EFFICIENT MODEL BASED DIAGNOSIS WITH MAXIMUM SATISFIABILITY

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- 1. Model-based diagnosis
- 2. Dominator-oriented encoding
- 3. ITC99 benchmark instances
- 4. Experimental results
- 5. Summary and future work







Comps $\triangleq \{Z_1, Z_2, Z_3, Z_4, O_1, O_2\}$

 \mathcal{F}_{Z_2}

 \mathcal{F}_{Z_3}

 \mathcal{F}_{Z_4}

 \mathcal{F}_{O_1}

$$\mathcal{F}_{z_1} \triangleq \mathsf{CNF}(z_1 \leftrightarrow \neg(i_1 \wedge i_3))$$

- $\triangleq \mathsf{CNF}(z_2 \leftrightarrow \neg(i_3 \wedge i_4))$
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S

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$$\mathsf{D} \triangleq \bigwedge_{\mathsf{c}\in\mathsf{Comps}}(\mathsf{Ab}(\mathsf{c})\vee\mathfrak{F}_{\mathsf{c}})$$

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 $Obs = \{ \langle i_1, i_2, i_3, i_4, i_5 \rangle = \langle 1, 0, 1, 1, 1 \rangle, \quad \langle o_1, o_2 \rangle = \langle 0, 1 \rangle \}$



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Obs = { $\langle i_1, i_2, i_3, i_4, i_5 \rangle$ = $\langle 1, 0, 1, 1, 1 \rangle$, $\langle 0_1, 0_2 \rangle$ = $\langle 0, 1 \rangle$ }

 \mathcal{F}_{Z_2}





 $\begin{array}{rcl} \mathsf{Comps} & \triangleq & \{z_1, z_2, z_3, z_4, o_1, o_2\} \\ & \mathsf{SD} & \triangleq & \bigwedge_{c \in \mathsf{Comps}}(\mathsf{Ab}(c) \lor \mathscr{F}_c) \\ & \mathsf{Obs} & \triangleq & \{i_1, \neg i_2, i_3, i_4, i_5, \neg o_1, o_2\} \\ & \mathsf{SD} \land \mathsf{Obs} \land \bigwedge_{c \in \mathsf{Comps}} \neg \mathsf{Ab}(c) \vDash \bot \end{array}$



 \checkmark

 $\begin{aligned} & \text{find } \Delta \subseteq \text{Comps s.t.} \\ & \text{SD} \land \text{Obs} \land \bigwedge_{c \in \Delta} \text{Ab}(c) \land \bigwedge_{c \in \text{Comps} \setminus \Delta} \neg \text{Ab}(c) \nvDash \bot \end{aligned}$



 $\mathbf{+}$

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 $\Delta = \{Z_2, O_1\}$



➡

find $\Delta \subseteq \text{Comps s.t.}$ SD \land Obs $\land \bigwedge_{c \in \Delta} Ab(c) \land \bigwedge_{c \in \text{Comps} \setminus \Delta} \neg Ab(c) \nvDash \bot$ $\Delta = \{z_2, o_1\}$ — minimize Δ with MaxSAT

DOMINATOR-ORIENTED ENCODING



v *dominates* $u \iff all$ paths from u to O include v



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v *dominates u* \iff *all* paths from *u* to *O* include *v*

diagnosis Δ is a TLD if it *does not contain* dominated gates



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z₁ is *dominated* and its output is *fixed*





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FILTERED EDGES AND NODES



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e is blocked or its fanout node is filtered




























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A node is *filtered* if all of its fanout edges are *filtered*



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- 1 **global:** (SD, Comps, Obs)
- 2 repeat

6

- 3 FindDominators()
- 4 FindBackboneComponents()
- 5 FindBlockedConnections()
 - if MaxNumberIterations(): break
- 7 until NoMoreChanges()
- 8 GenMaxsatModel()

Algorithm 1: MBD to MaxSAT compilation

1. computing dominators

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possible structural decompositions

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subproblems can be solved separately

Standard way to compute Δ :

- 1. $\sum_{c \in \text{Comps}} Ab(c) \leq k$
- 2. iterate over k

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• |Comps| is large (up to millions)

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core-guided MaxSAT can exploit this:

- $Ab(c) = 0 \quad \forall c \in Comps$ by default
- relax on demand, i.e. Ab(c) = 1 when needed

ITC99 BENCHMARK INSTANCES



new challenging suite - ITC99:



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• 8 ITC99 circuits



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• -2097 instances (hard for SATbD/SCryptoDiagnoser) = 5903

EXPERIMENTAL RESULTS

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 - 1. ISCAS85 (16174 instances)
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ISCAS85 SUITE



16174 instances	scrypto	eva	wboinc
% solved	100.0	100.0	100.0
% scrypto wins	_	23.4	0.1
% eva wins	76.6	—	0.0
% wboinc wins	99.9	100.0	—

Table 1: Statistics for ISCAS85 suite



Figure 2: Cactus plot for ITC99 suite



Figure 3: Scatter plots for ITC99 suite

5903 instances	scrypto	eva	wboinc
% solved	62.4	89.7	90.6
% scrypto wins	_	2.2	0.4
% eva wins	97.8	_	13.4
% wboinc wins	99.6	86.6	—

Table 2: Statistics for ITC99 suite

SUMMARY AND FUTURE WORK

• new DOE approach to MBD:

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- new challenging MBD suite (5903 instances)
- further optimizations for the DOE
- application to other related practical problems

QUESTIONS?