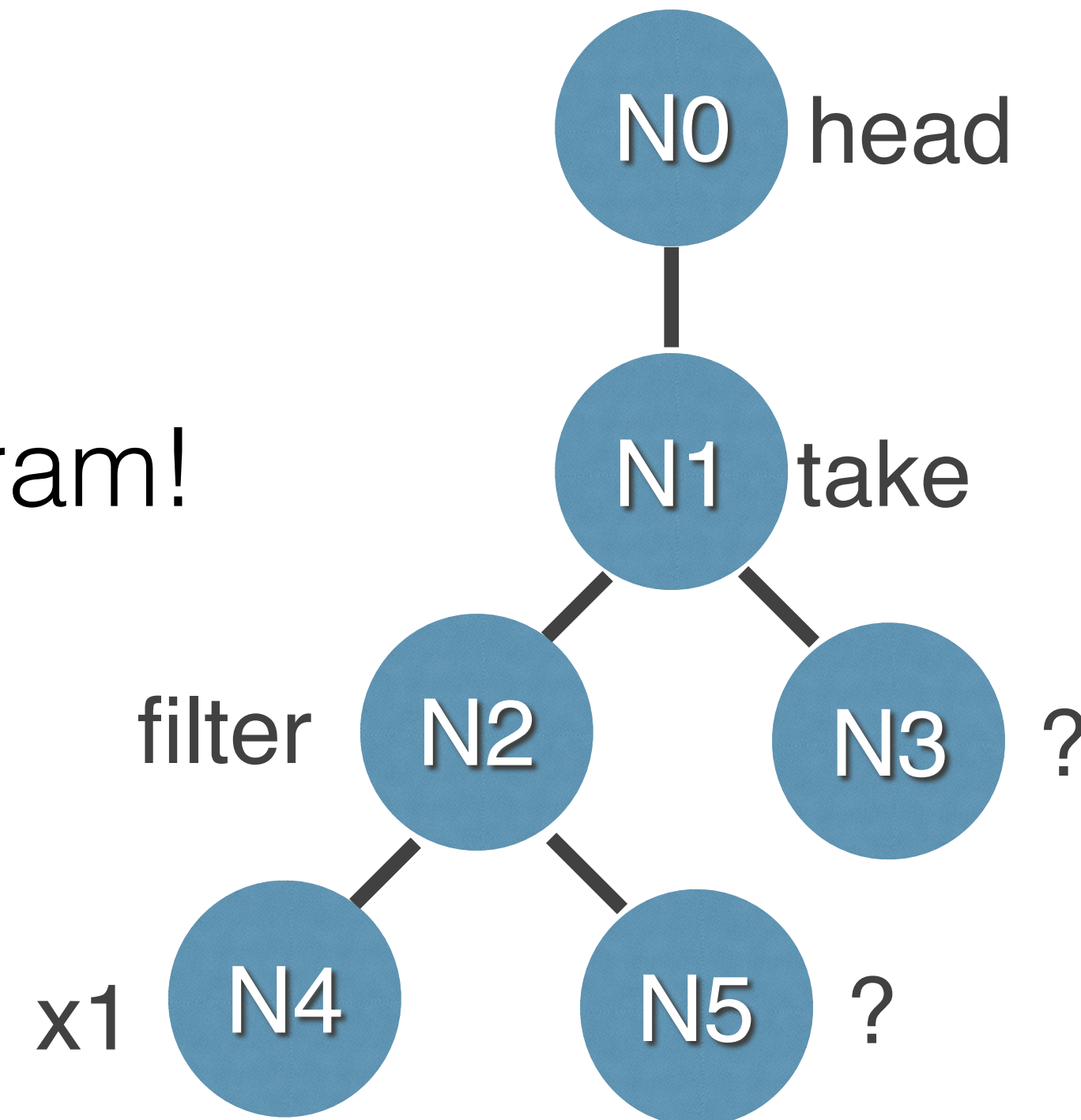
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We are only pruning **one** partial program!



# Pruning the Search Space

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- $y = 158$



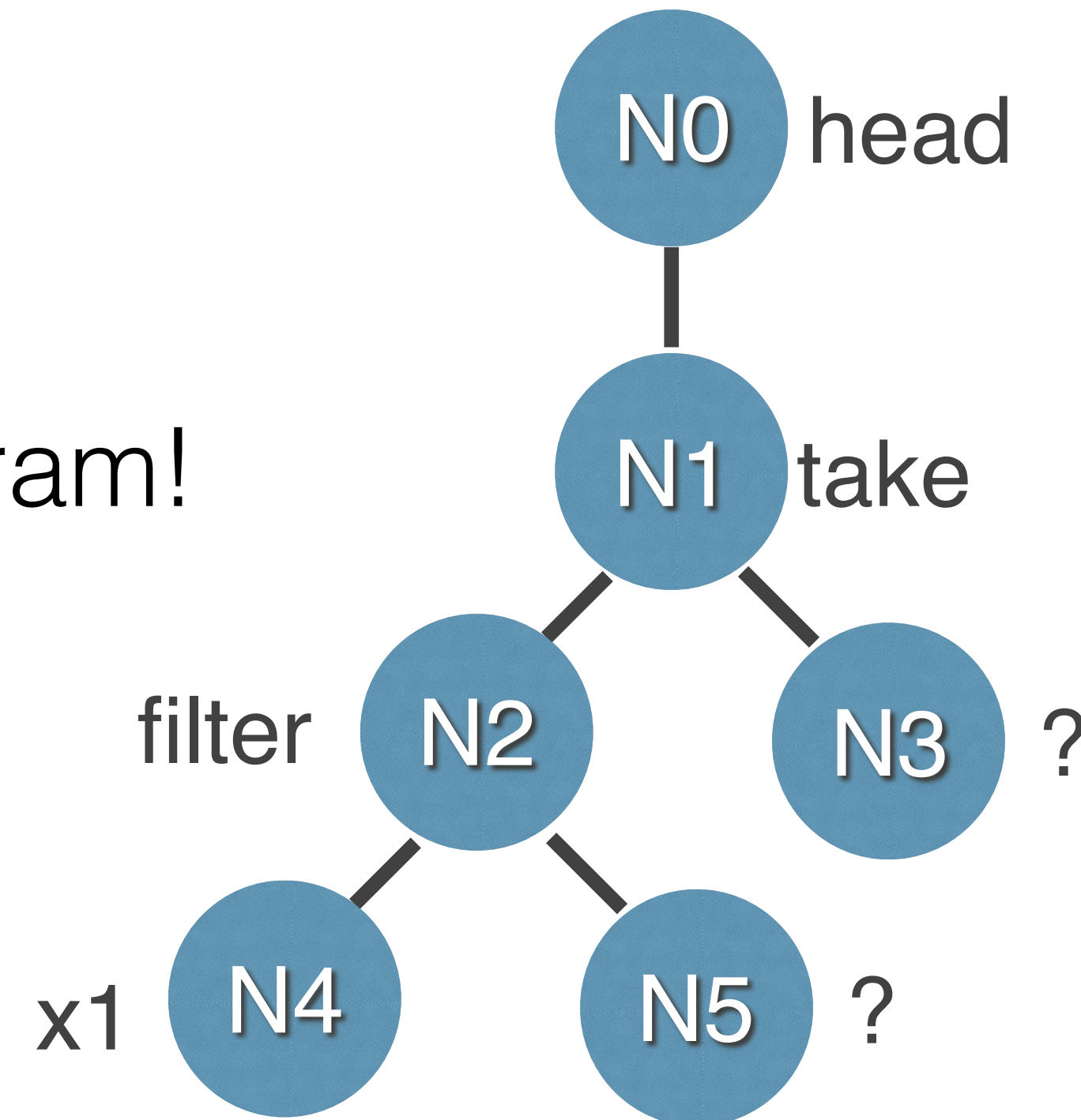
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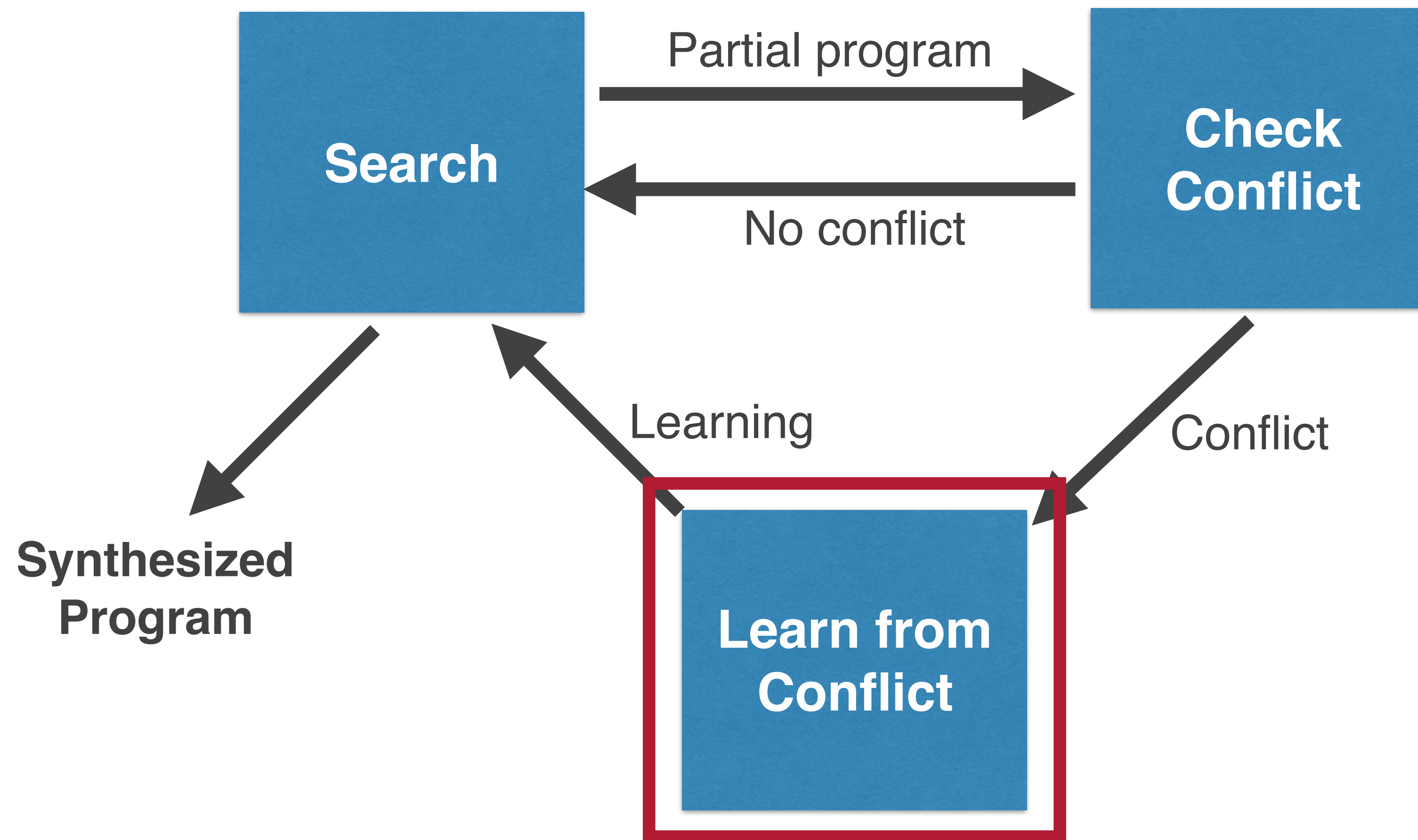
We are only pruning **one** partial program!



Can we prune **equivalent infeasible** partial programs?



# Conflict-Driven Synthesis



# Learning from Mistakes

- **Goal:** : Learn equivalent infeasible partial programs

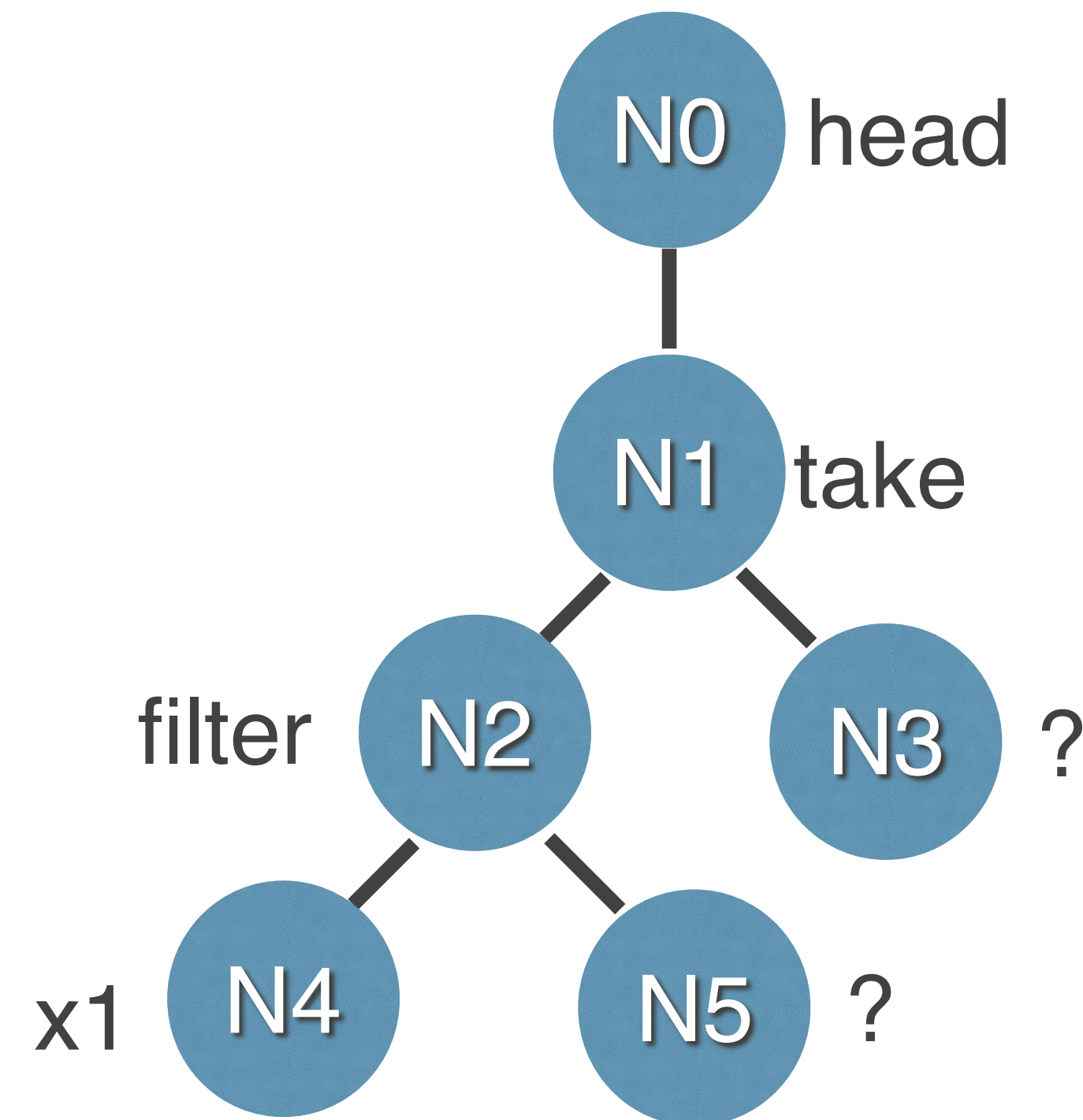


# Learning from Mistakes

- **Goal:** : Learn equivalent infeasible partial programs

## Equivalent modulo conflict:

- Two components  $X$  and  $X'$  are **equivalent modulo conflict** at node  $N$  if replacing  $X$  with  $X'$  leads to the same conflict



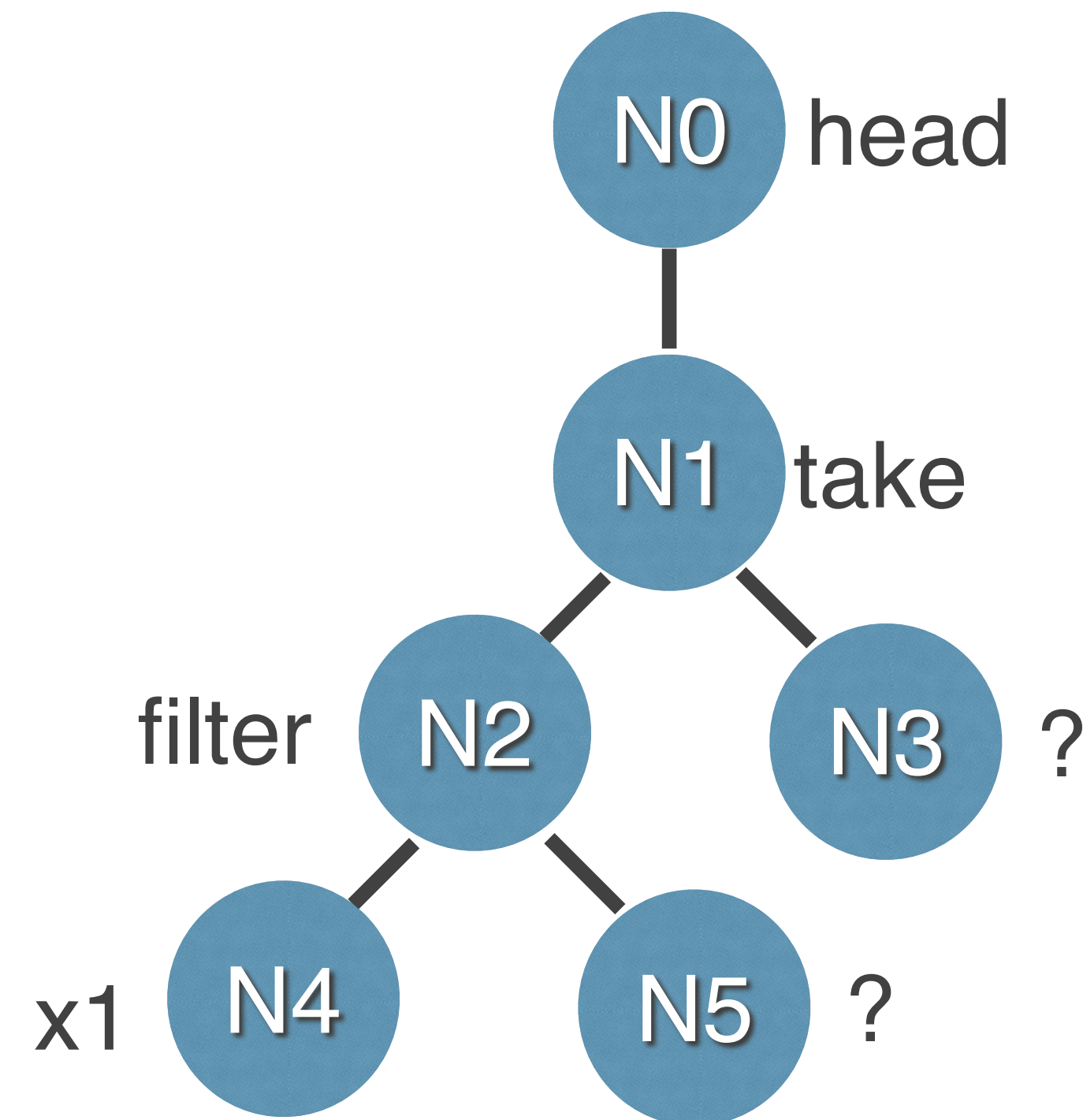
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**How to detect equivalent modulo conflict components?**



# Learning from Mistakes

**How to detect equivalent modulo conflict components?**

N0 ->  
(head)

$$y \leq n1.max$$

N1 ->  
(take)

$$n1.max \leq n2.max$$

$$n1.size < n2.size$$
$$n1.size = n3$$

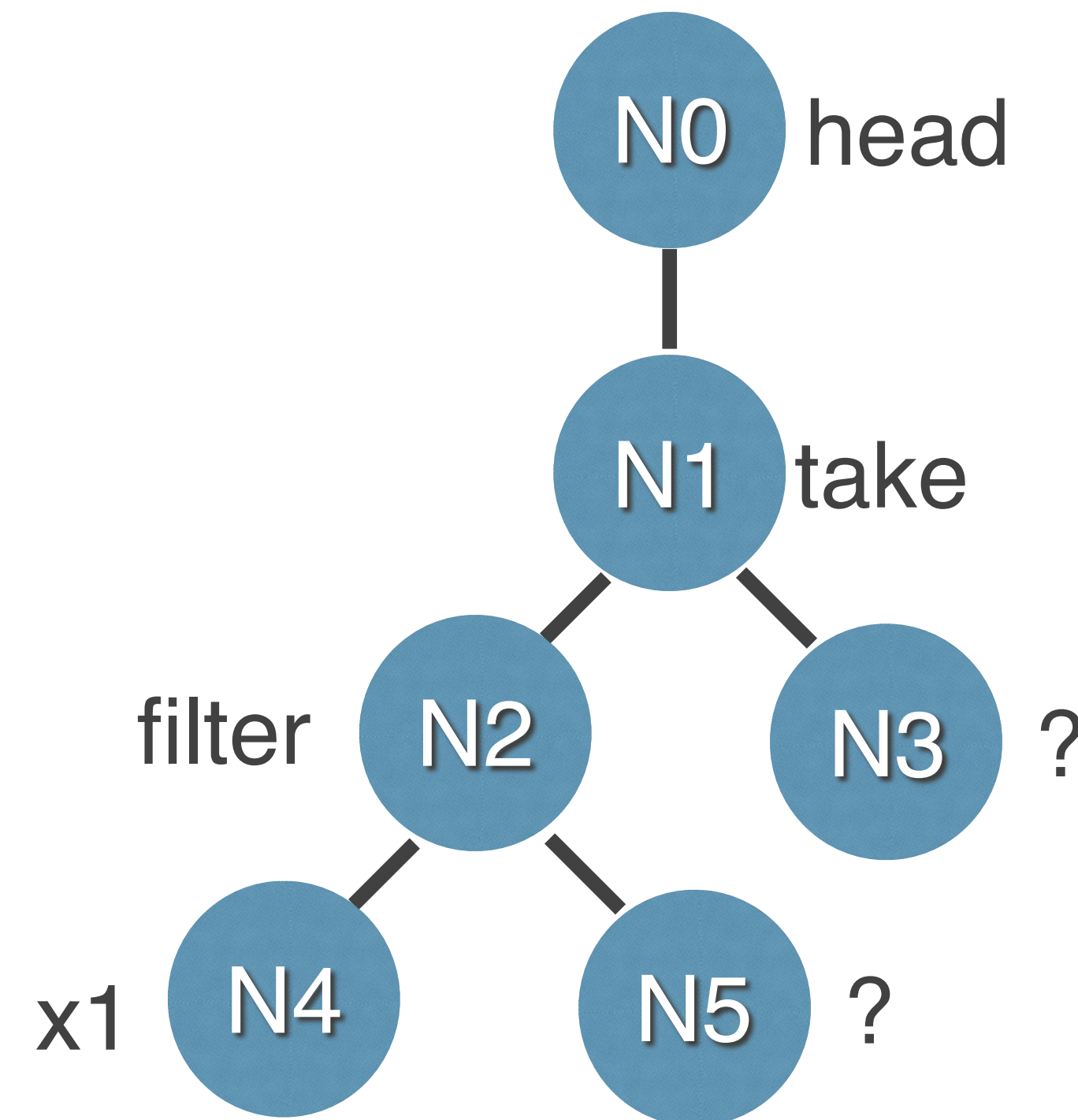
N2 ->  
(filter)

$$n2.size < n4.size$$

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# Learning from Mistakes

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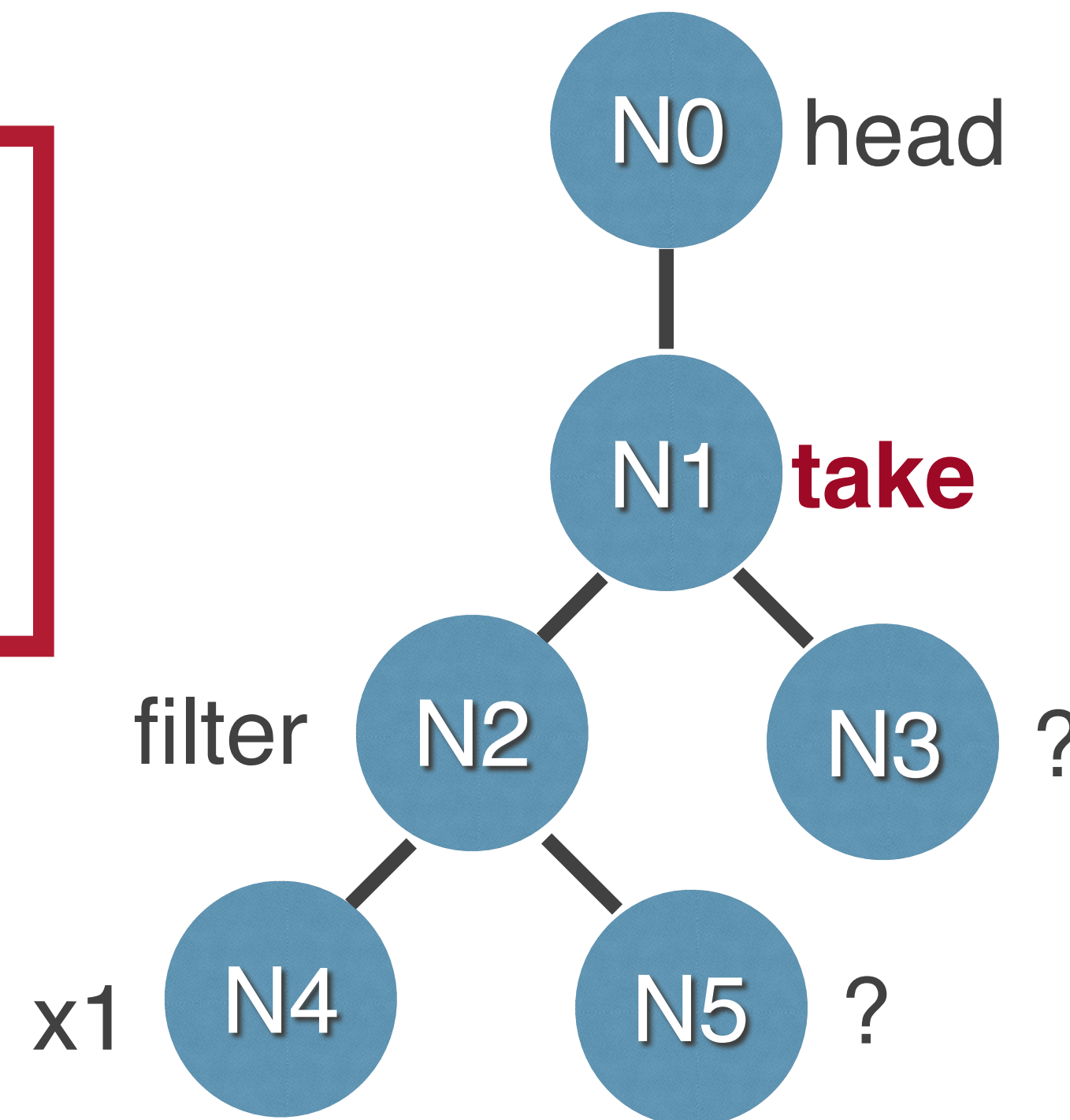
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**$n2.max \leq n4.max$**

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(x1)

**$n4 = x1$**



# Learning from Mistakes

How to detect equivalent modulo conflict components?

**Take**  $n1.max \leq n2.max$

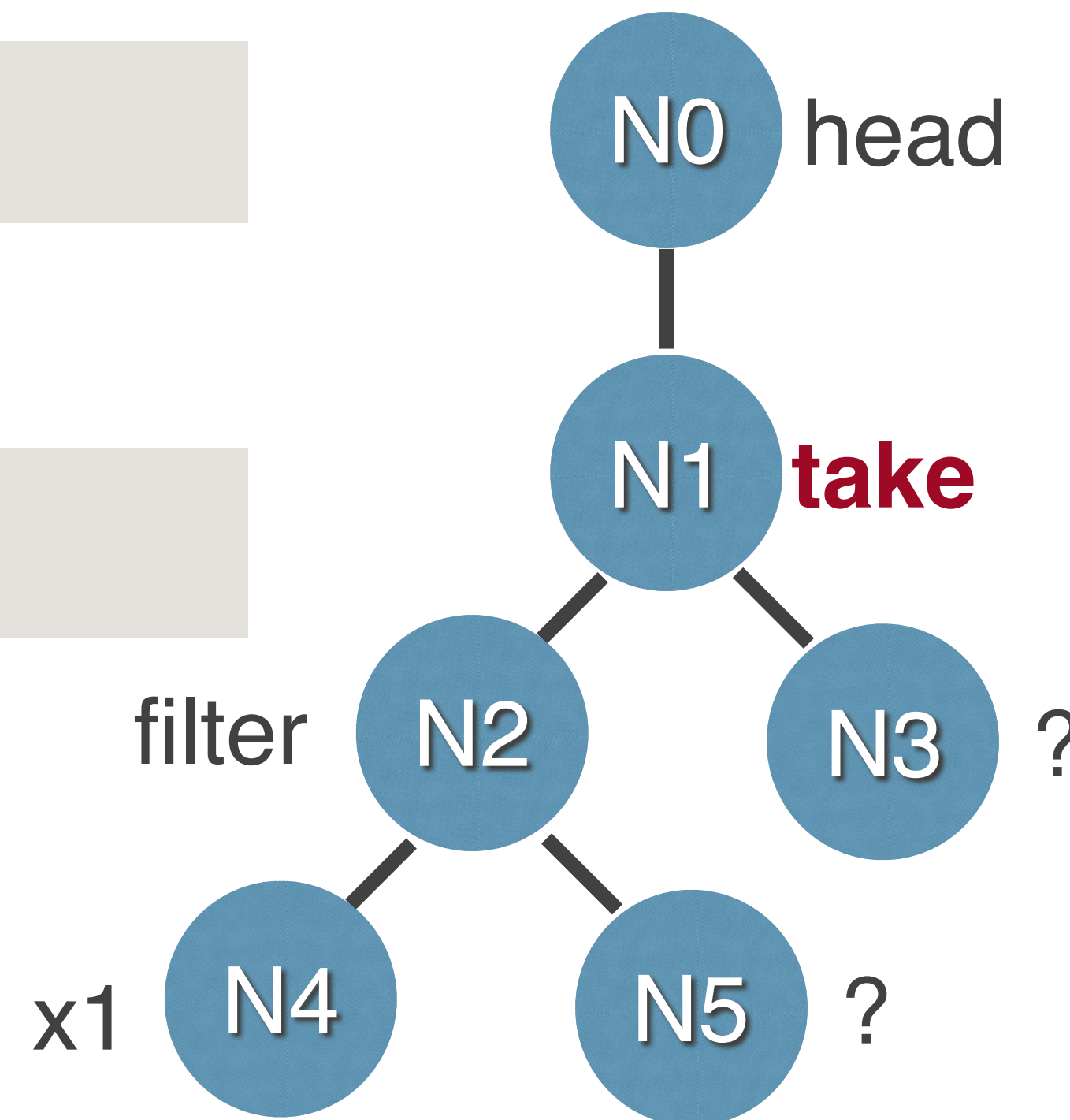
Sort  $n1.max = n2.max$

Reverse  $n1.max = n2.max$

Filter  $n1.max \leq n2.max$

If the specification of  $X'$  implies  $X$   
then  $X \equiv X'$ :

- $take \equiv sort \equiv reverse \equiv filter$



# Learning from Mistakes

## How to detect equivalent modulo conflict components?

Take  $n1.max \leq n2.max$

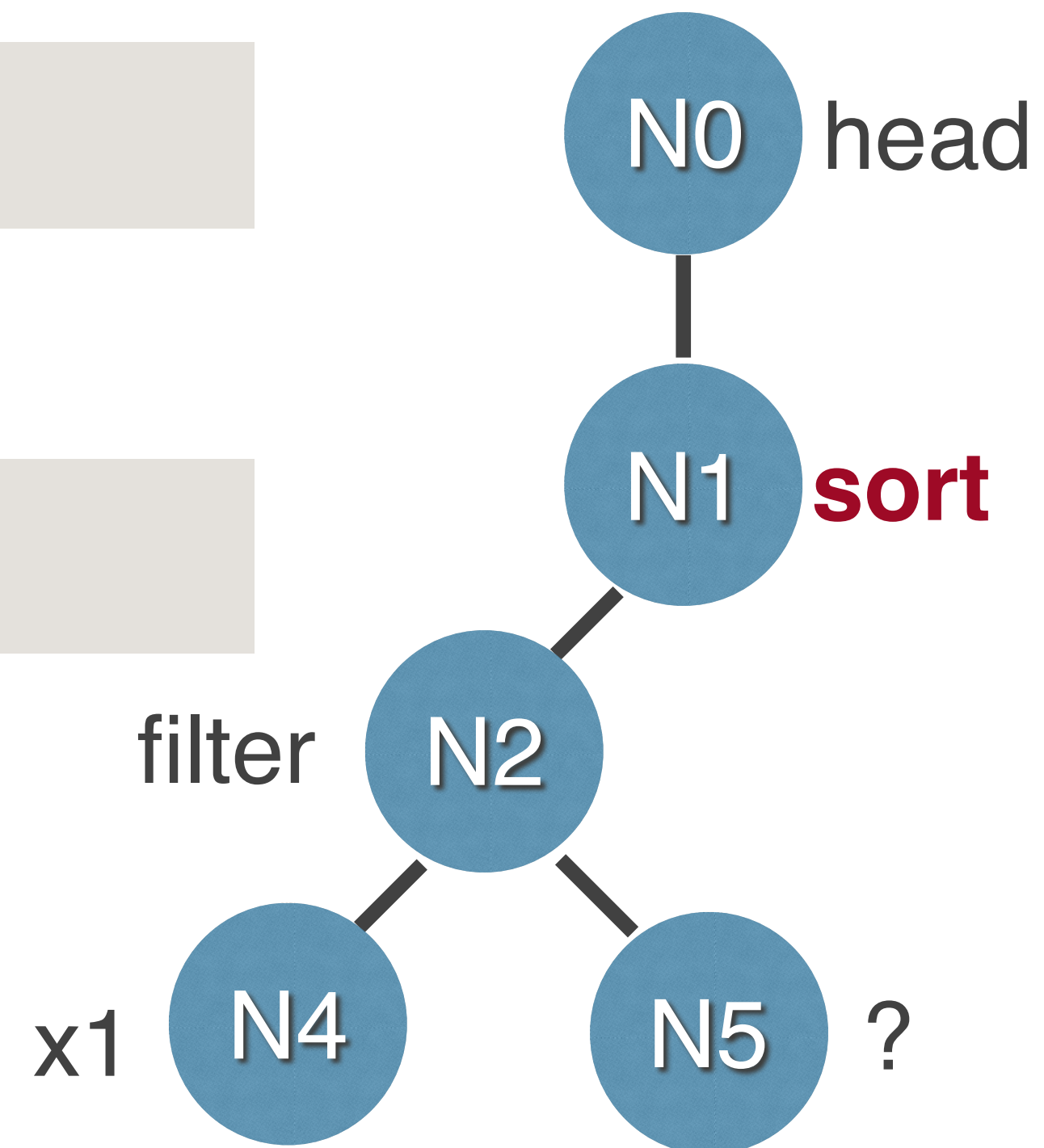
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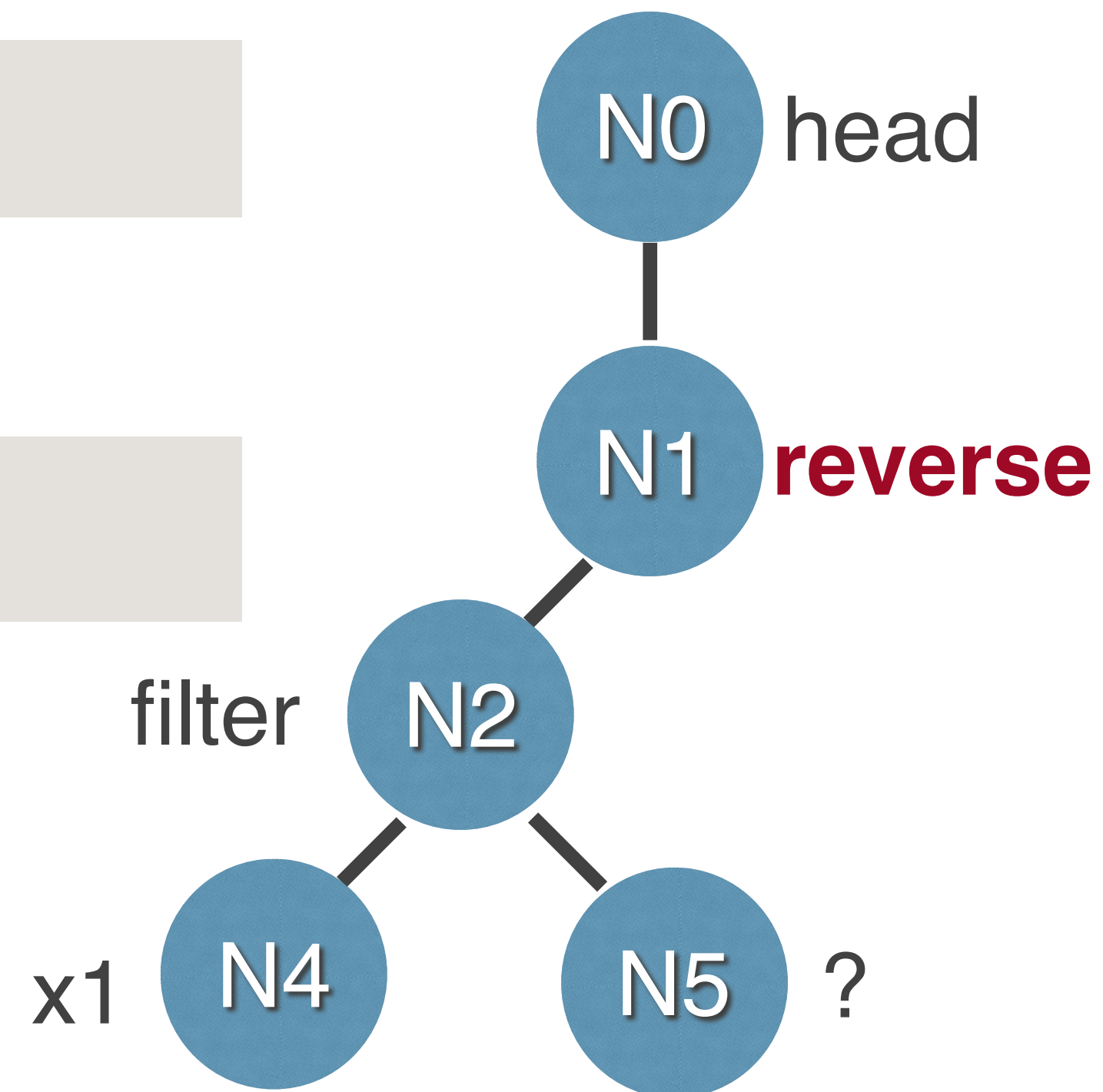
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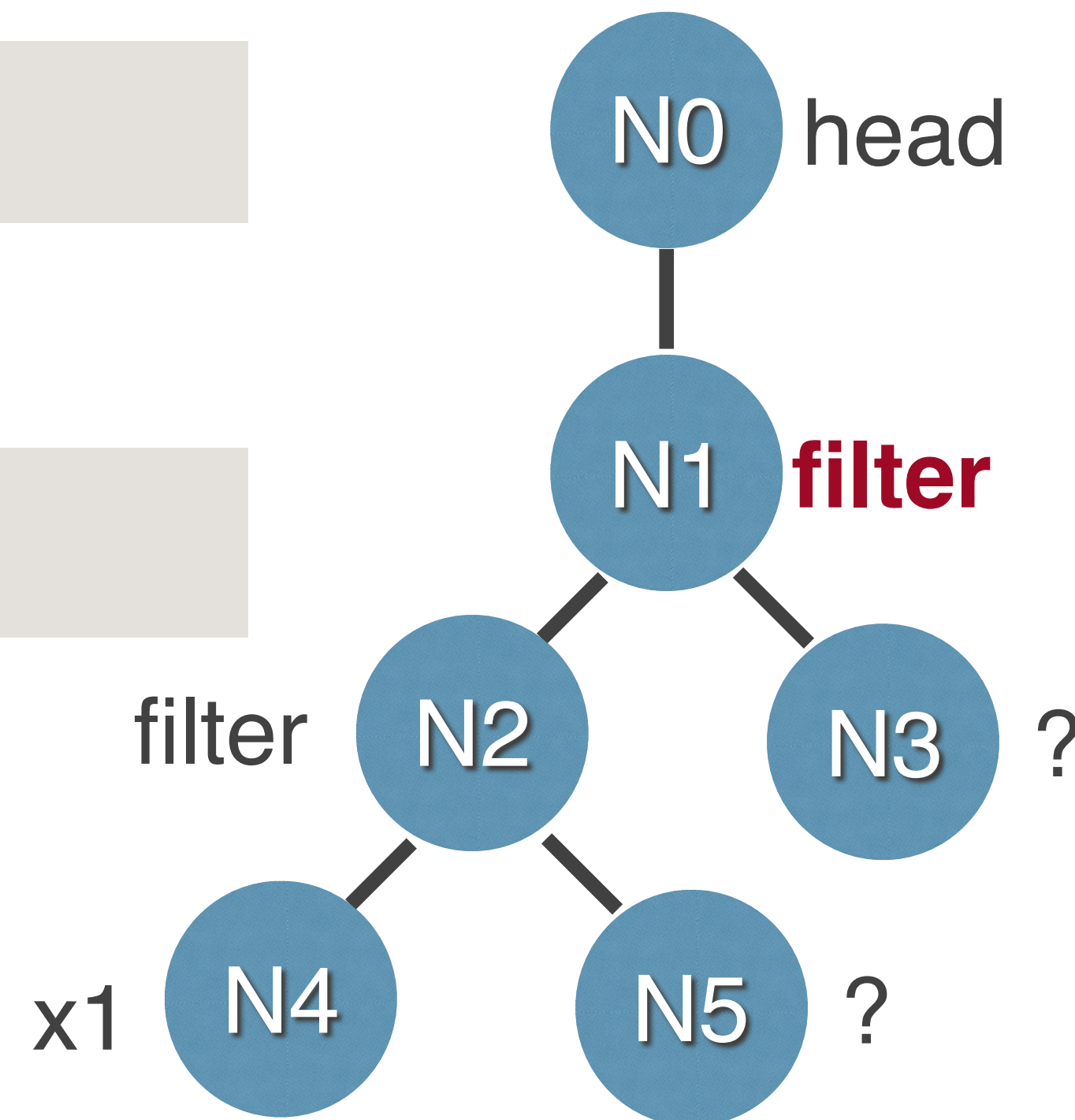
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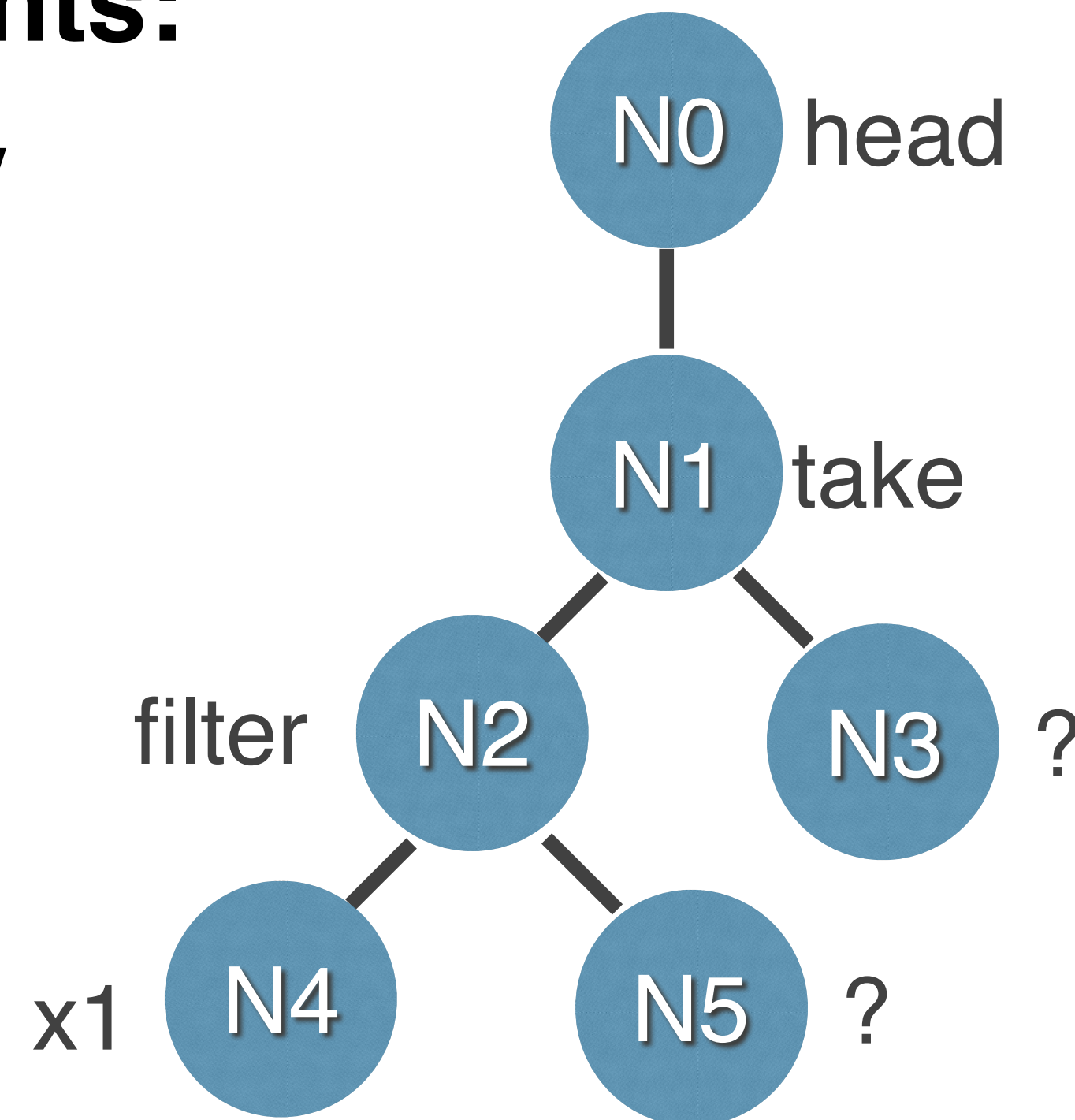


# Learning from Mistakes

**How to detect equivalent modulo conflict components?**

**Using modulo conflict components:**

- We can learn a lemma that allow us to rule out **63** other partial programs!
- Learning allows the synthesis algorithm to avoid similar mistakes in the future!



# Conflict-Driven Synthesis



# Conflict-Driven Synthesis

Search

NO ?

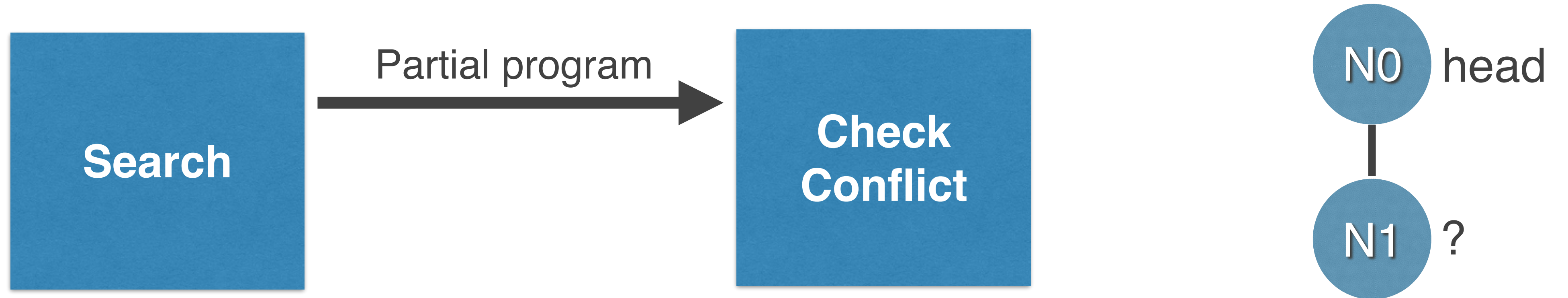




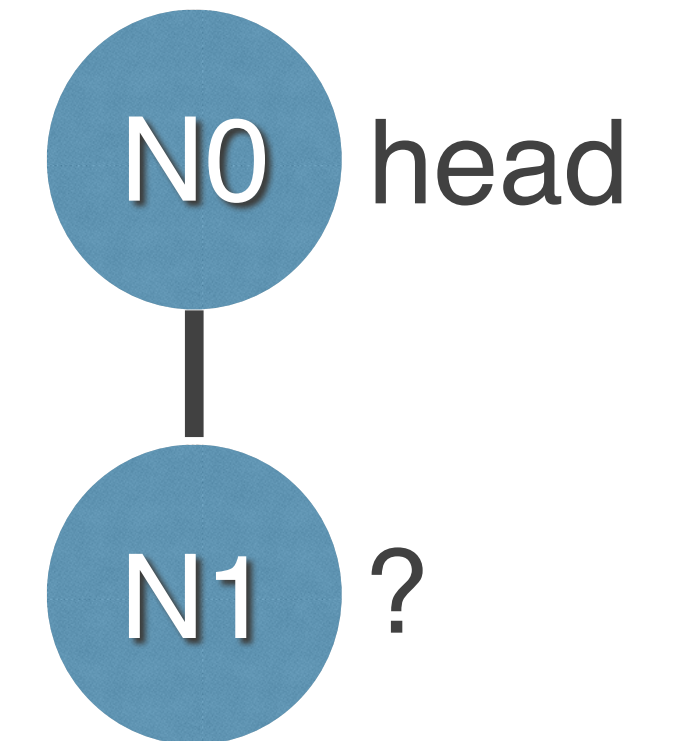
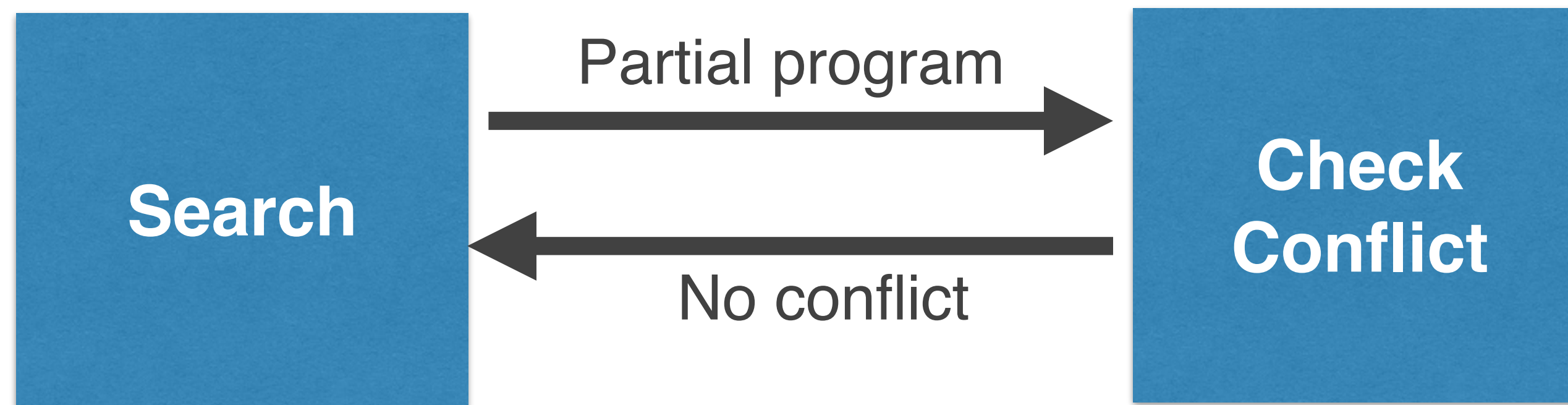
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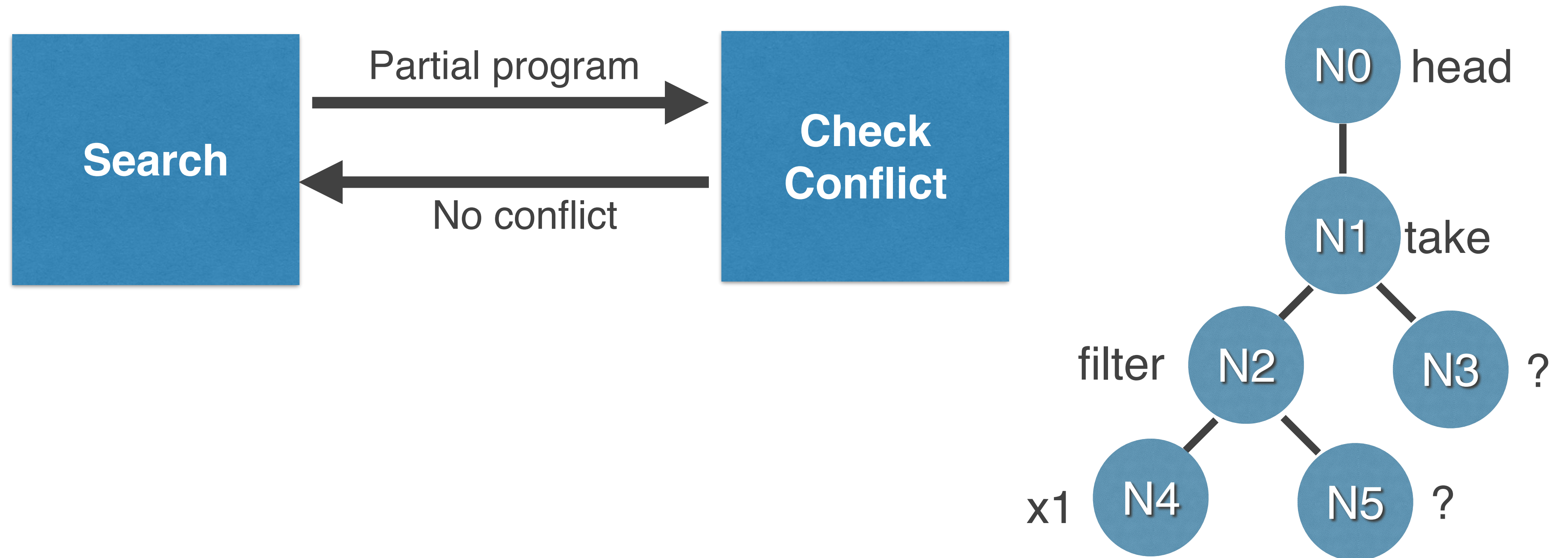
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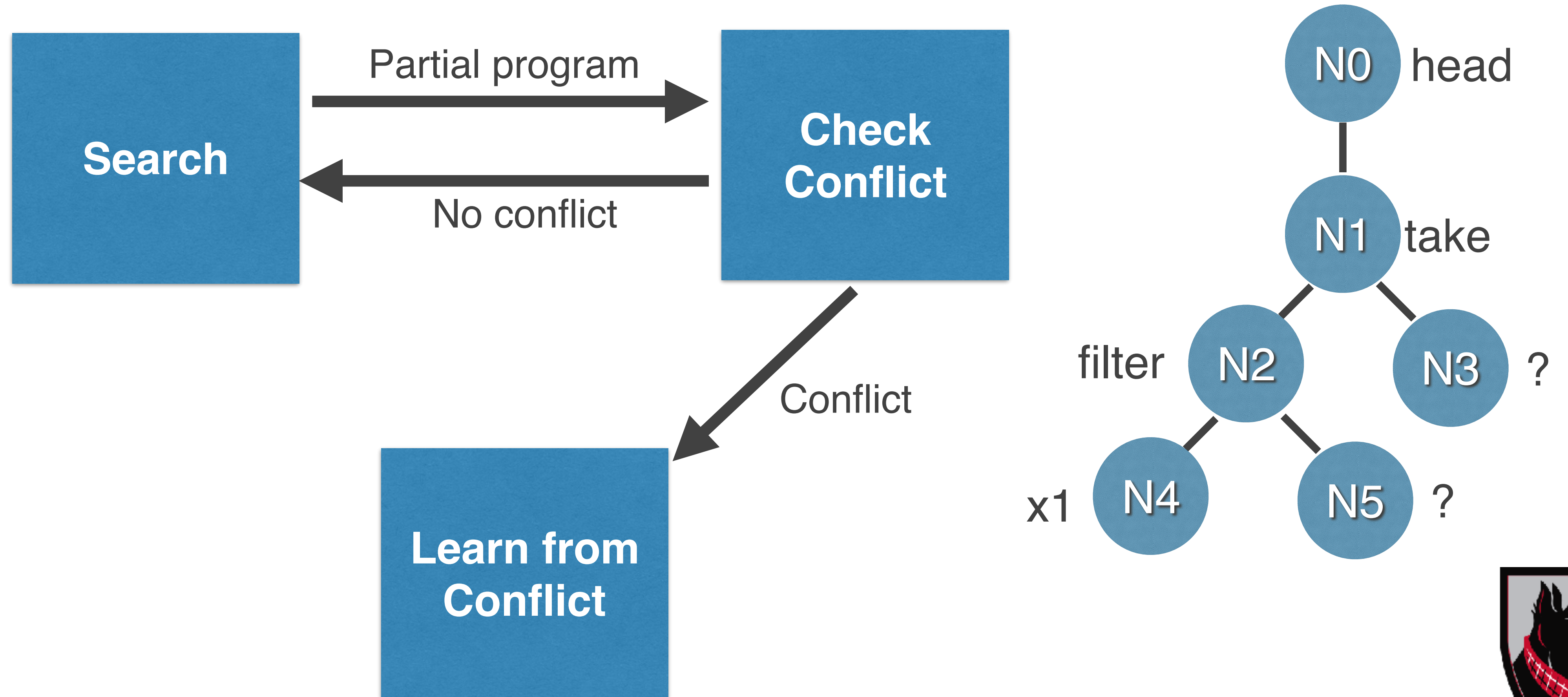
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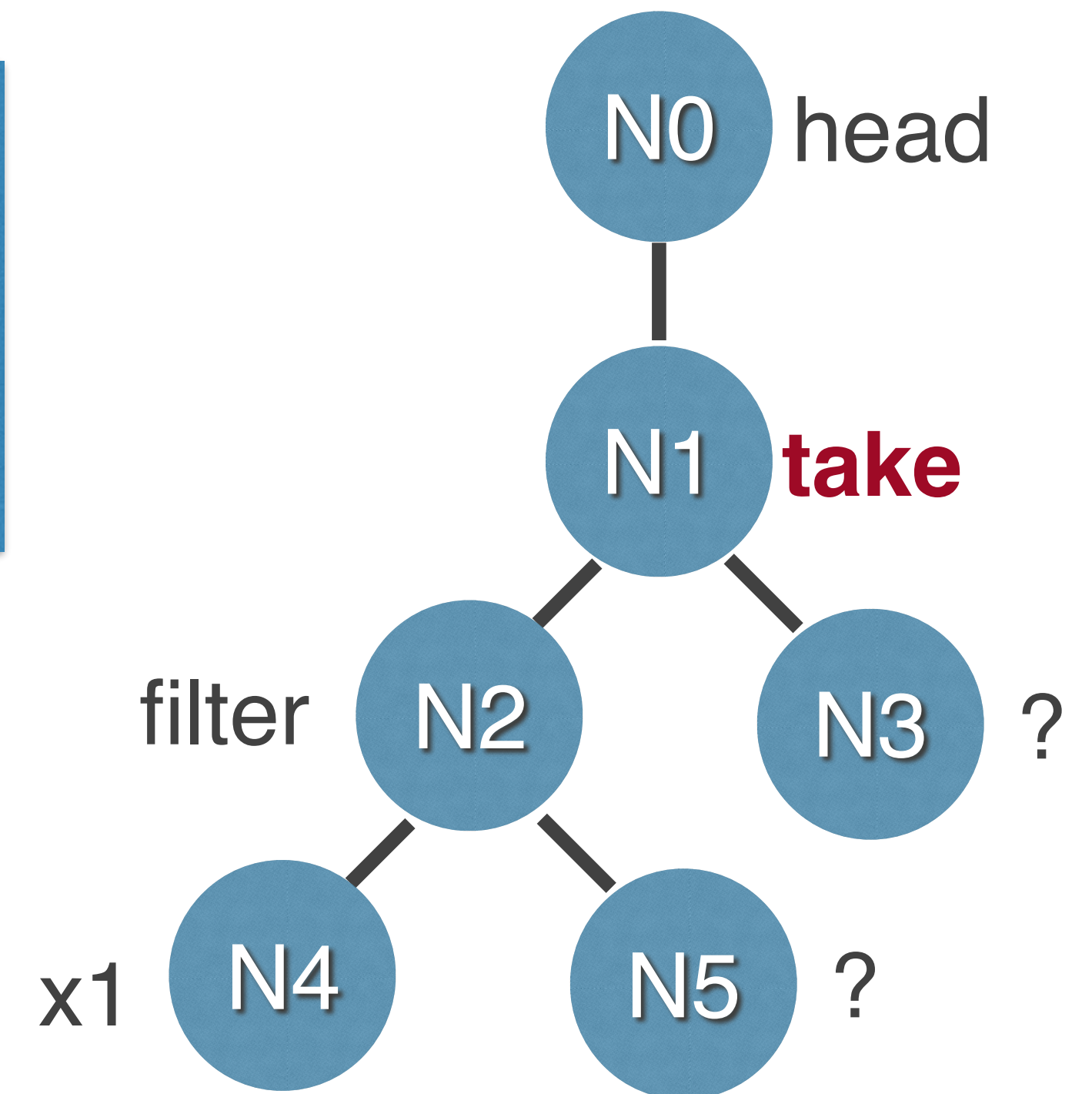
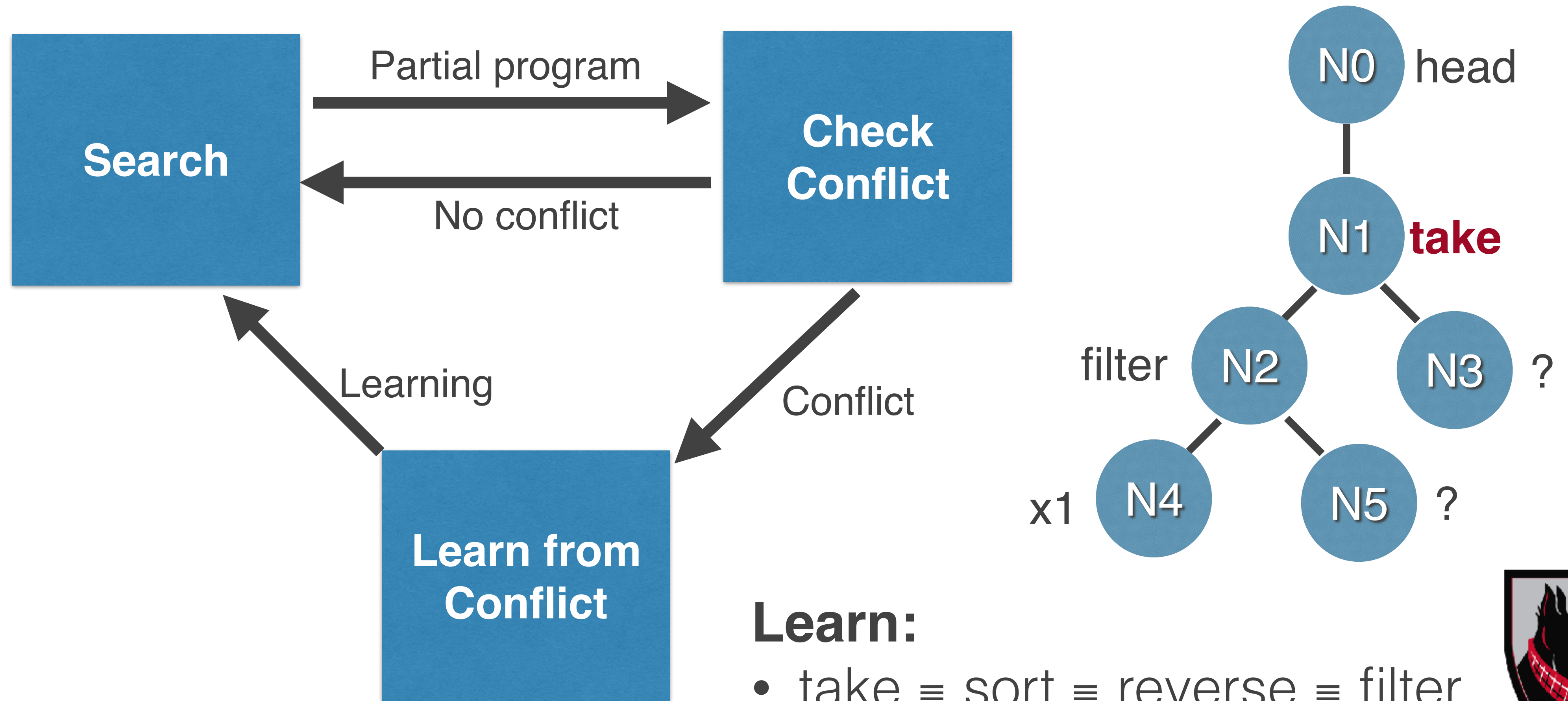
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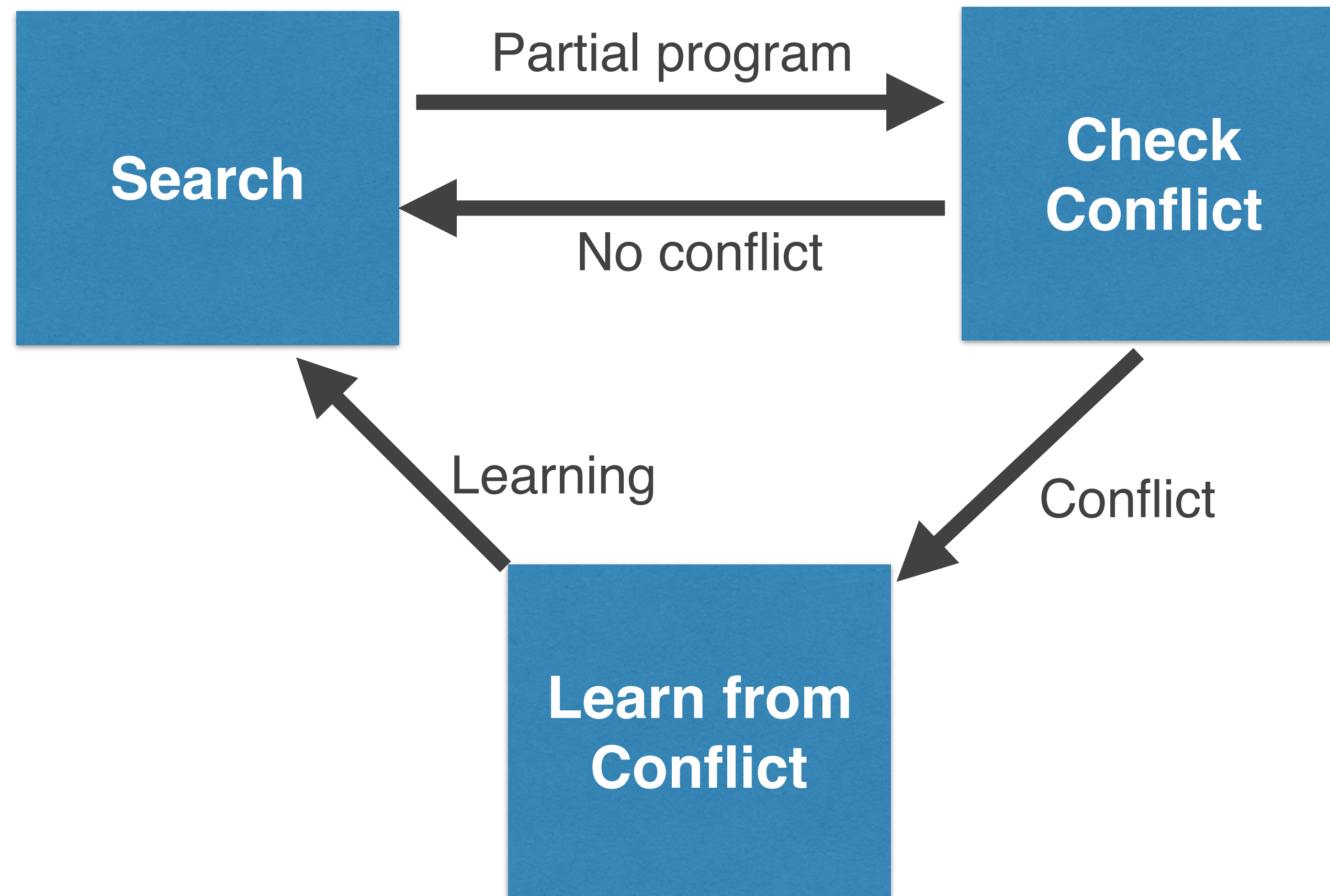


## Learn:

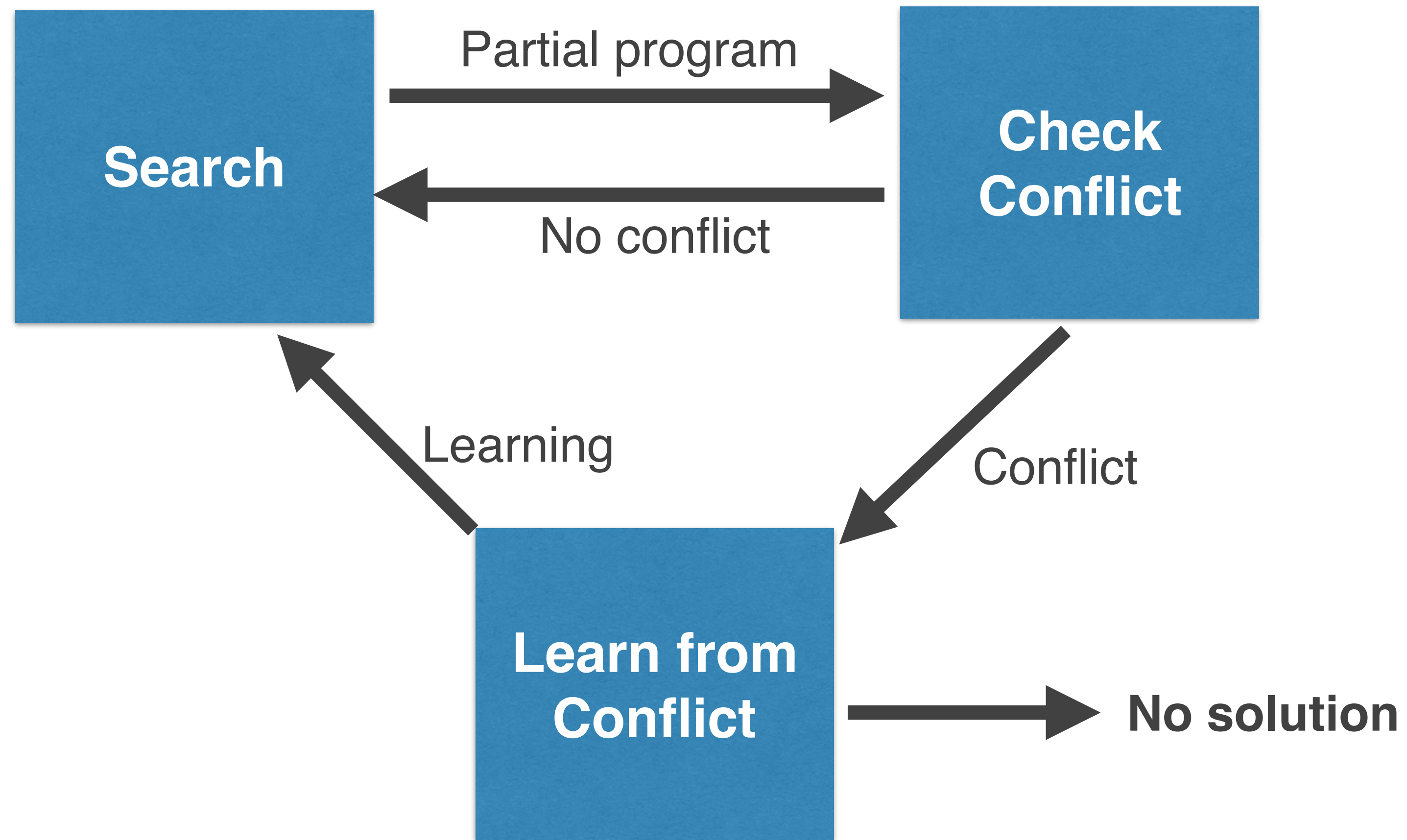
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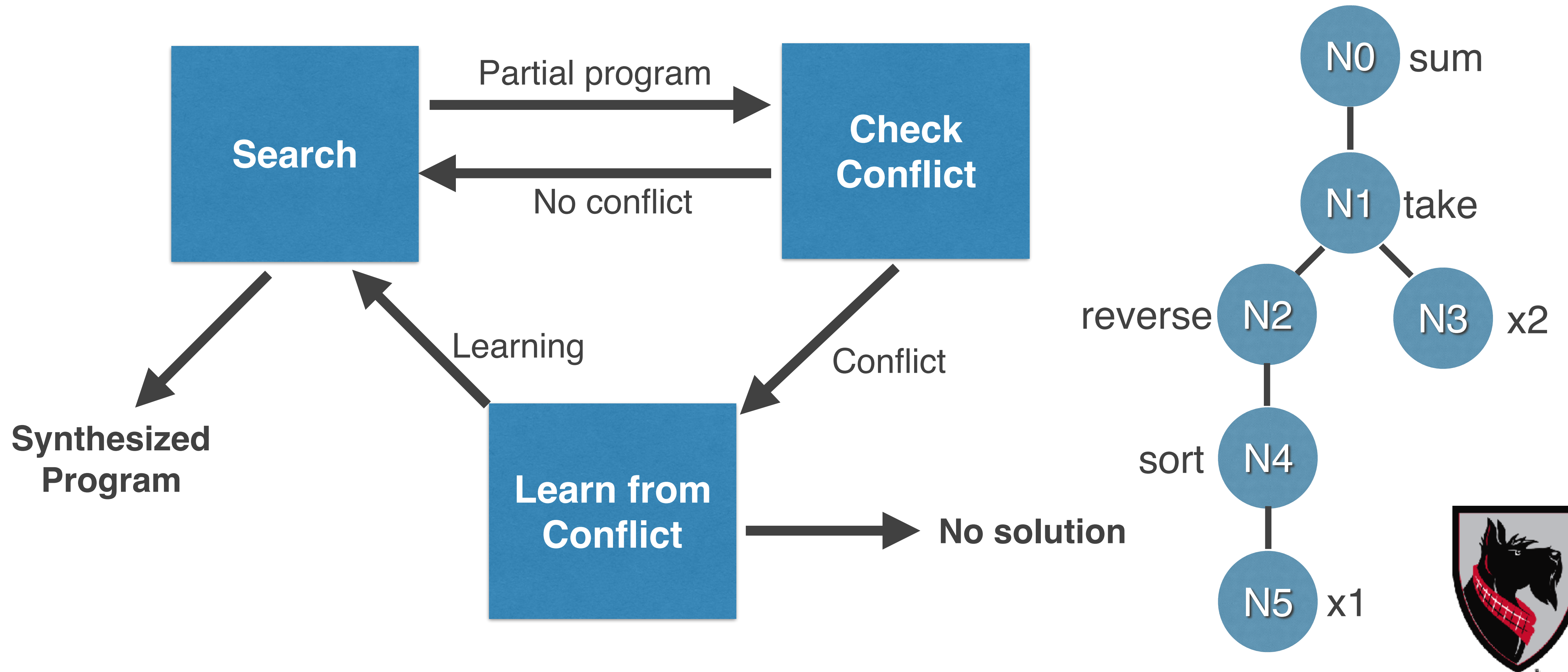


# Conflict-Driven Synthesis





# Conflict-Driven Synthesis



# Experimental Evaluation

## **DeepCoder** (Microsoft Research):

- List manipulation synthesizer
- Uses deep learning to guide the search
- We reimplemented DeepCoder statistical model in our Conflict-Driven Synthesis Framework

## **Benchmarks:**

- 100 challenging benchmarks described in DeepCoder's paper

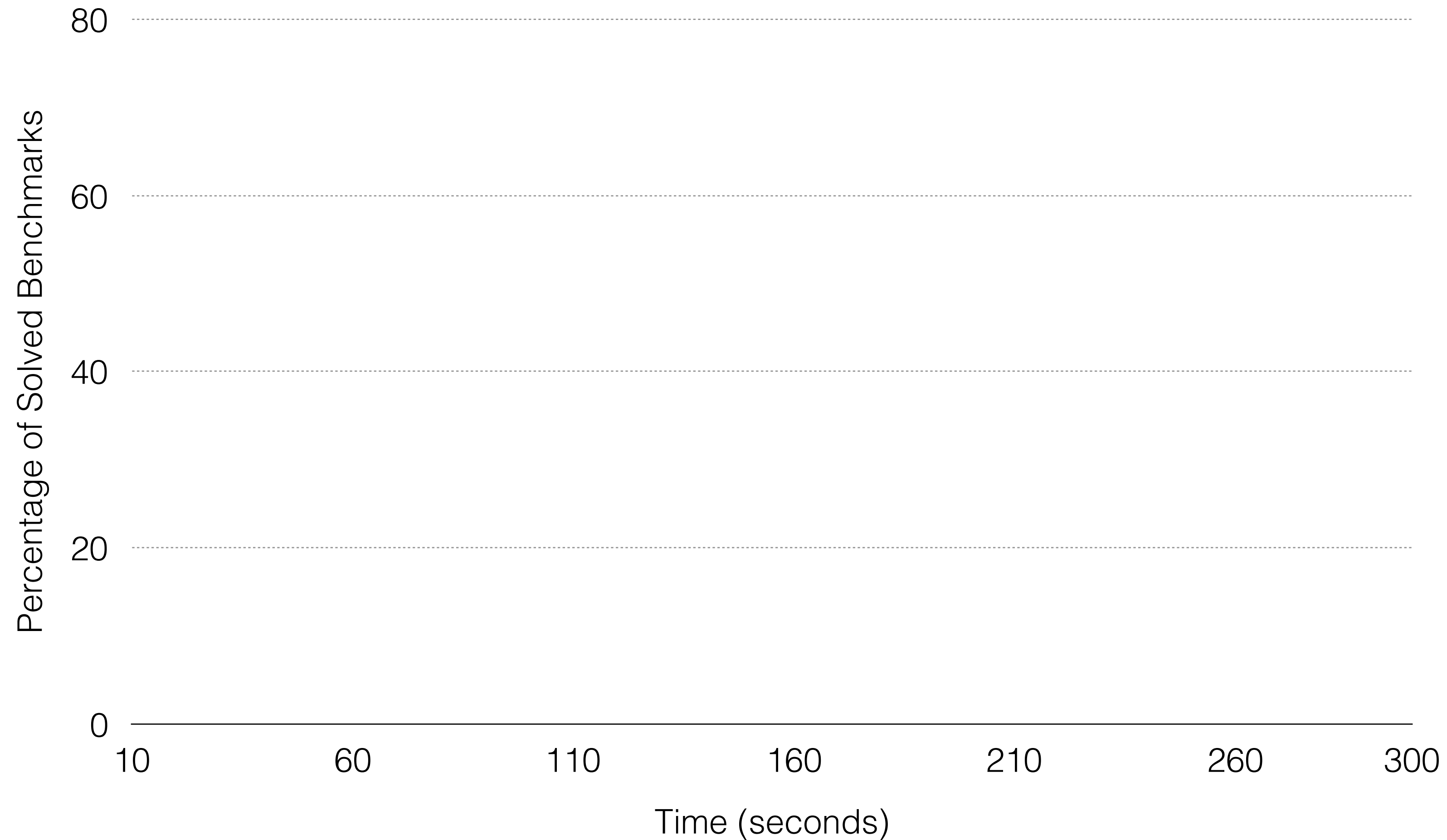


# Neo vs DeepCoder



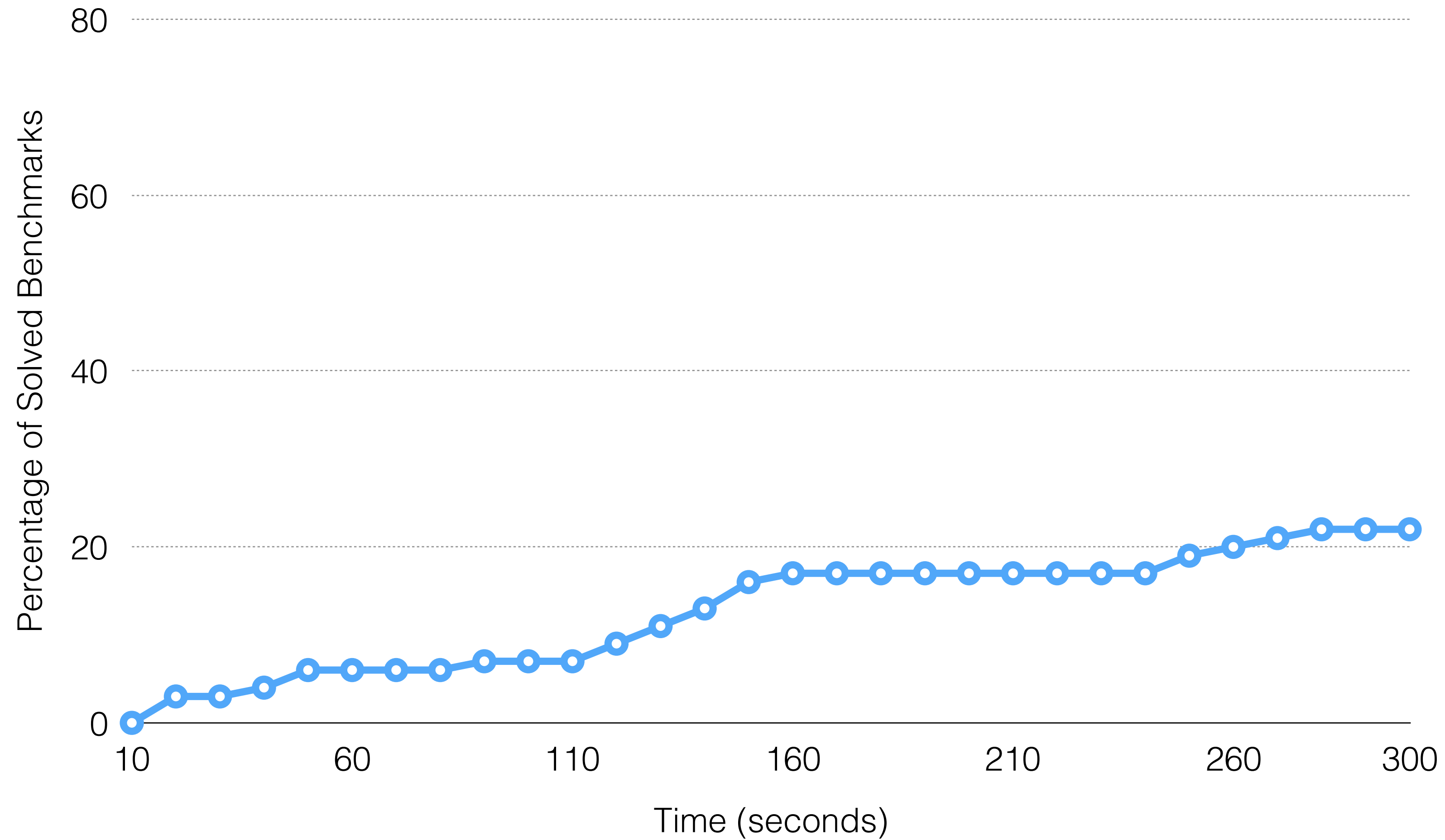
# Neo vs DeepCoder

- Enumeration
- ML + Deduction
- DeepCoder (Machine Learning)
- Neo (ML + Deduction + Logical Learning)

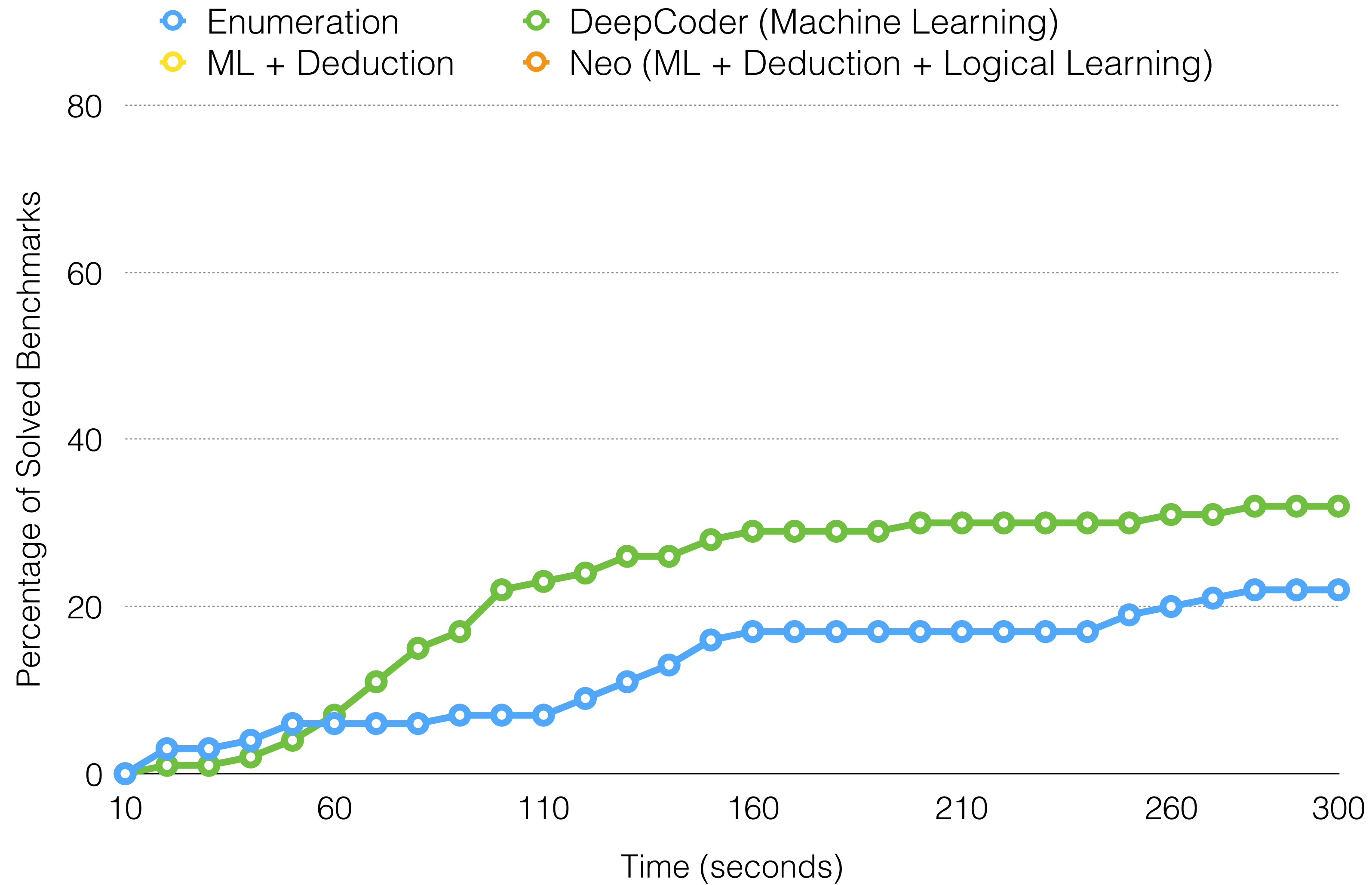


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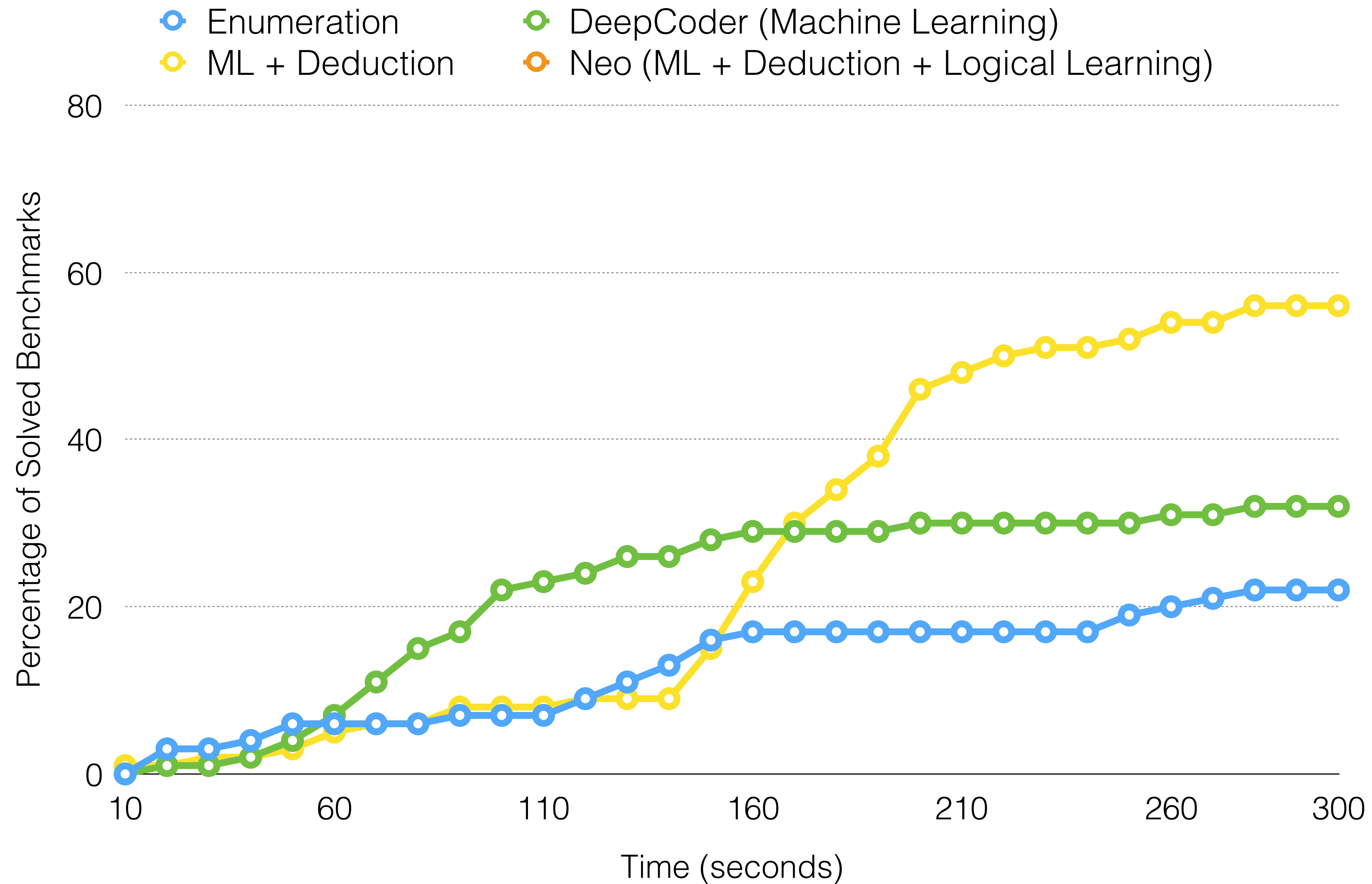
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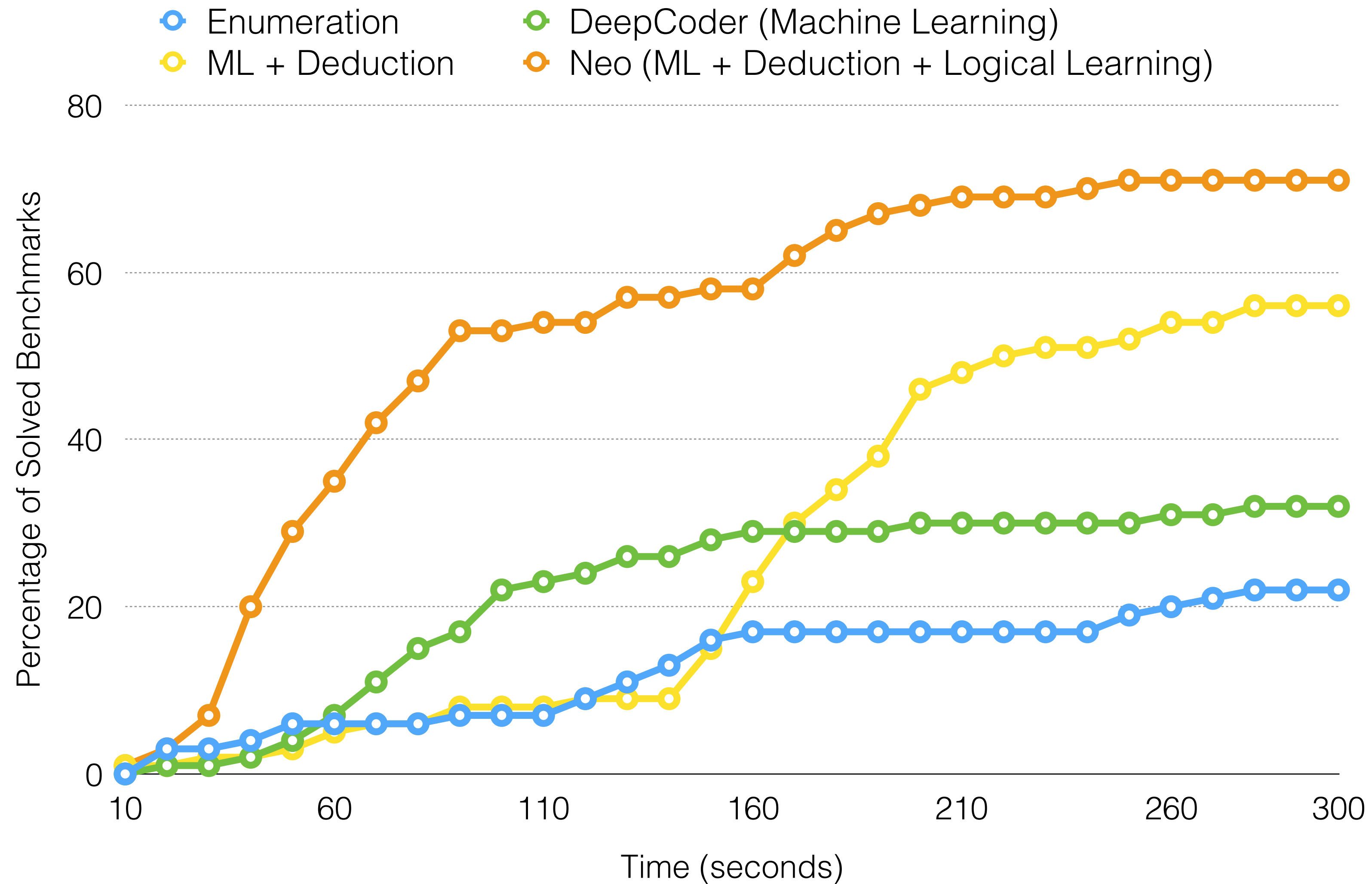
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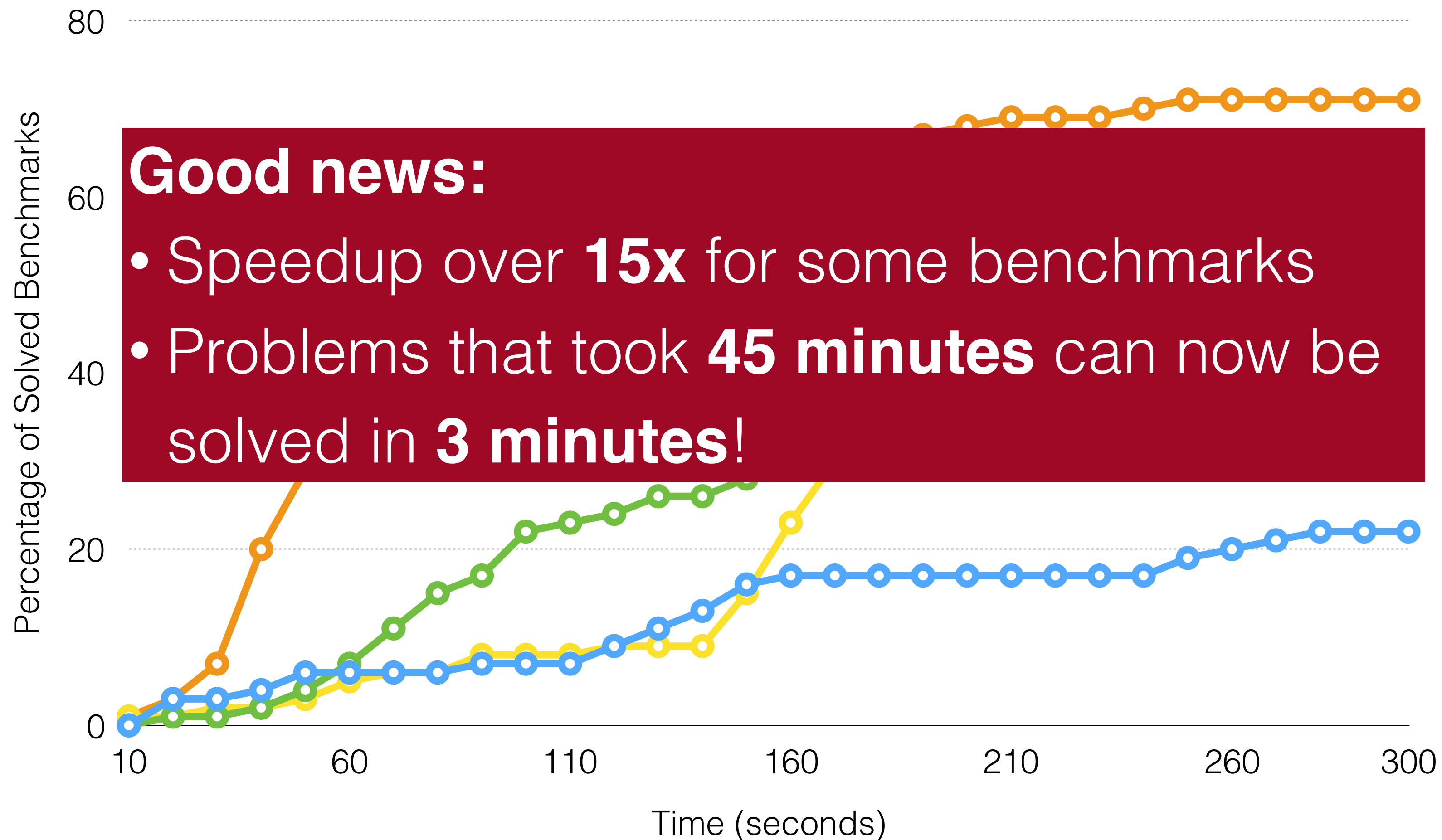
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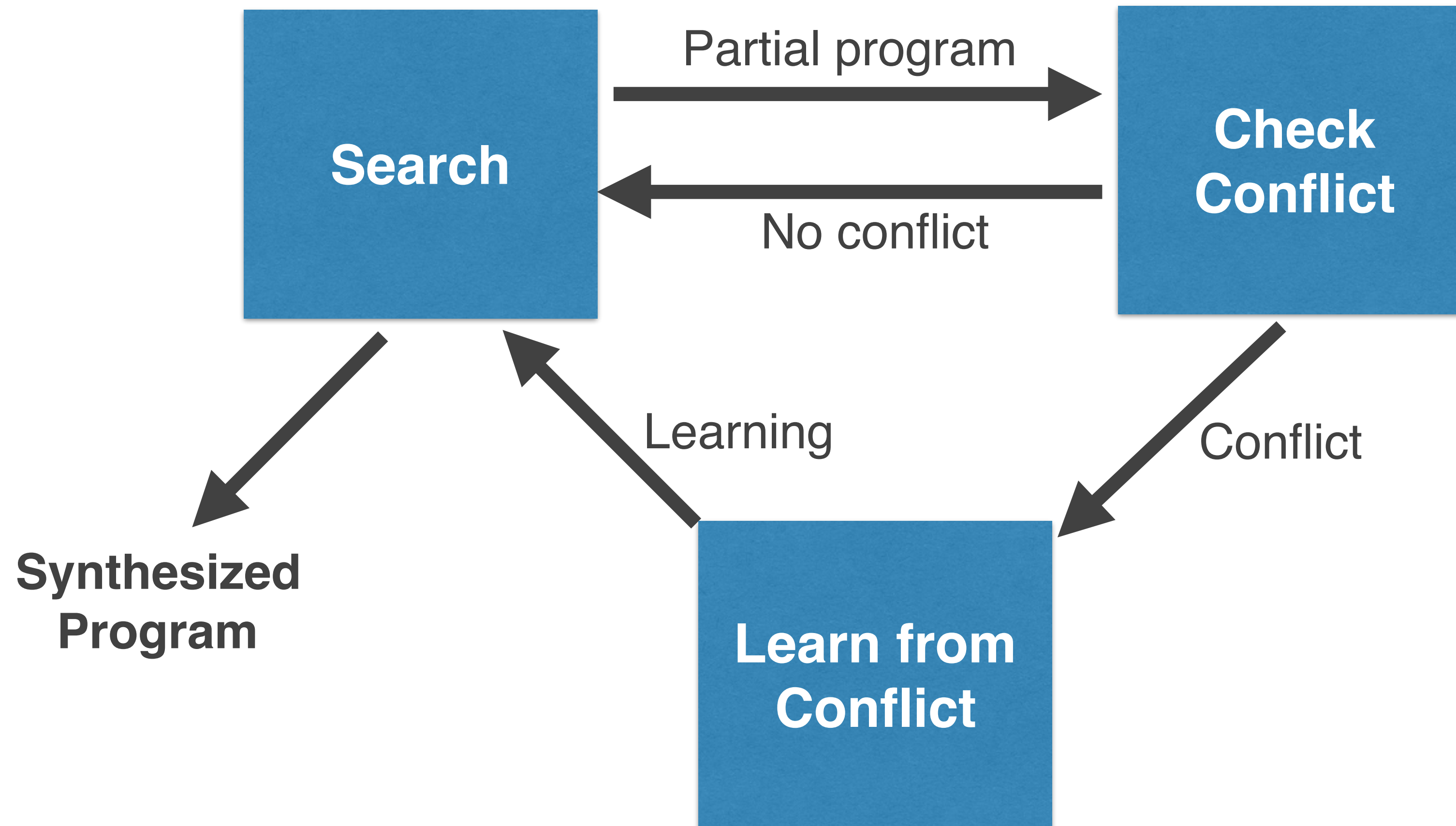


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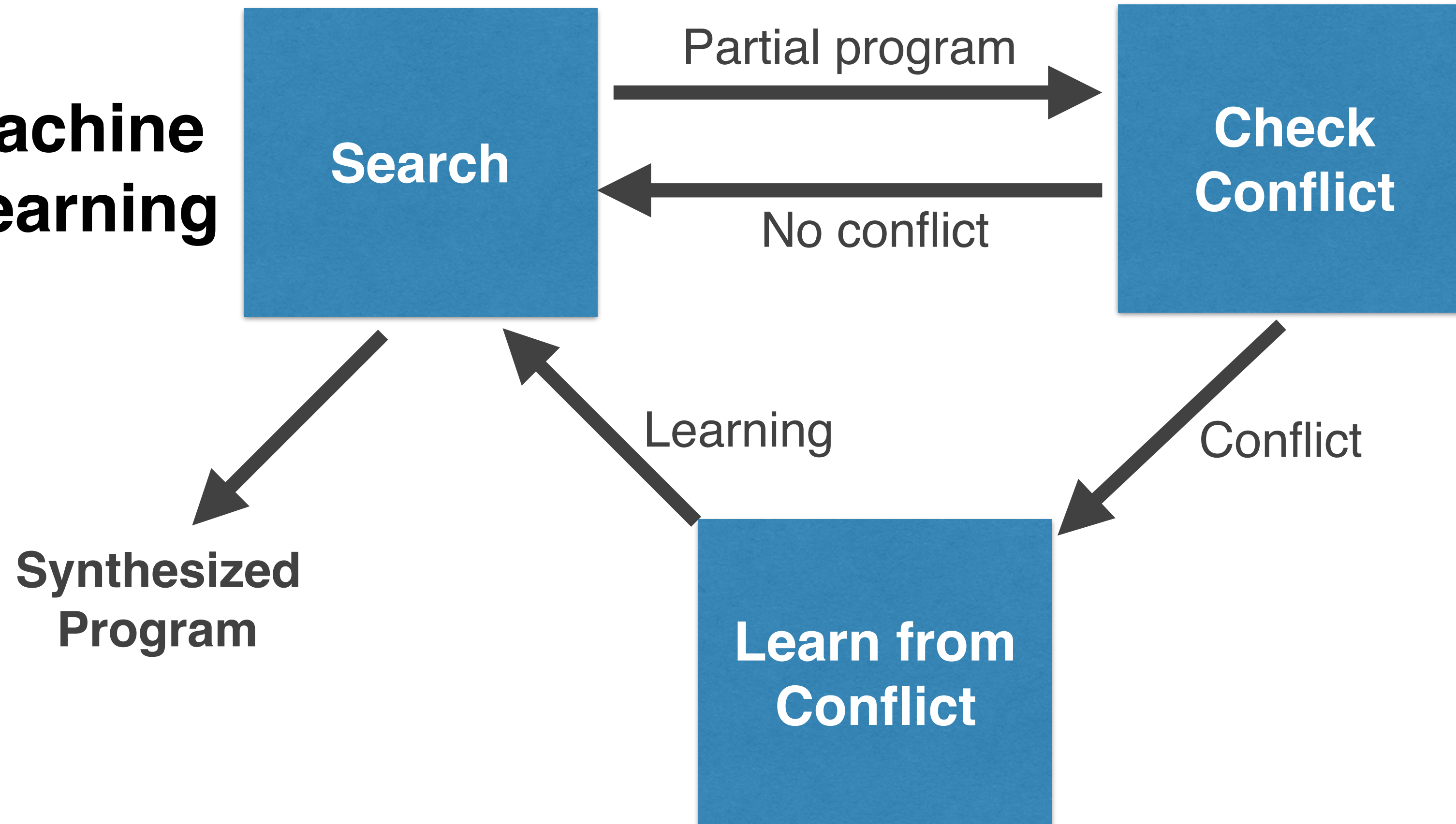
# Neo: Conflict-Driven Synthesis



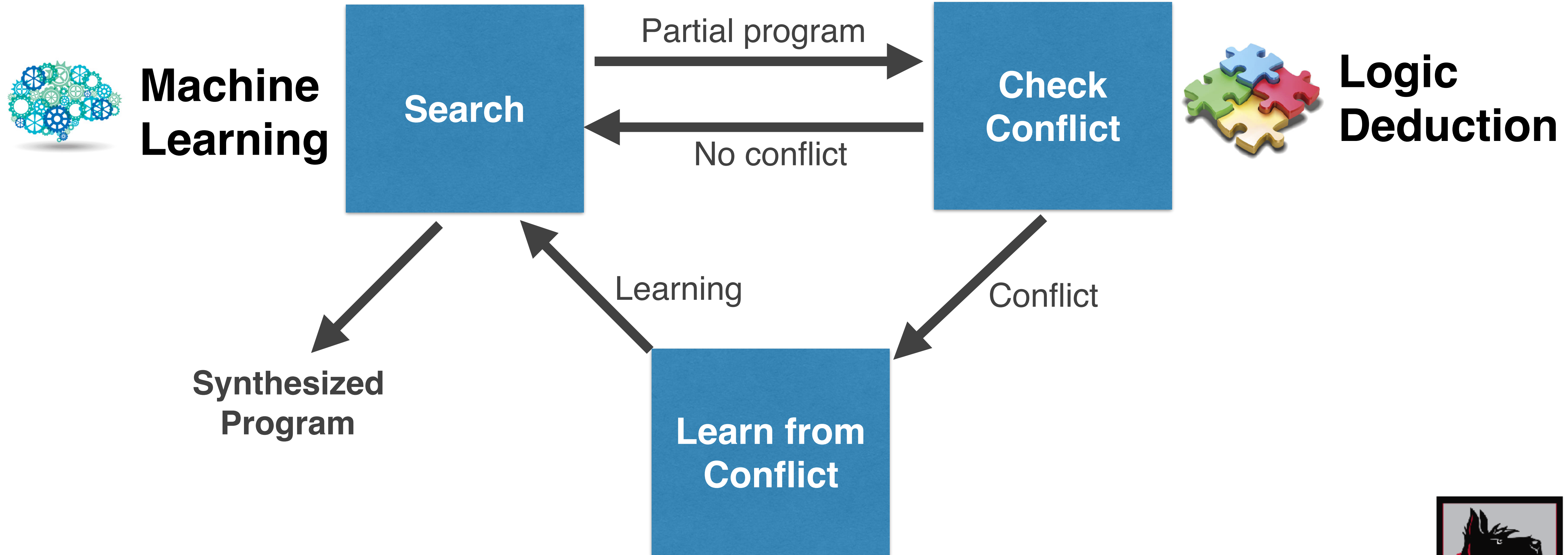
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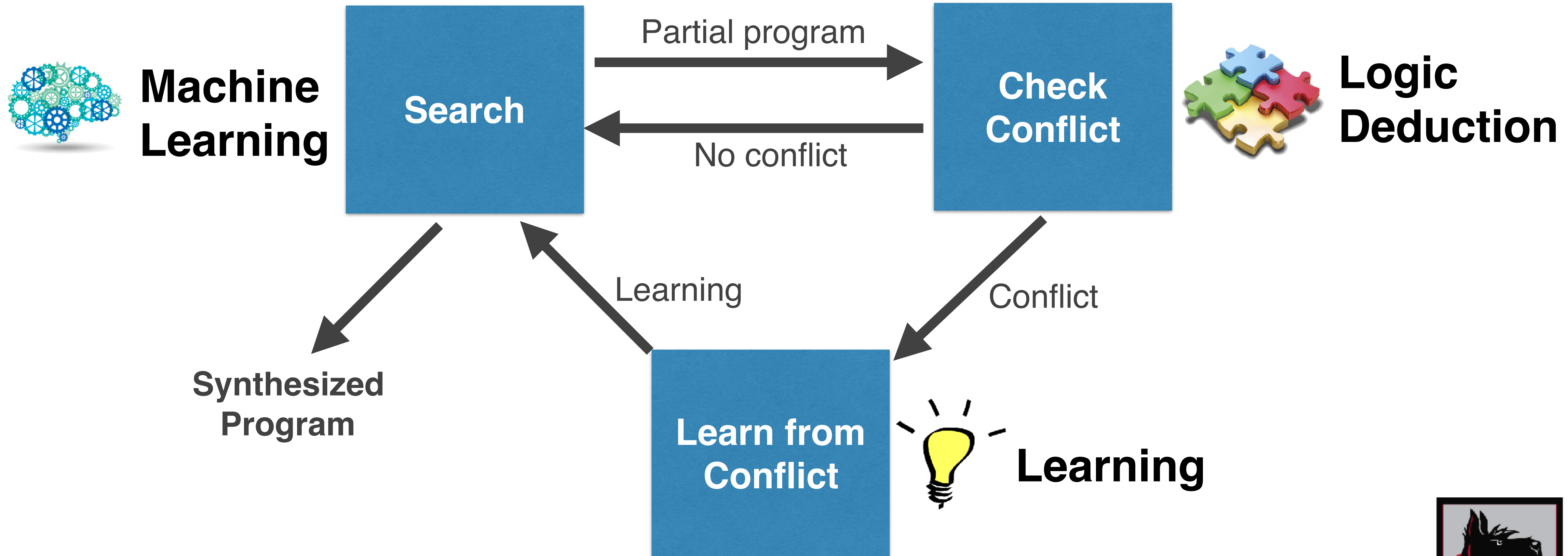
**Machine Learning**



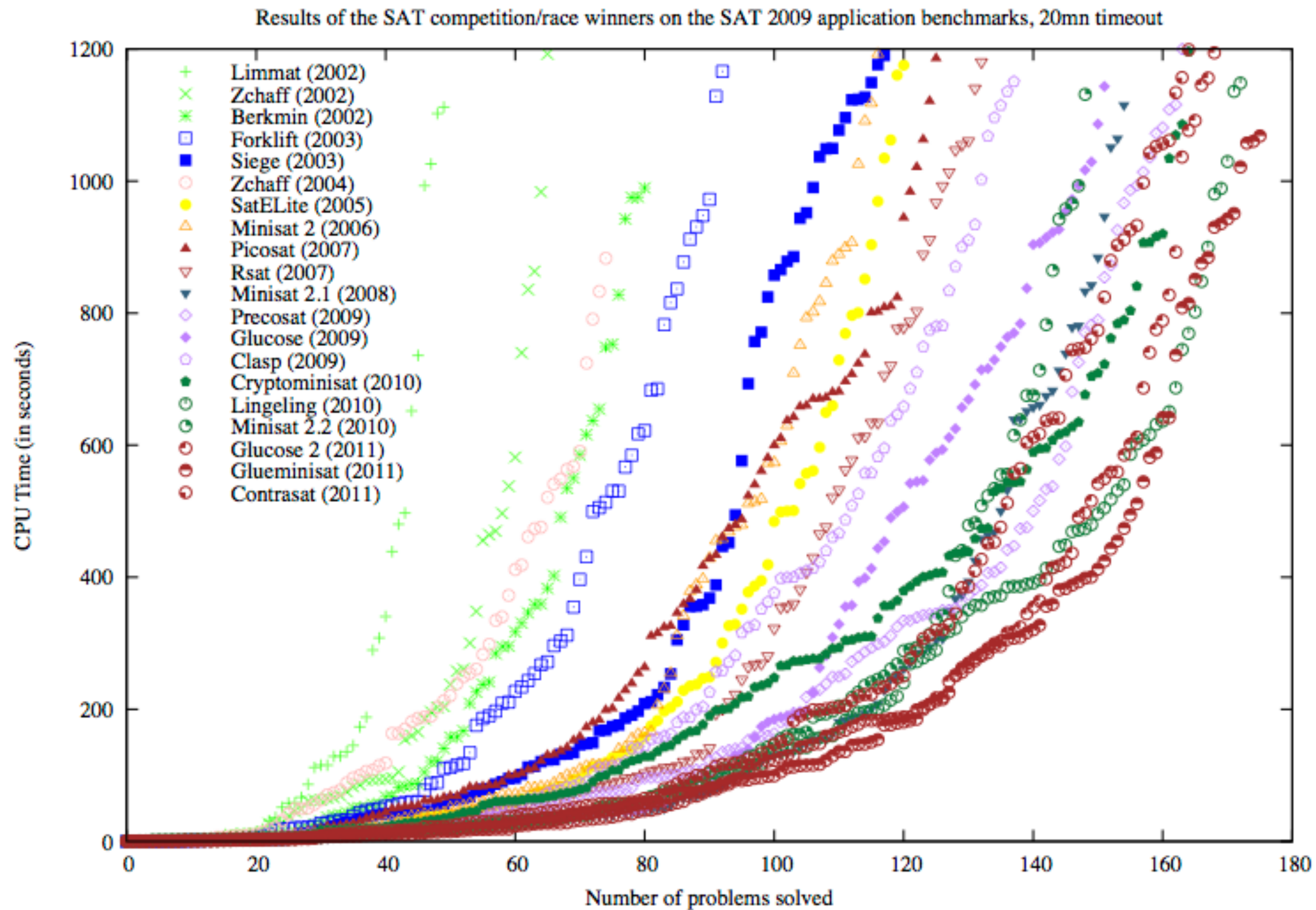
# Neo: Conflict-Driven Synthesis



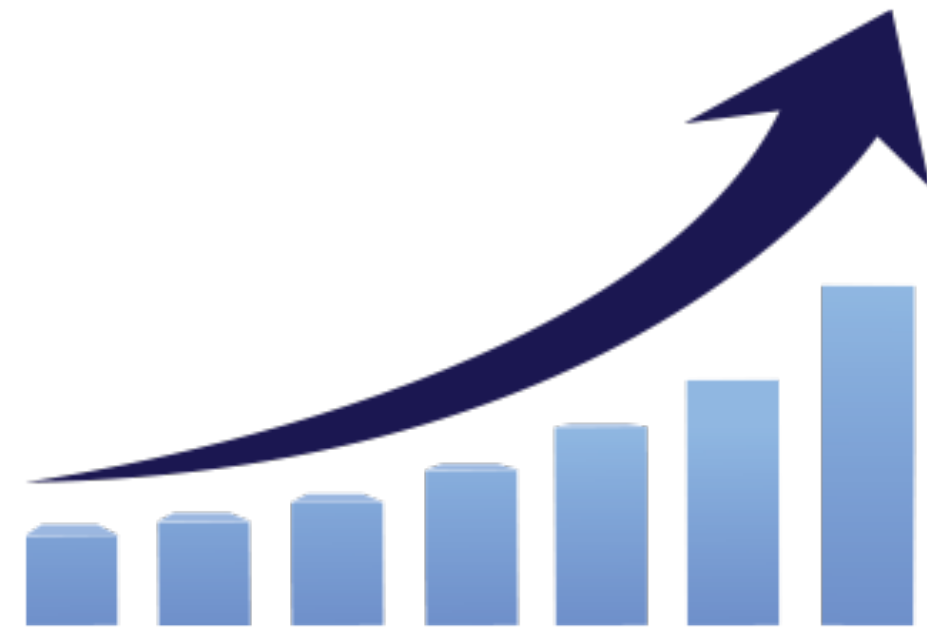
# Neo: Conflict-Driven Synthesis



# Scalability Through Learning



# Scalability of Program Synthesis

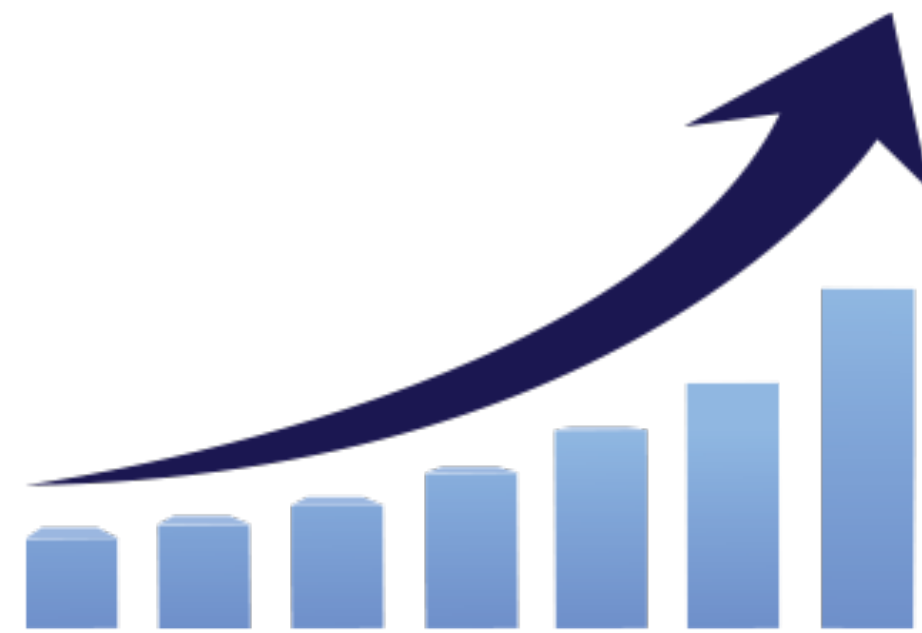


- **SAT Solving:**

- <1996: SAT solving was seen as intractable!
- 1996-now: Conflict-Driven Clause Learning SAT solvers revolutionized the field!



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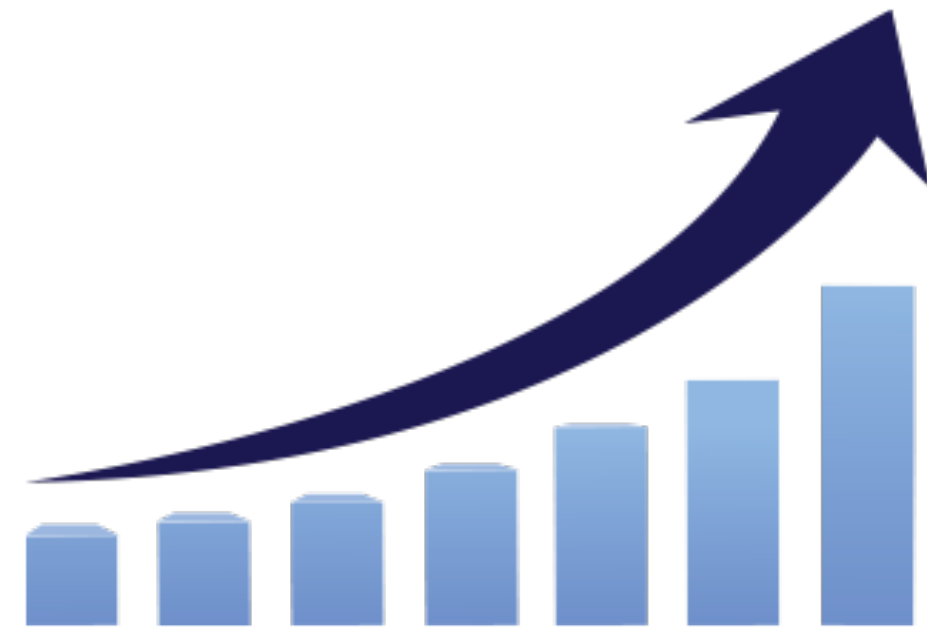
- **Program Synthesis:**

- First step towards learning from mistakes





# Scalability of Program Synthesis



- **SAT Solving:**

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- **Program Synthesis:**

- First step towards learning from mistakes
- Can **learning** push the **boundaries** of program synthesis?



# Applications of Program Synthesis



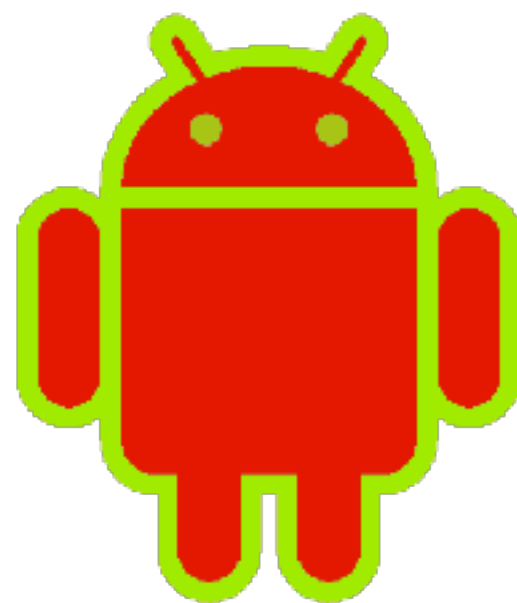
Data Science



Databases



Program Repair



Security



Computer-Aided  
Education



And many others!

